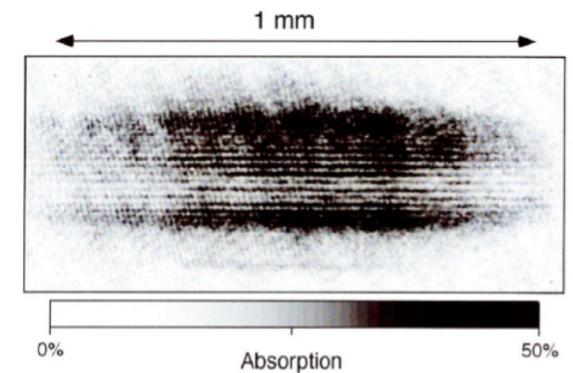
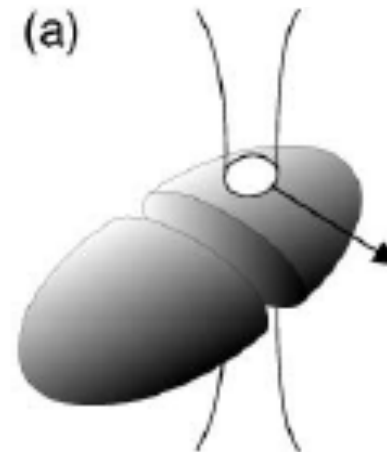
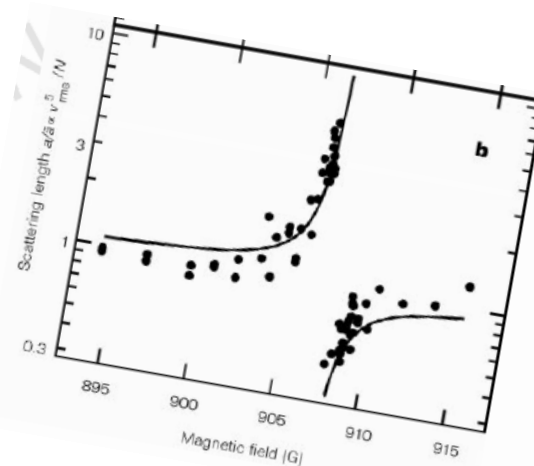
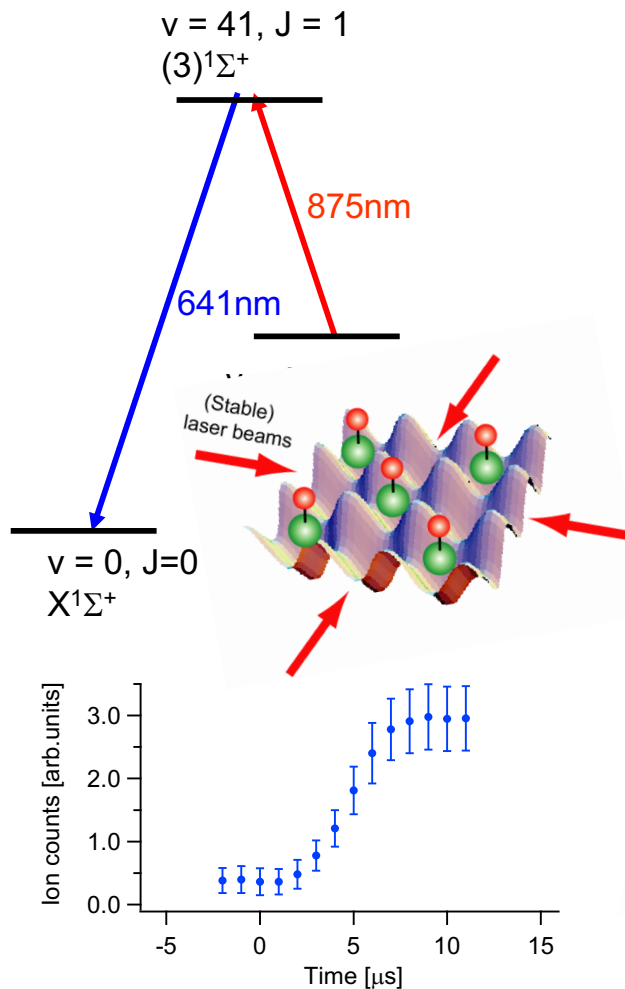


# *What can we do with a quantum degenerate mixture ?*

Shin Inouye  
Osaka City University



# *Outline*

*How to cool atoms*

*Properties of BEC*

*Tuning interactions (Feshbach resonance)*

*Cold molecules*

*Conclusion and Outlook*



Everybody loves to cool liquids ...

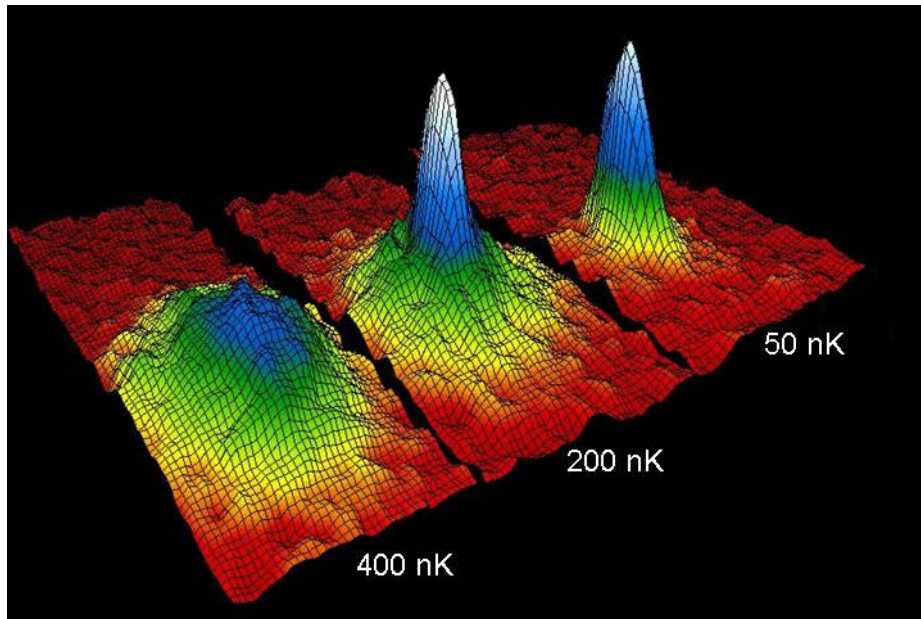


but, we are interested in cooling gases!

# Significance of cold atom research

“Ideal system” to study Condensed Matter Physics!

Produced in 1995



Anderson et al., Science, 269 198 (1995)

Awarded in 2001  
(Cornell, Ketterle, Wieman)







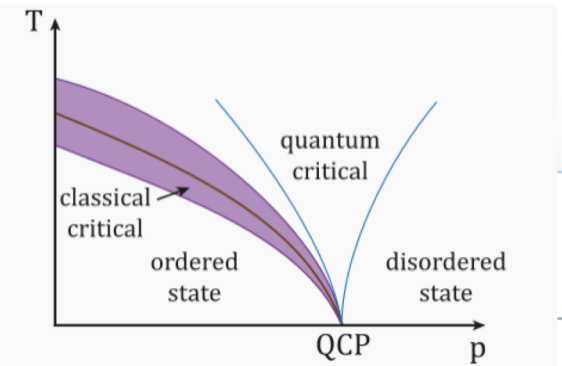
WIKIPEDIA  
The Free Encyclopedia

Article

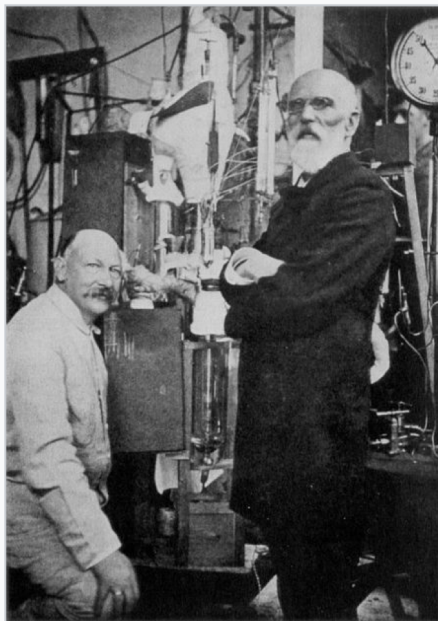
Talk

# Condensed matter physics

From Wikipedia, the free encyclopedia



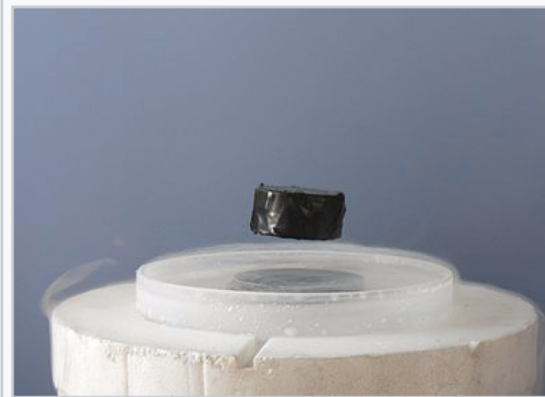
Phases · Phase transition · QCP



Heike Kamerlingh Onnes and Johannes van der Waals with the helium liquefactor at Leiden in 1908



A replica of the first point-contact transistor in Bell labs



A magnet levitating above a high-temperature superconductor. Today

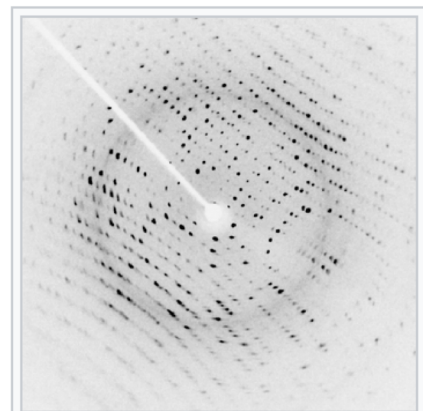
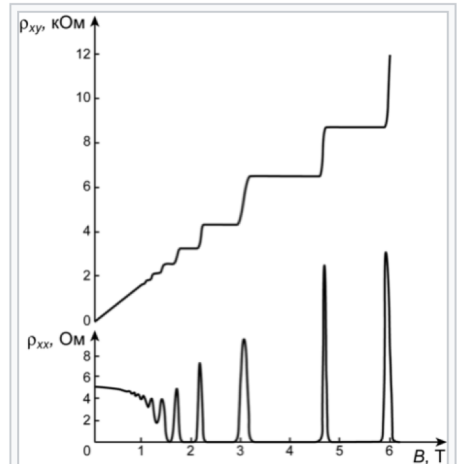
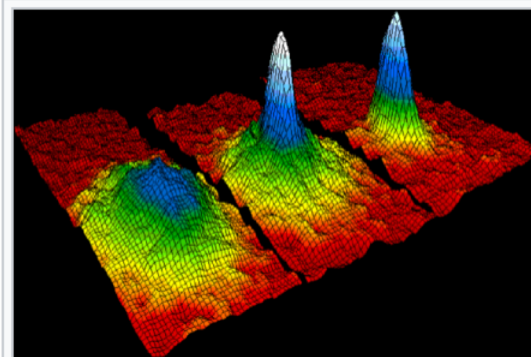


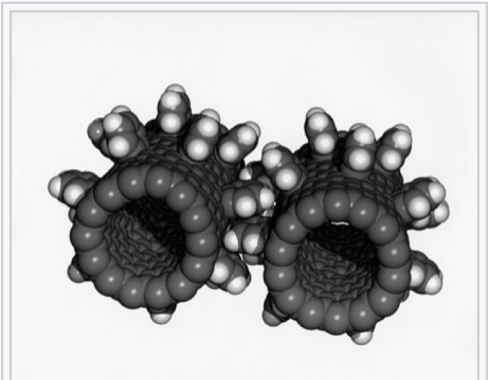
Image of X-ray diffraction pattern from a protein crystal.



The quantum Hall effect:

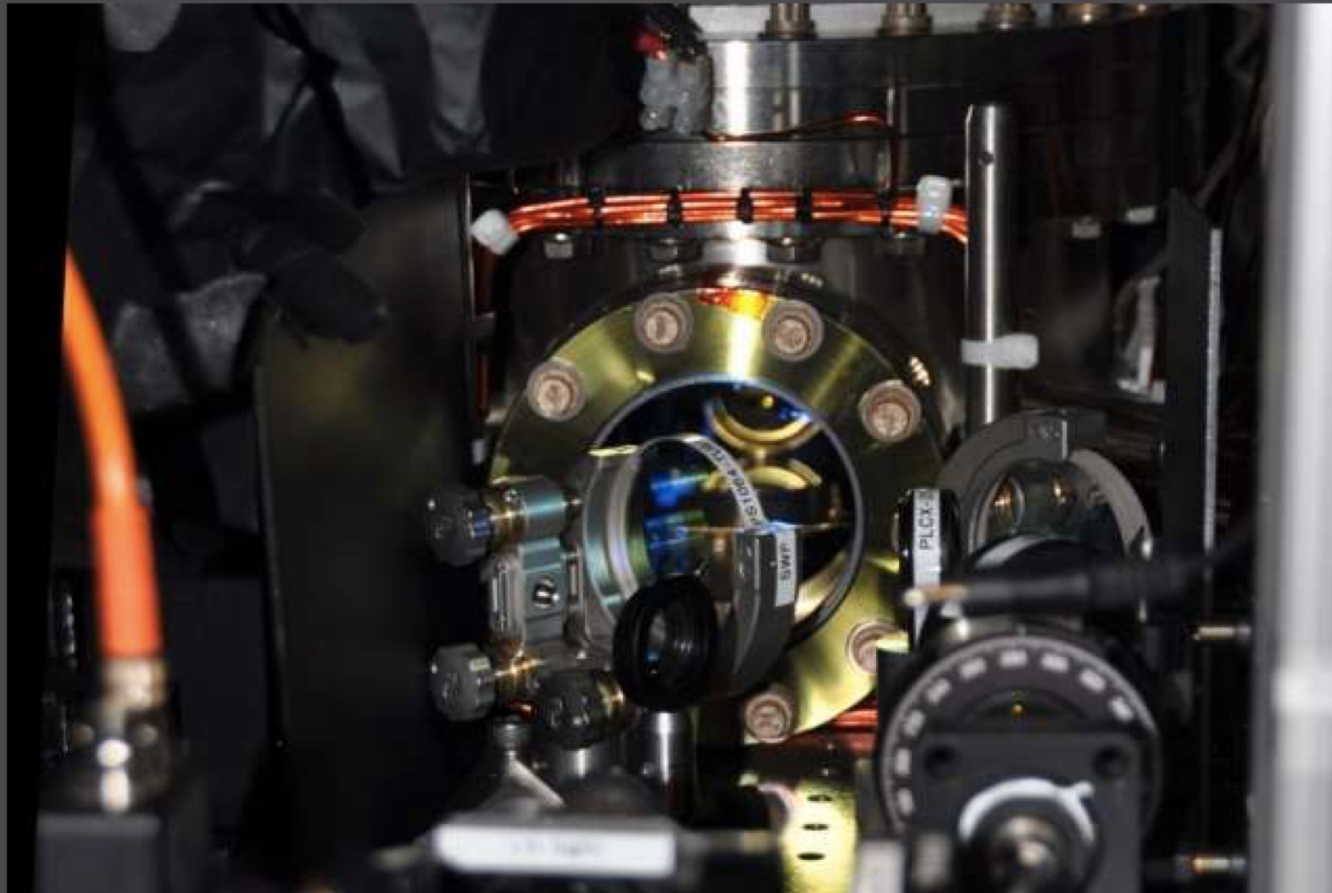


The first Bose-Einstein condensate



Computer simulation of nanogears

# Researchers create new form of matter —supersolid is crystalline and superfluid at the same time

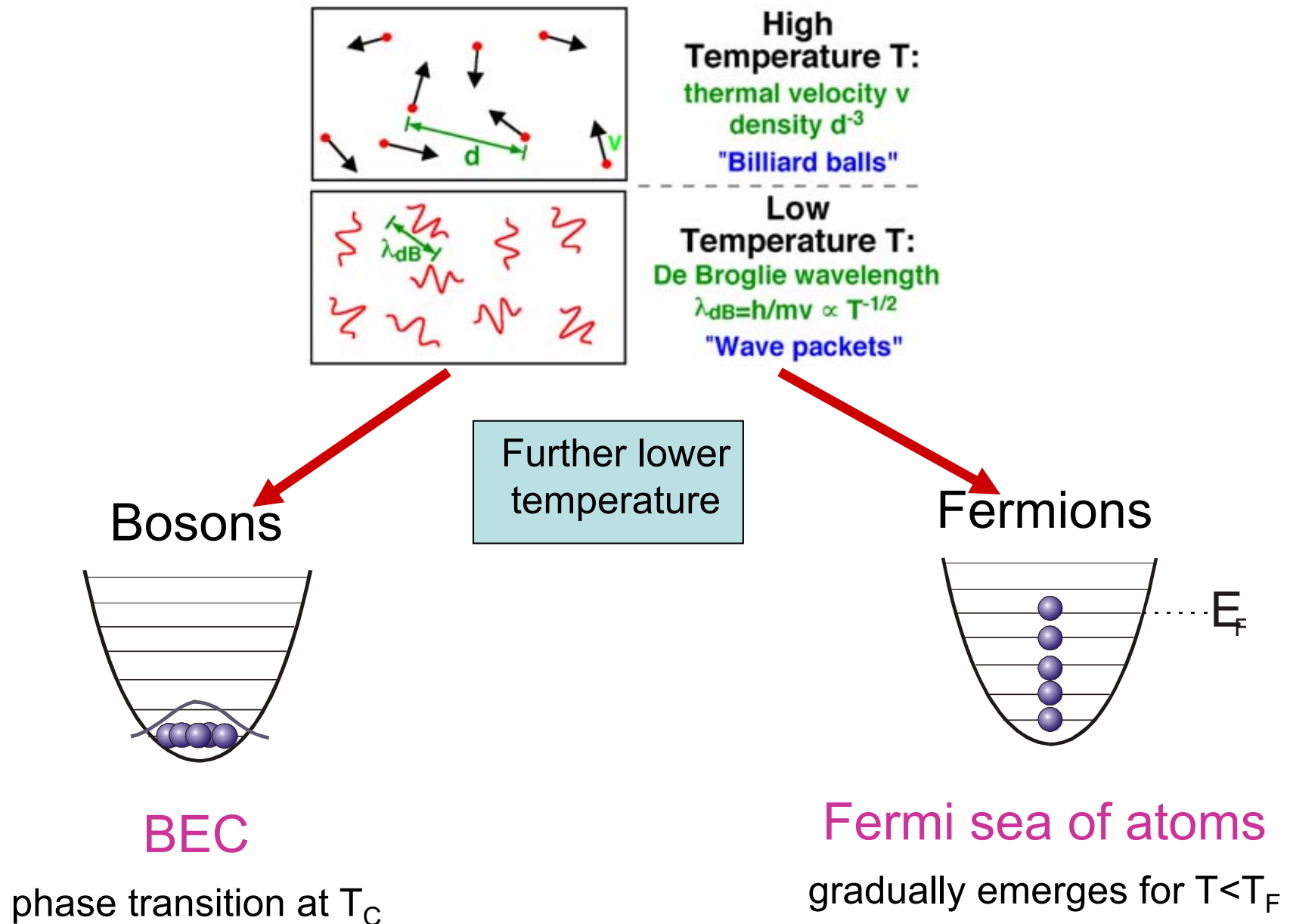


This image shows the equipment used by the Ketterle group to create a supersolid. Credit: Massachusetts Institute of Technology

MIT physicists have created a new form of matter, a supersolid, which combines the properties of solids with those of superfluids.

phys.org  
March 3,  
2017

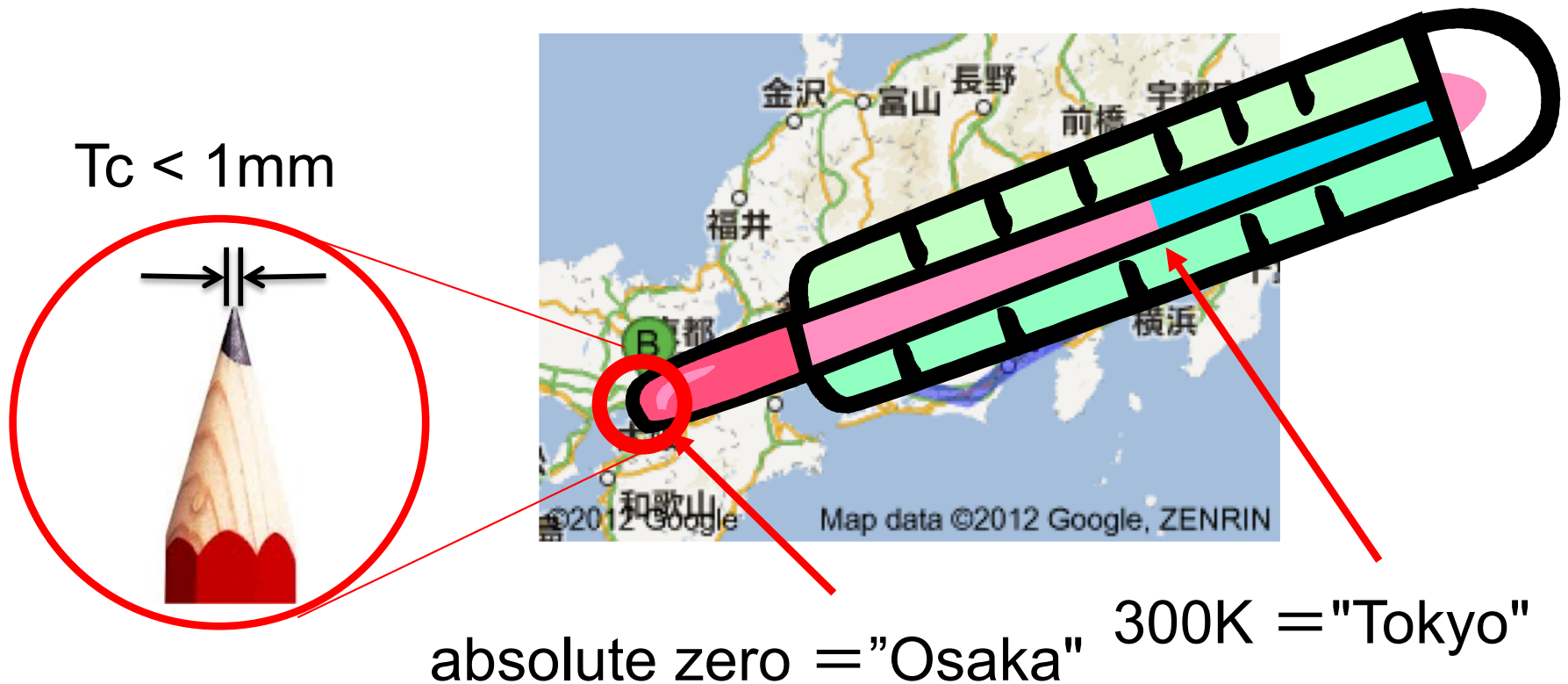
# What is ultracold quantum gas?



Problem with gases: Typical  $T_c$  is quite low

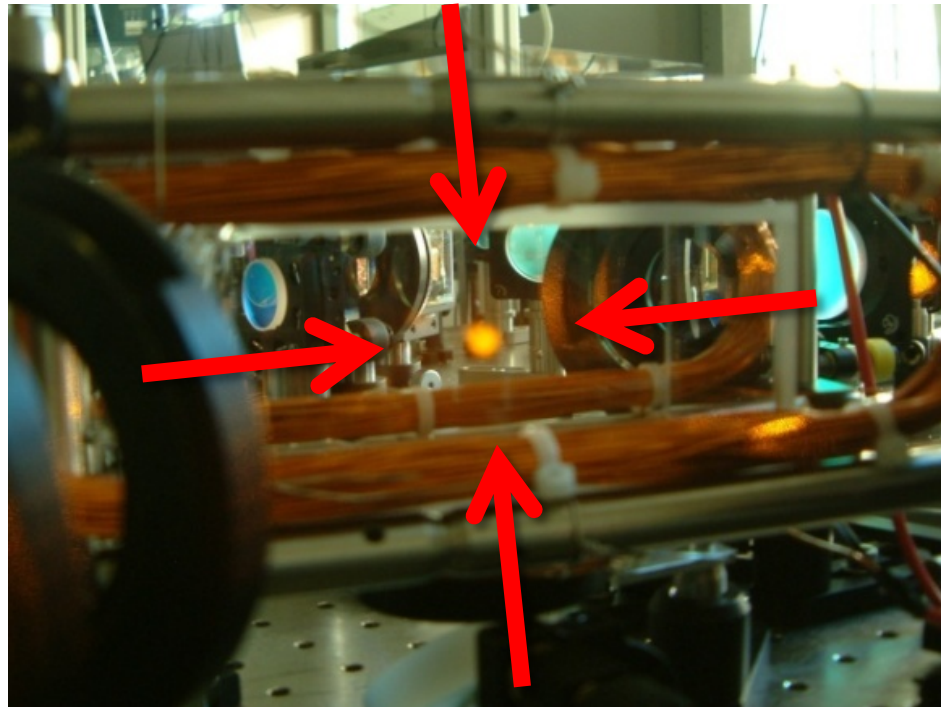
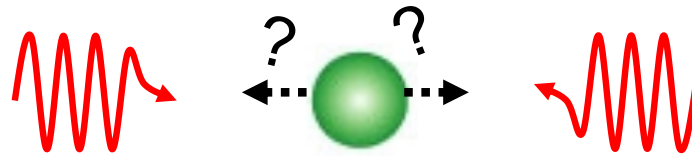
$$T_c = \frac{h^2}{2\pi m k_B} \left( \frac{n}{2.612} \right)^{2/3}$$

0.000 000 1K = 100nK





# Laser cooling !





# Technological breakthroughs

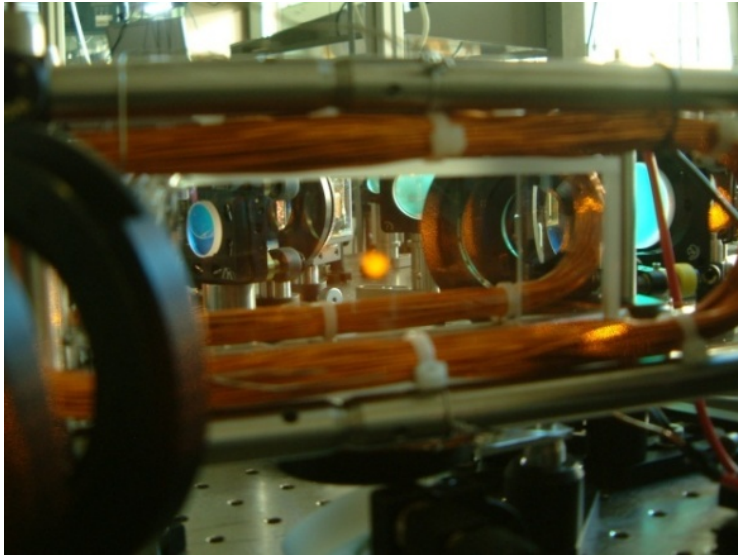
laser cooling + evaporative cooling



300 K to 1 mK



1 mK to 100 nK



(MOT)

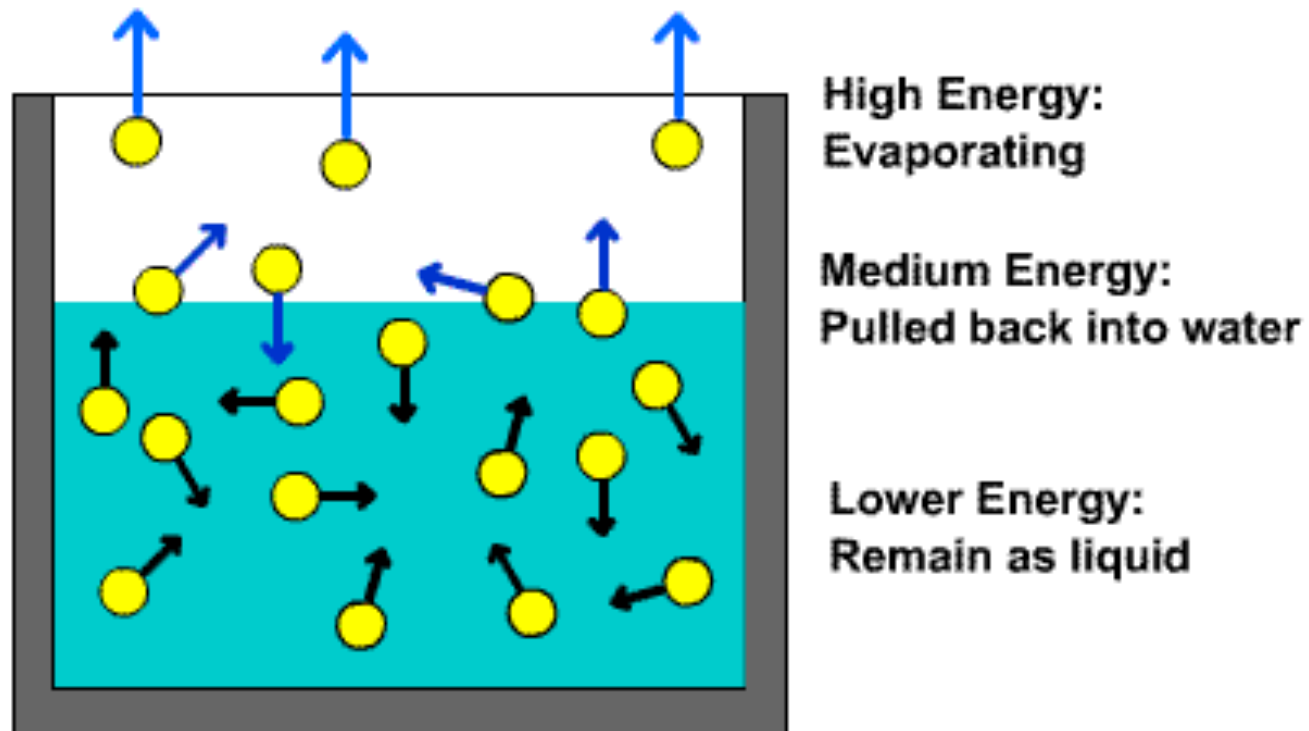


(Magnetic trap)

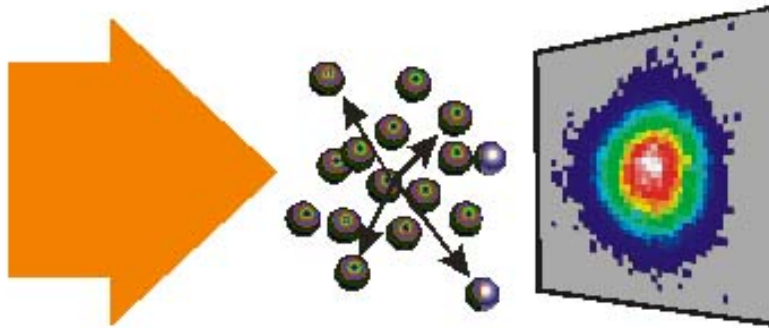
-> lowest man-made temperature !

A. E. Leanhardt, T. A. Pasquini, M. Saba, A. Schirotzek, Y. Shin, D. Kielpinski, D. E. Pritchard, and W. Ketterle:  
*Adiabatic and Evaporative Cooling of Bose-Einstein condensates below 500 Picokelvin.*  
Science 301, 1513-1515 (2003).

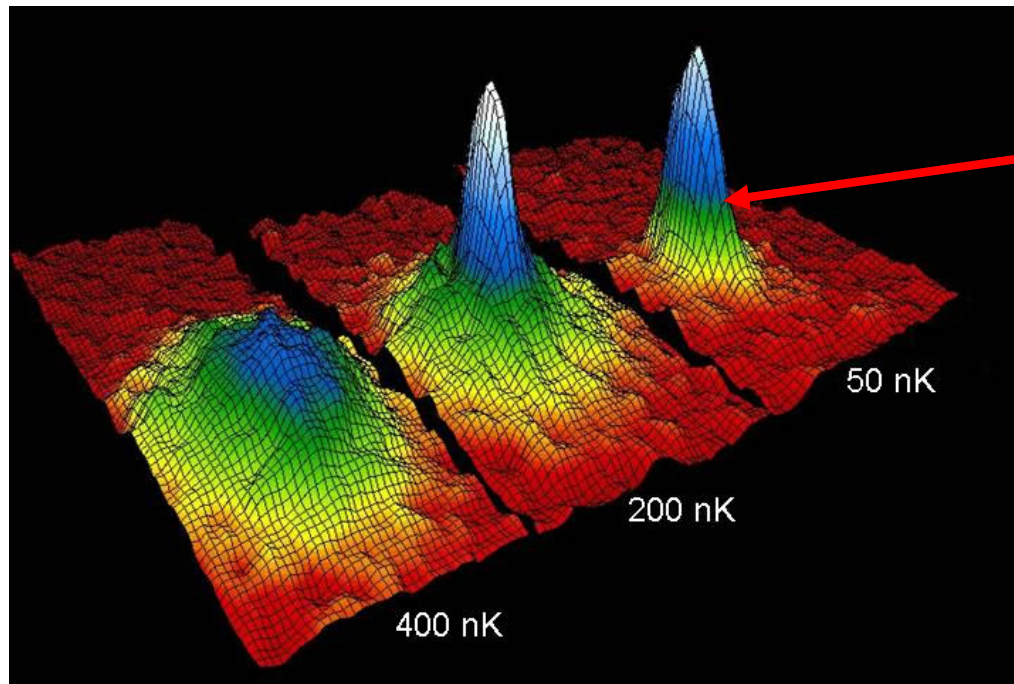
# Evaporative cooling



# Bose-Einstein condensation



Time-of-flight:  
Release atoms from the trap,  
wait for tens of milli-seconds,  
and take shadow picture.



Suddenly momentum  
distribution becomes  
narrower.

↓  
Bose-Einstein  
Condensation!

Anderson et al., Science, 269 198 (1995)

# *Outline*

*How to cool atoms*

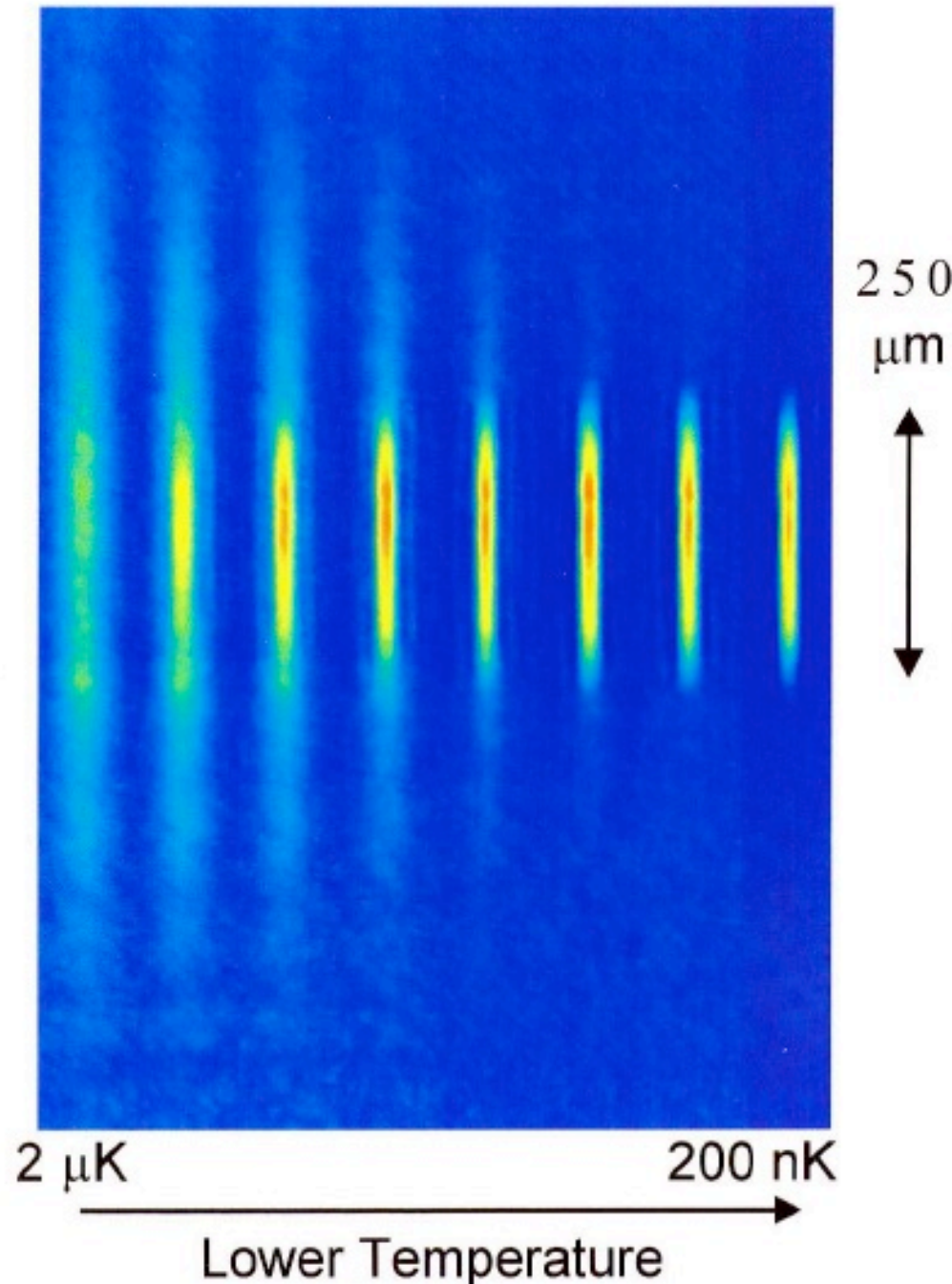
*Properties of BEC*

*Tuning interactions (Feshbach resonance)*

*Cold molecules*

*Conclusion and Outlook*





## Typical parameters

- Density:  $\sim 10^{14} \text{ cm}^{-3}$
- Temperature:  $< 100 \text{ nK}$
- Number of atoms:  $< 10^7$
- Size:  $20 \times 20 \times 200 \text{ } \mu\text{m}$
- Life time:  $> 10 \text{ s}$
- Atomic species: Rb, Na, Li, ...

## Properties of a BEC

- gaseous superfluid
- macroscopic wavefunction  
(Quantum depletion:  
alkali BEC  $< 1\%$ , liq. He  $> 90\%$ )



## What we are looking at?

$$\rho(\vec{r}) = \langle \hat{\psi}^\dagger(\vec{r}) \hat{\psi}(\vec{r}) \rangle$$

$$H = \int d\mathbf{r} \left[ \underbrace{-\hat{\psi}^\dagger(\mathbf{r}) \frac{\hbar^2}{2m} \nabla^2 \hat{\psi}(\mathbf{r})}_{\text{Kinetic energy}} + \underbrace{V(\mathbf{r}) \hat{\psi}^\dagger(\mathbf{r}) \hat{\psi}(\mathbf{r})}_{\text{Confining potential}} + \underbrace{\frac{U_0}{2} \hat{\psi}^\dagger(\mathbf{r}) \hat{\psi}^\dagger(\mathbf{r}) \hat{\psi}(\mathbf{r}) \hat{\psi}(\mathbf{r})}_{\text{Interaction between atoms}} \right]$$

Kinetic  
energy

Confining  
potential

Interaction  
between atoms

$$U_0 = 4\pi\hbar^2 a/m.$$

It is useful to introduce  $\psi(\mathbf{r})$

$$\hat{\psi}(\mathbf{r}) = \psi(\mathbf{r}) + \delta\hat{\psi}(\mathbf{r}).$$

  
c-number

  
quantum fluctuation

# Order parameter and Spontaneous Symmetry Breaking

$\psi(\mathbf{r})$  satisfies Penrose-Onsager relation:

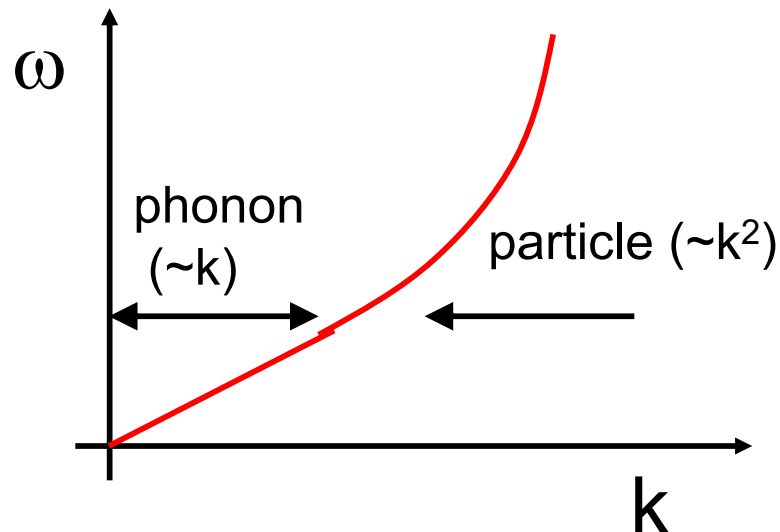
$$\langle \hat{\psi}^+(\vec{r}) \hat{\psi}(\vec{r}') \rangle = \psi^*(\vec{r}) \psi(\vec{r}') + \underbrace{\langle \delta \hat{\psi}^+(\vec{r}) \delta \hat{\psi}(\vec{r}') \rangle}$$

vanishes as  $|\mathbf{r}-\mathbf{r}'| \rightarrow \infty$

Hamiltonian is unchanged under global gauge transformation:

$$\psi(\vec{r}) \rightarrow e^{i\alpha} \psi(\vec{r})$$

Nambu-Goldstone mode: phonon



## Propagation of Sound in a Bose-Einstein Condensate

M. R. Andrews, D. M. Kurn, H.-J. Miesner, D. S. Durfee, C. G. Townsend, S. Inouye, and W. Ketterle

*Department of Physics and Research Laboratory of Electronics, Massachusetts Institute of Technology,  
Cambridge, Massachusetts 02139*

(Received 20 March 1997; revised manuscript received 27 May 1997)

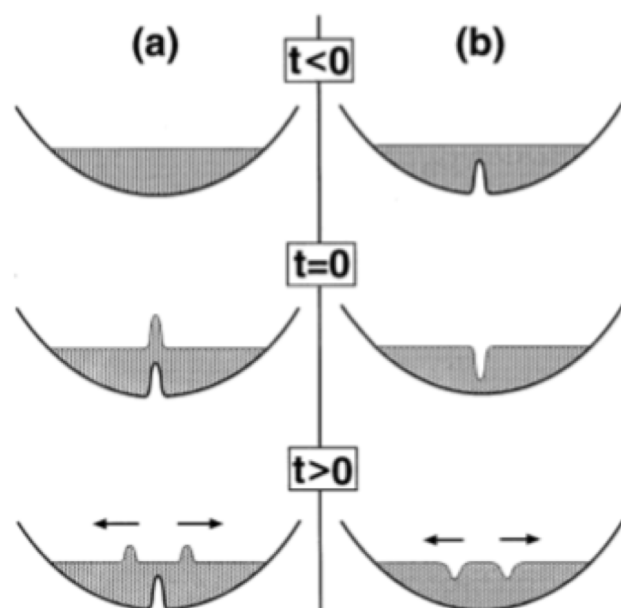
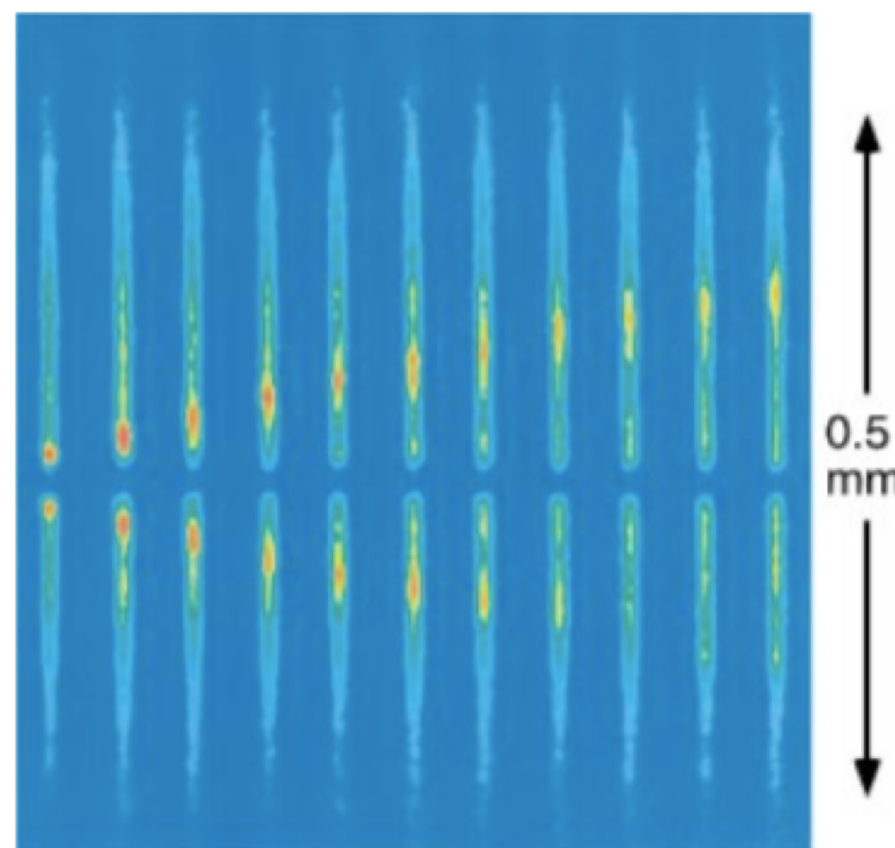


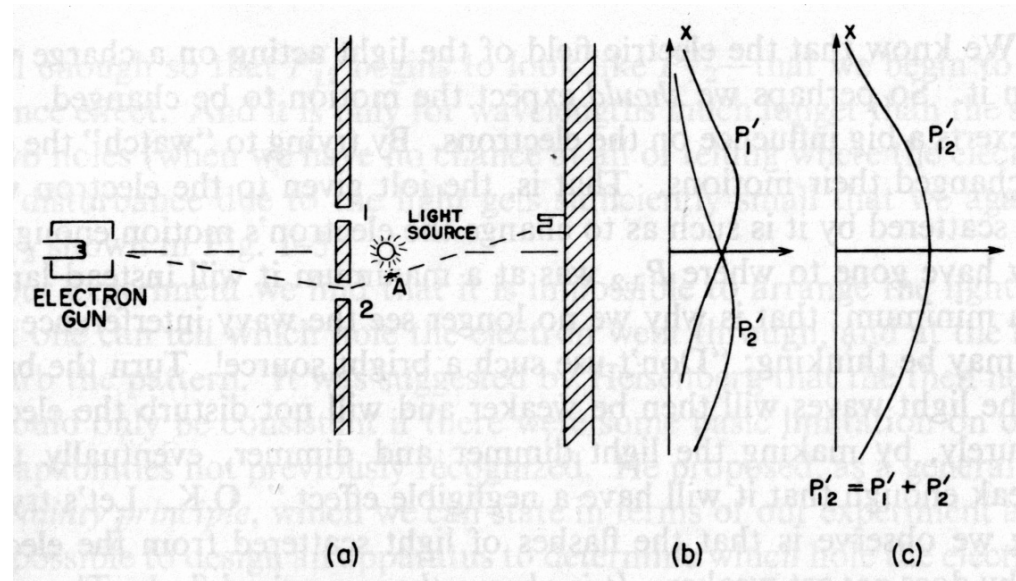
FIG. 1. Excitations of wave packets in a Bose-Einstein condensate. A condensate is confined in the potential of a magnetic trap. At time  $t = 0$ , a focused, blue-detuned laser beam is suddenly switched on (a) or off (b) and, by the optical dipole force, creates, respectively, two positive or negative perturbations in density which propagate at the speed of sound.



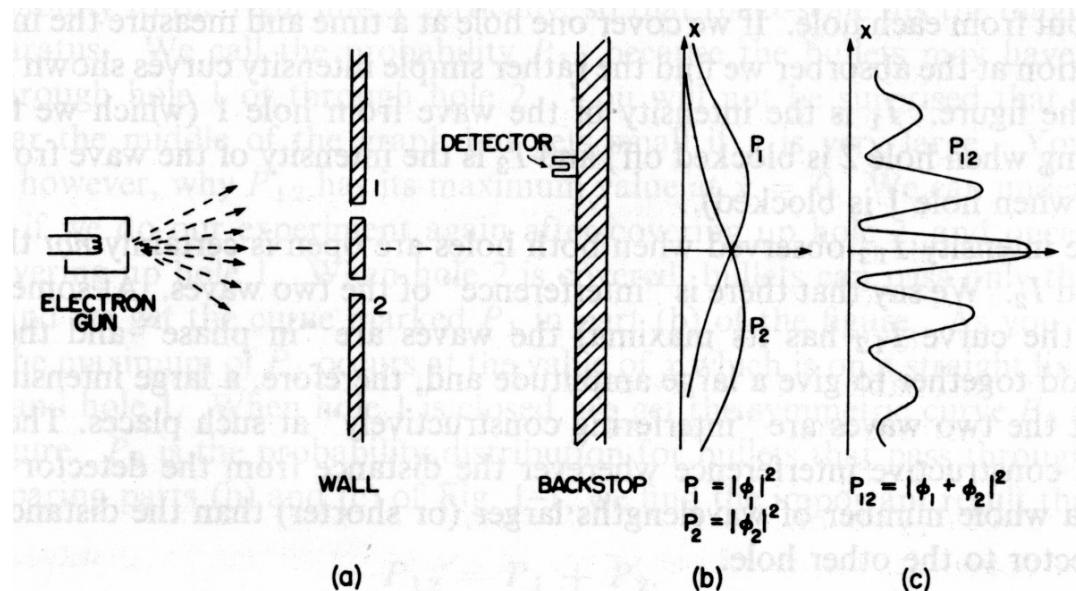
# Direct confirmation of macroscopic wavefunction?

## Interference!

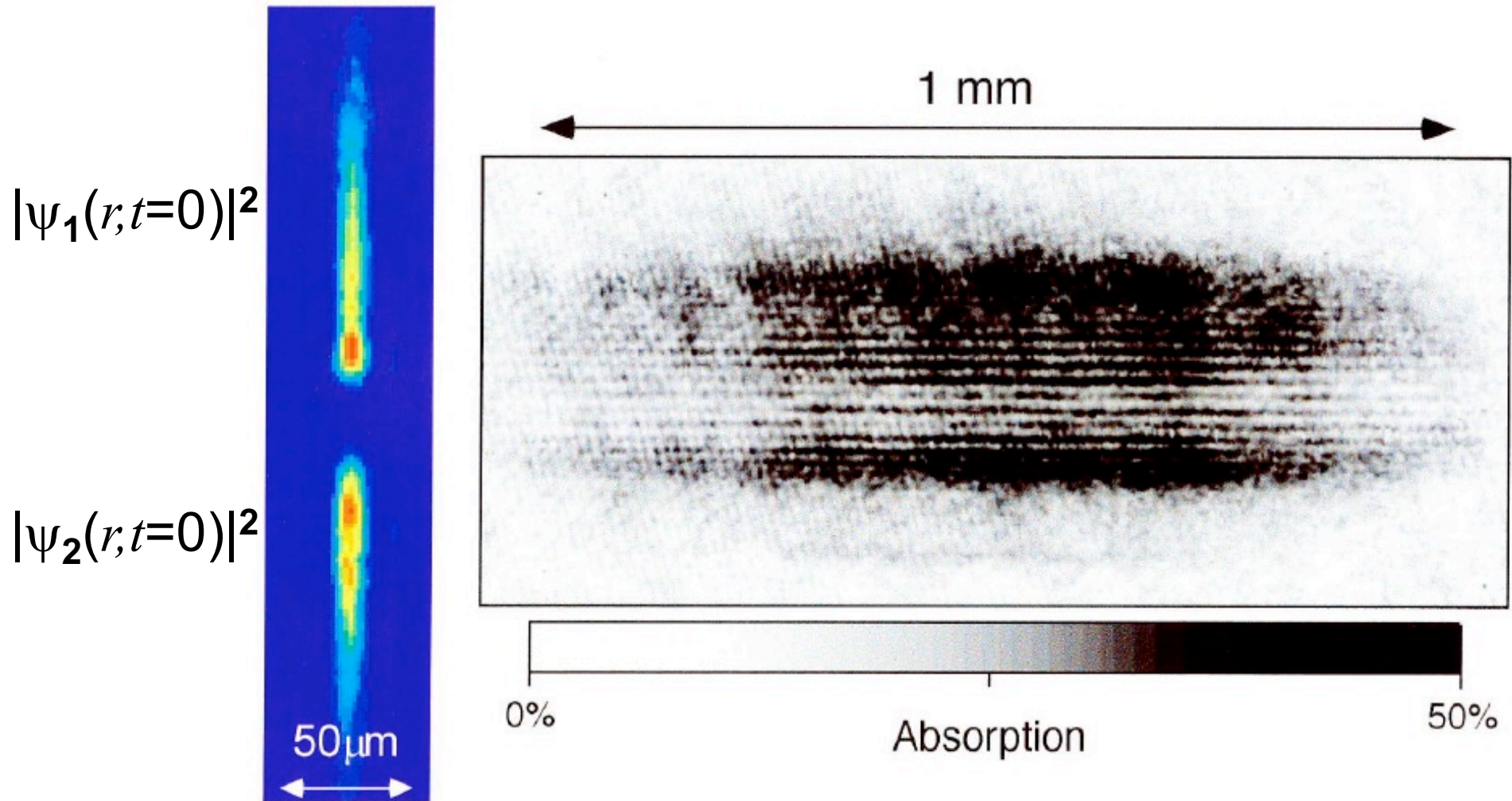
Classical  
mechanics



Quantum  
mechanics



# Two condensates ... interfere!



$$|\psi_1(r, t = T) + \psi_2(r, t = T)|^2$$

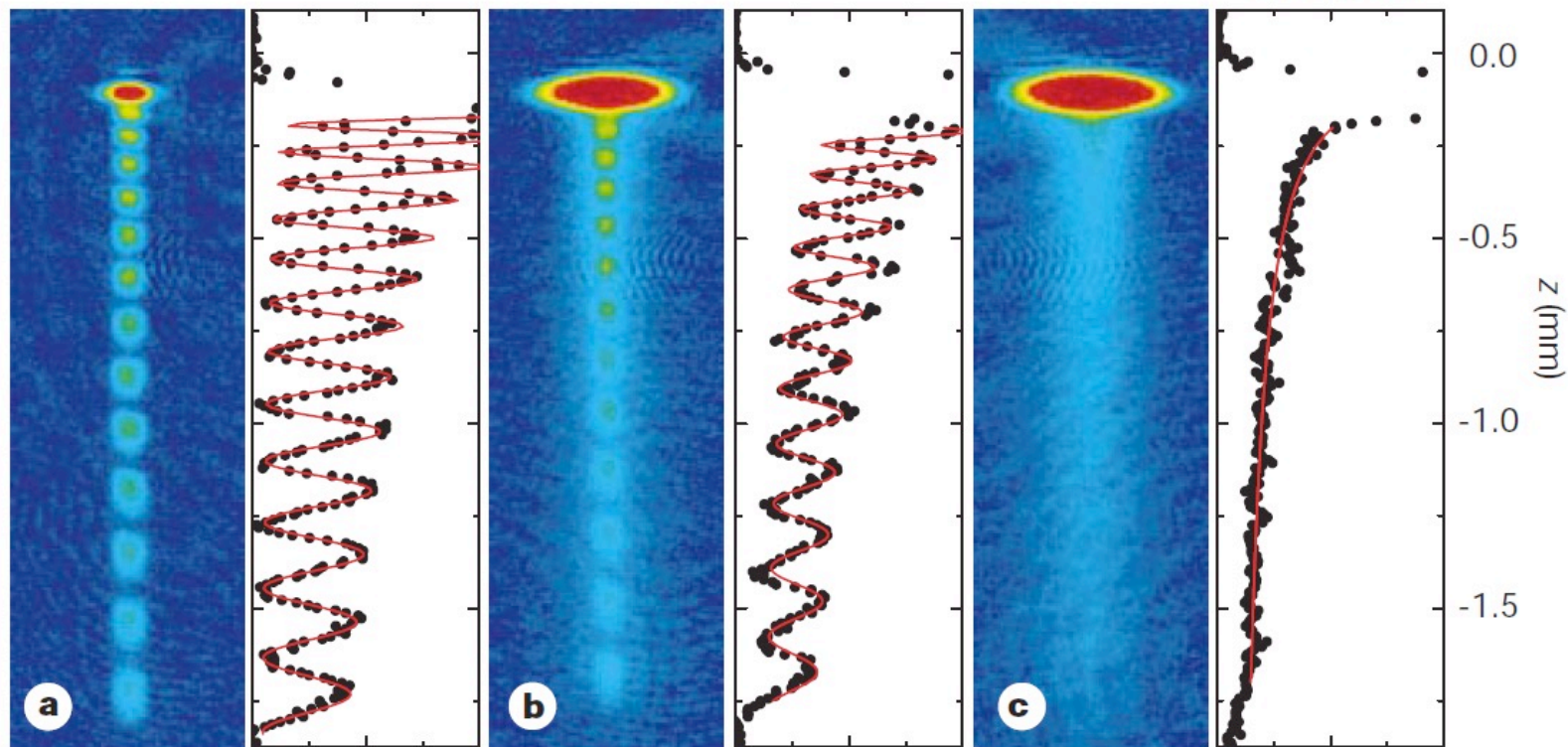
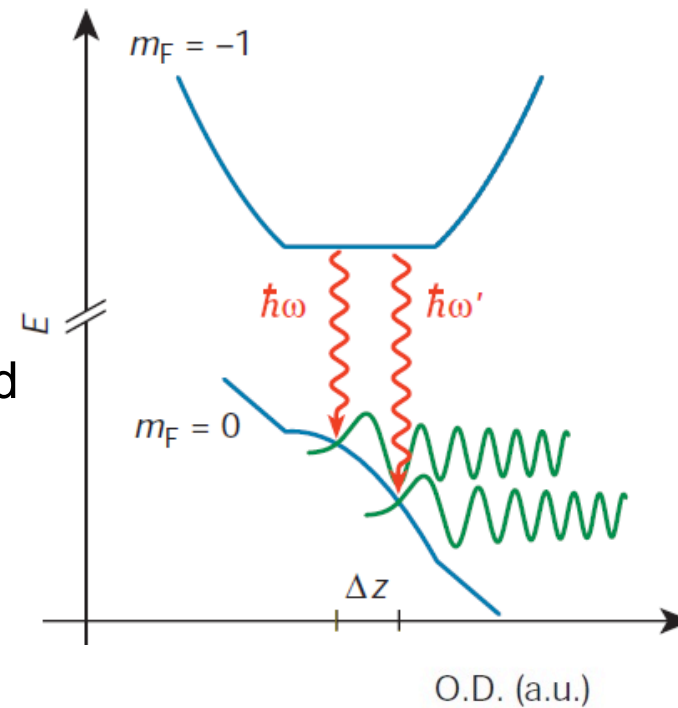
M. R. Andrews *et al.*, Science **275**, 637 (1997)



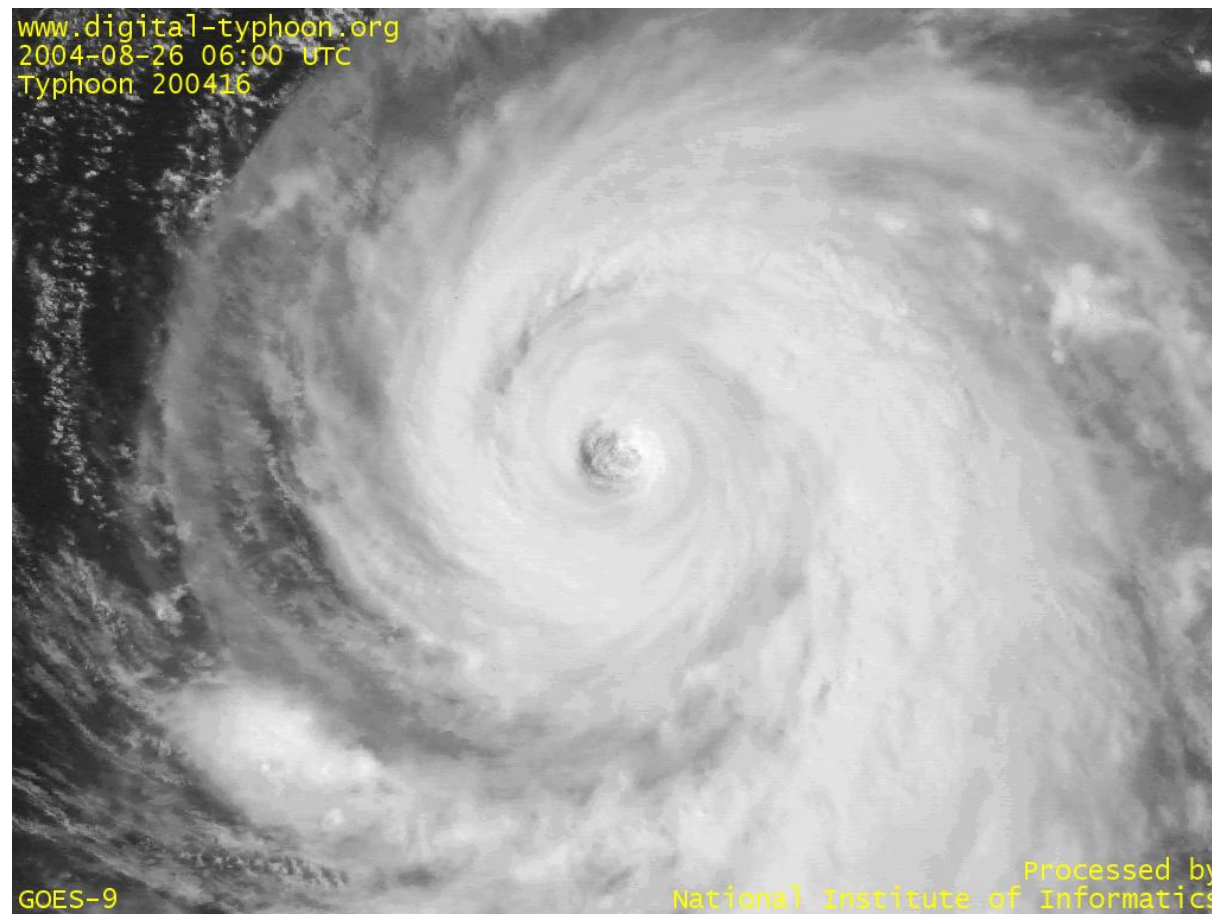
# Measurement of 1st-order **spatial** coherence

Extract matterwave from two separated points and make them interfere.

I. Bloch, T. W. Hänsch & T. Esslinger  
Nature 403, 166–170 (2000)



# Vortex !



# Rotate a BEC with a laser beam

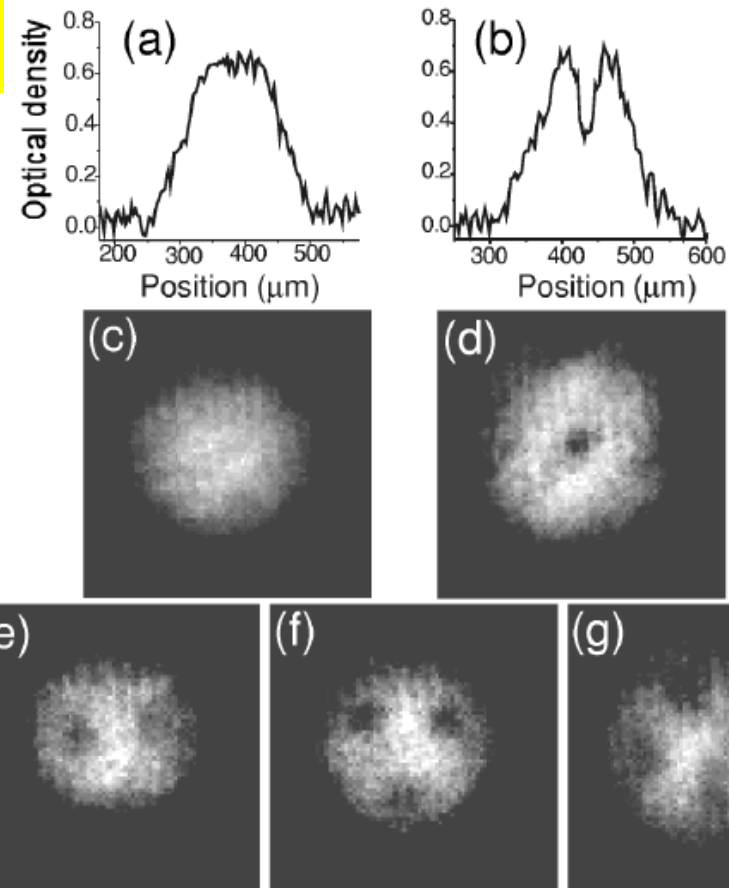
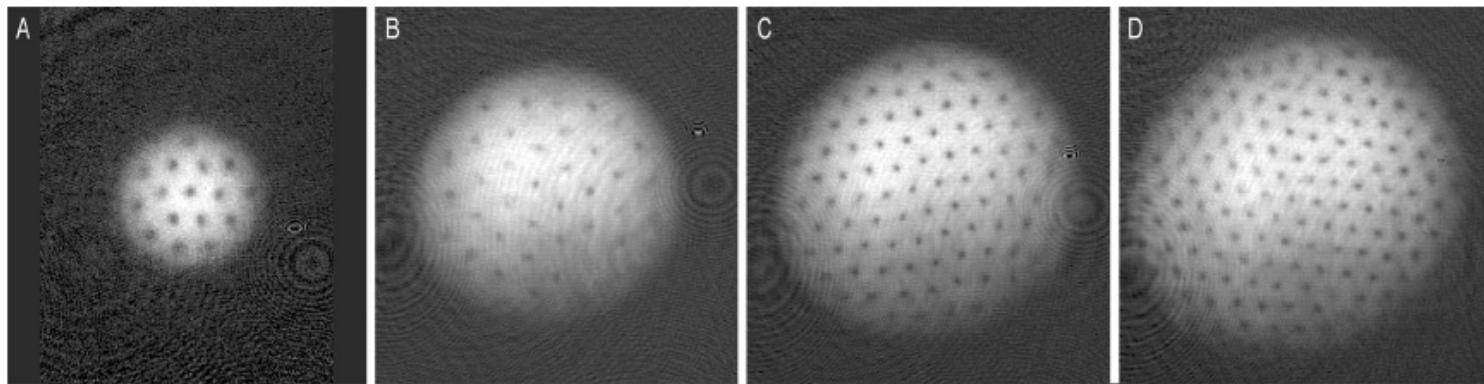


FIG. 1. Transverse absorption images of a Bose-Einstein condensate stirred with a laser beam (after a 27 ms time of flight). For all five images, the condensate number is  $N_0 = (1.4 \pm 0.5) 10^5$  and the temperature is below 80 nK. The rotation frequency  $\Omega/(2\pi)$  is, respectively, (c) 145 Hz, (d) 152 Hz, (e) 169 Hz, (f) 163 Hz, (g) 168 Hz. In (a) and (b) we plot the variation of the optical thickness of the cloud along the horizontal transverse axis for the images (c) (0 vortex) and (d) (1 vortex).

K. W. Madison, F. Chevy, W. Wohlleben\*, and J. Dalibard  
Phys. Rev. Lett. 84, 806–809 (2000)  
Vortex Formation in a Stirred Bose-Einstein Condensate

# Vortex lattice !

Fig. 1. Observation of vortex lattices. The examples shown contain approximately (A) 16, (B) 32, (C) 80, and (D) 130 vortices. The vortices have "crystallized" in a triangular pattern. The diameter of the cloud in (D) was 1 mm after ballistic expansion, which represents a magnification of 20.

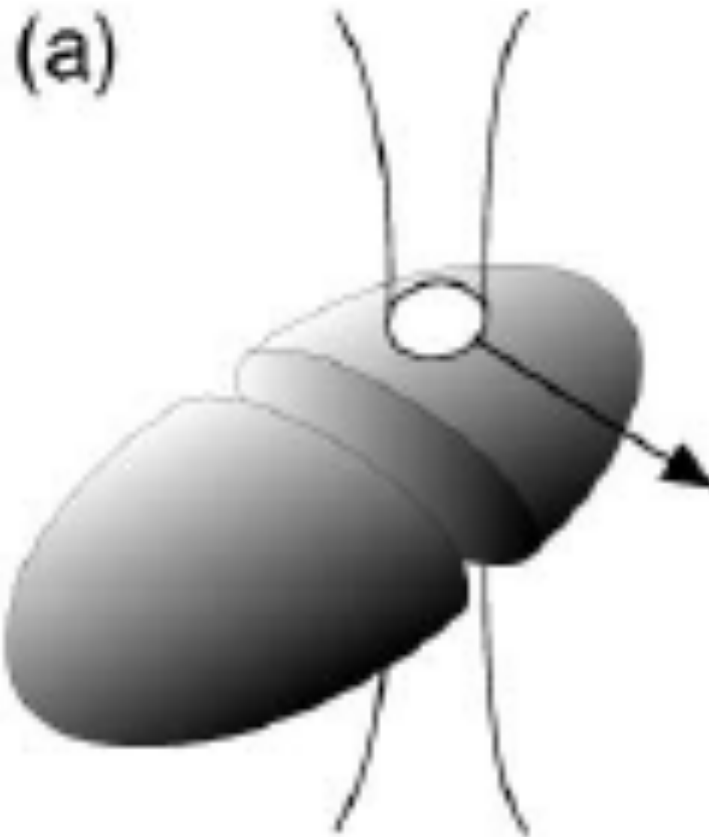


Slight asymmetries in the density distribution were due to absorption of the optical pumping light.

## Abrikosov lattice

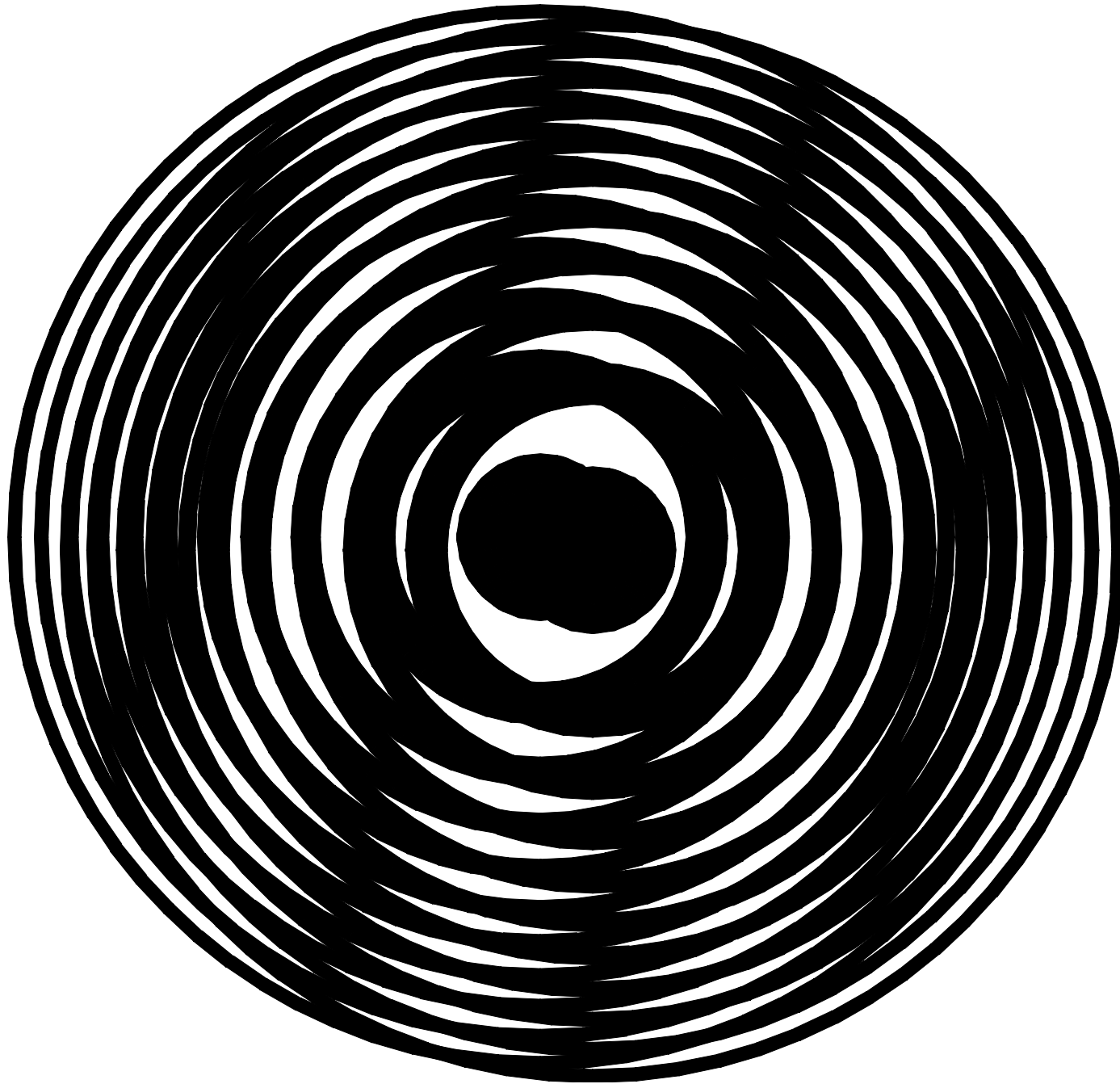
J.R. Abo-Shaeer, C. Raman, J.M. Vogels, and W. Ketterle:  
*Observation of Vortex Lattices in Bose-Einstein Condensates.*  
Science 292, 476-479 (2001).

sweeping a laser beam to generate vortex!

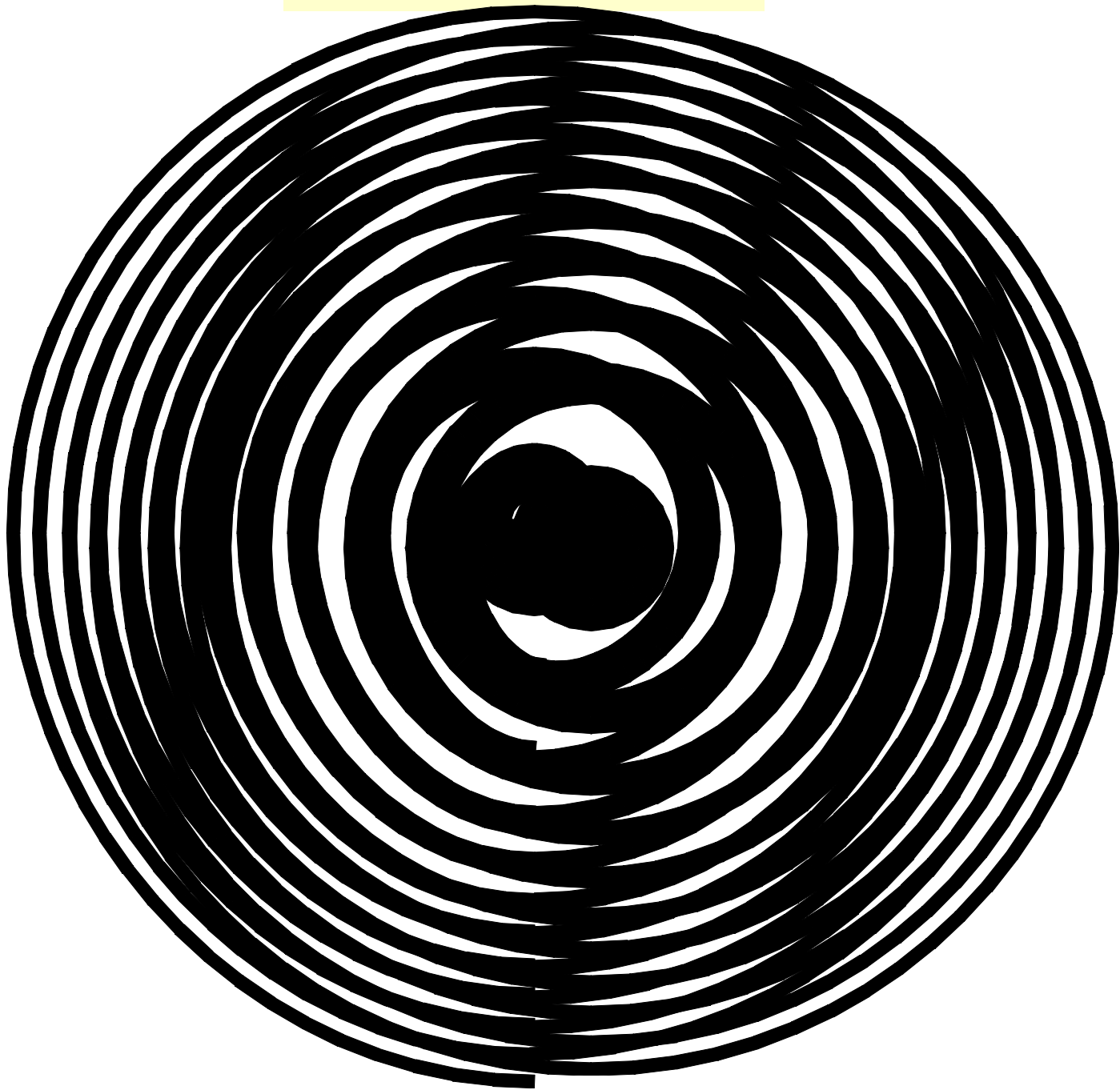




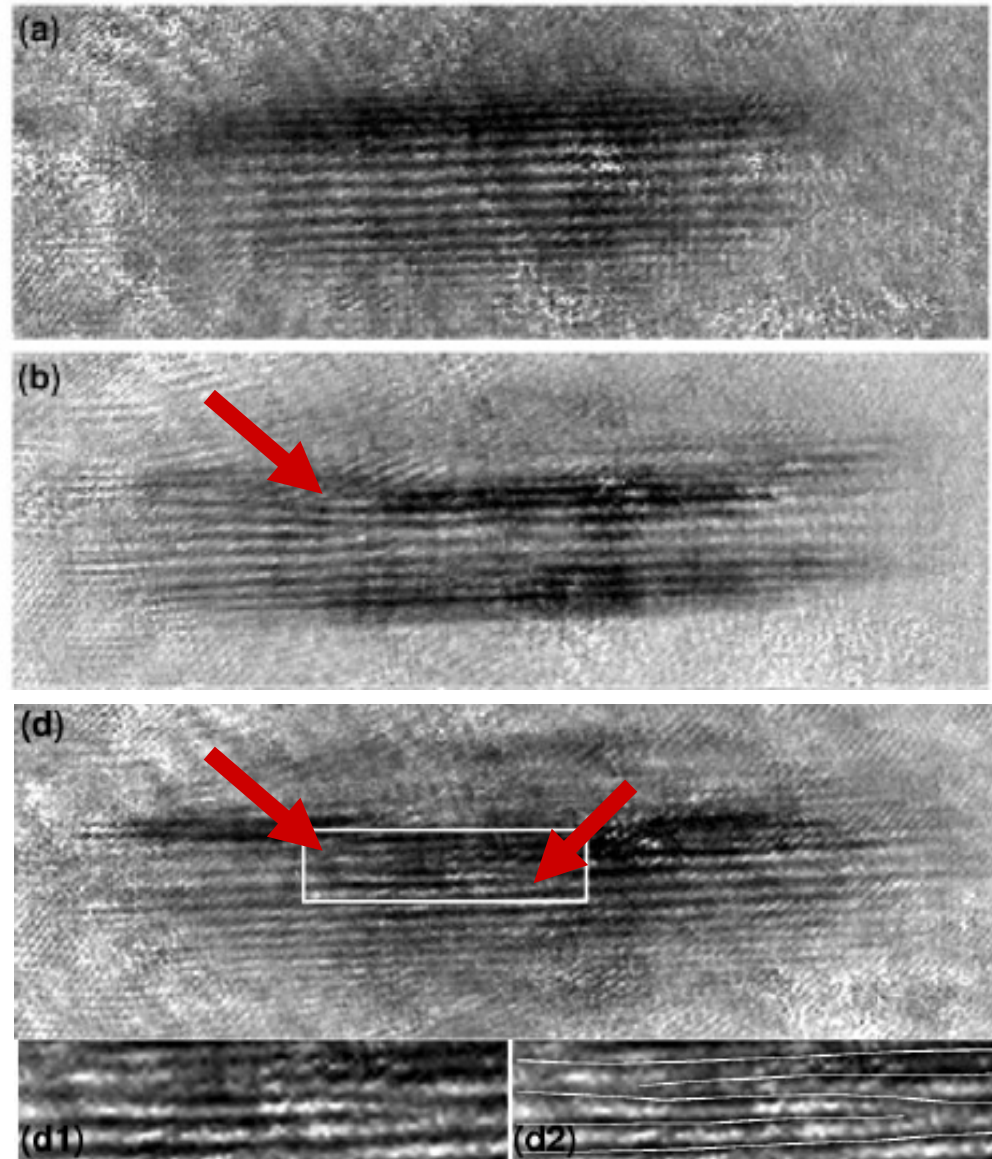
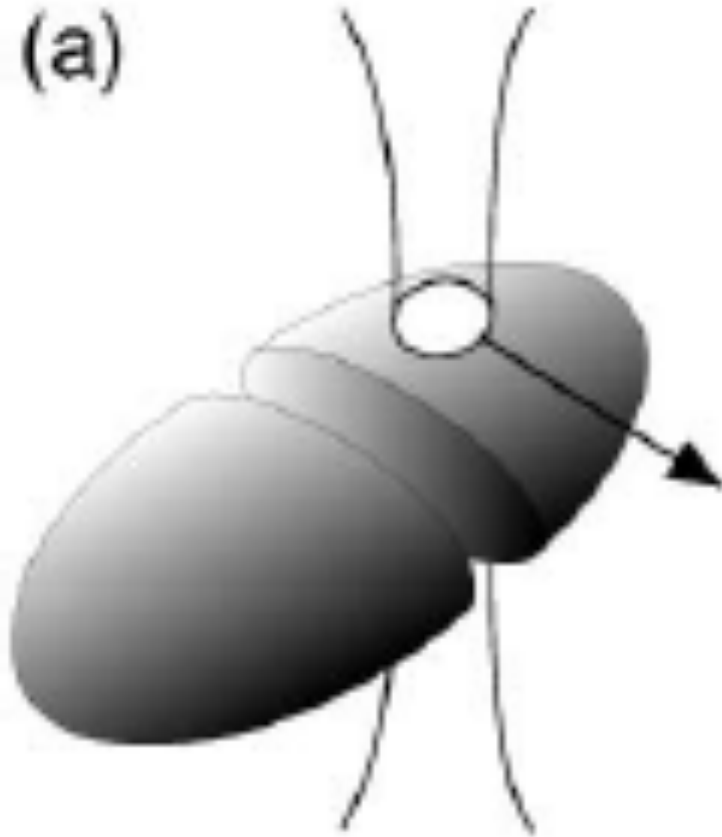
(wavefronts of matterwaves realeased from two BECs)



BEC with a vortex



# Interferometric detection of vortex pair



"Observation of vortex phase singularities in Bose-Einstein condensates."  
S. Inouye *et al.*, PRL, **87**, 080402 (2001).

# *Outline*

*How to cool atoms*

*Properties of BEC*

*Tuning interactions (Feshbach resonance)*

*Cold molecules*

*Conclusion and Outlook*



$$H = \int d\mathbf{r} \left[ \underbrace{-\hat{\psi}^\dagger(\mathbf{r}) \frac{\hbar^2}{2m} \nabla^2 \hat{\psi}(\mathbf{r})}_{\text{Kinetic energy}} + \underbrace{V(\mathbf{r}) \hat{\psi}^\dagger(\mathbf{r}) \hat{\psi}(\mathbf{r})}_{\text{Confining potential}} + \underbrace{\frac{U_0}{2} \hat{\psi}^\dagger(\mathbf{r}) \hat{\psi}^\dagger(\mathbf{r}) \hat{\psi}(\mathbf{r}) \hat{\psi}(\mathbf{r})}_{\text{Interaction between atoms}} \right]$$

Kinetic  
energy

Confining  
potential

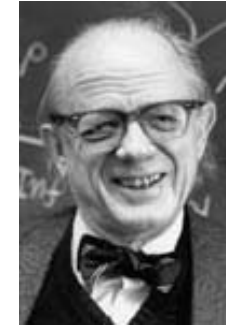
Interaction  
between atoms

$$U_0 = 4\pi\hbar^2 a/m.$$

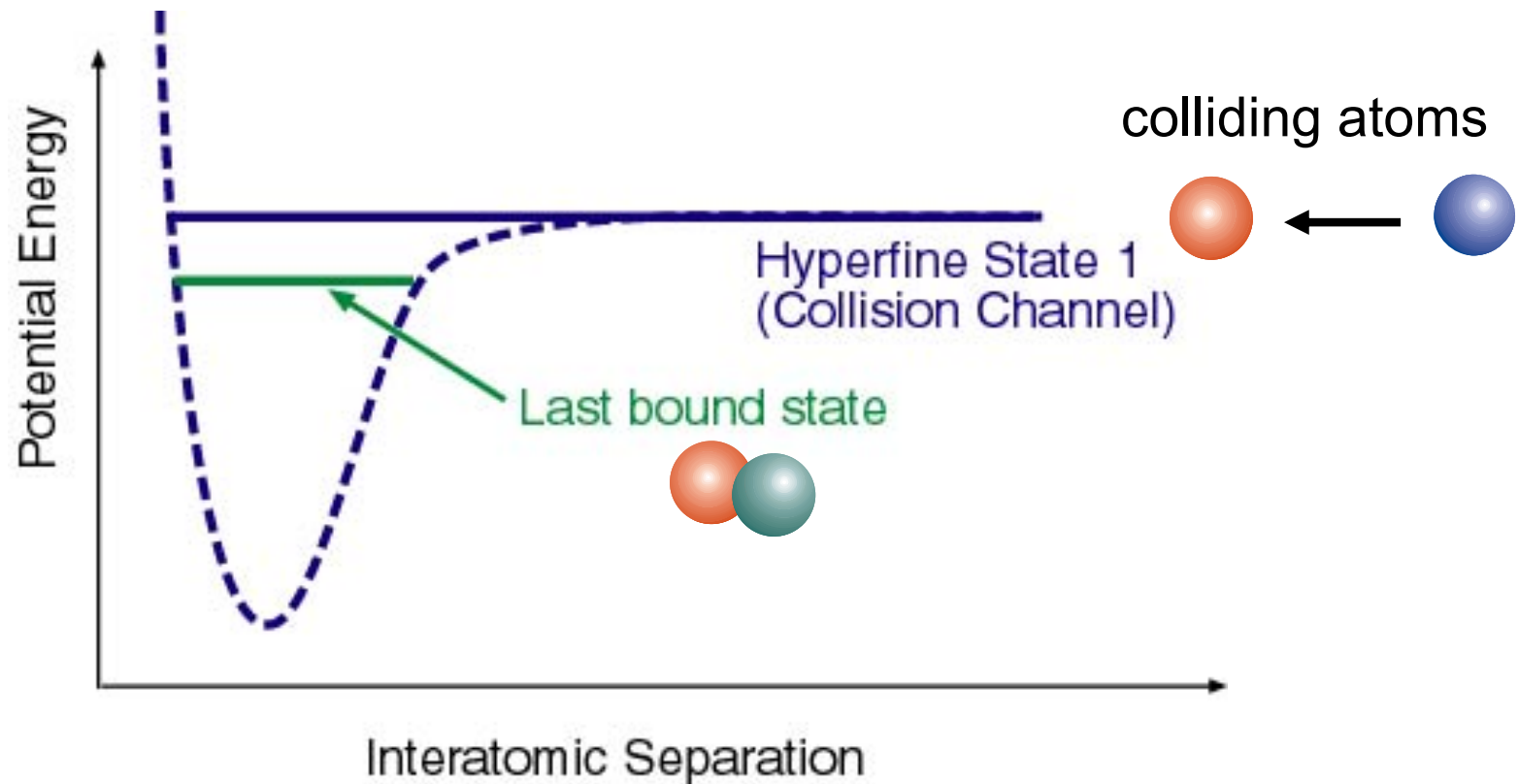
Can we tune the scattering length?



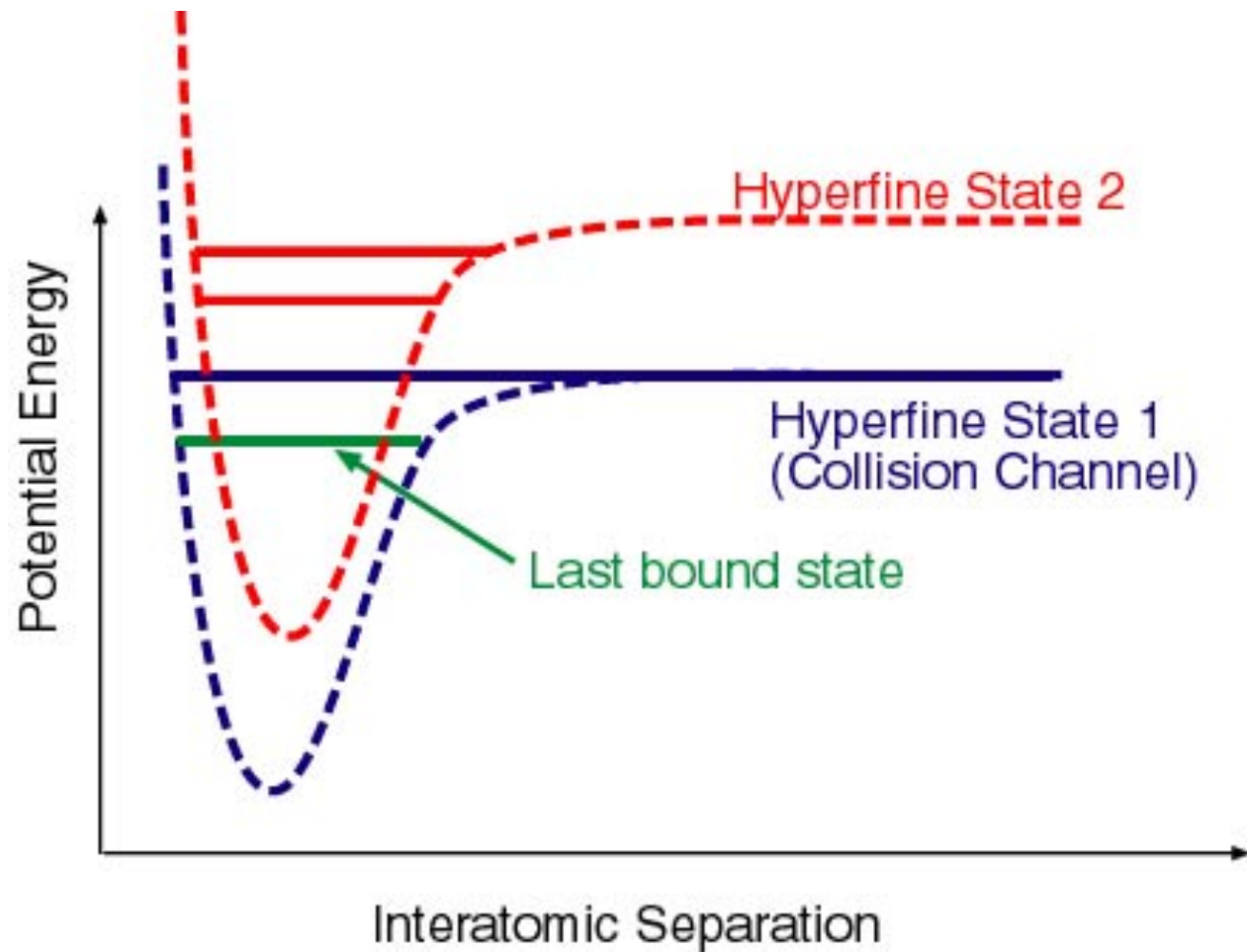
## Tuning the interaction (Feshbach resonance)



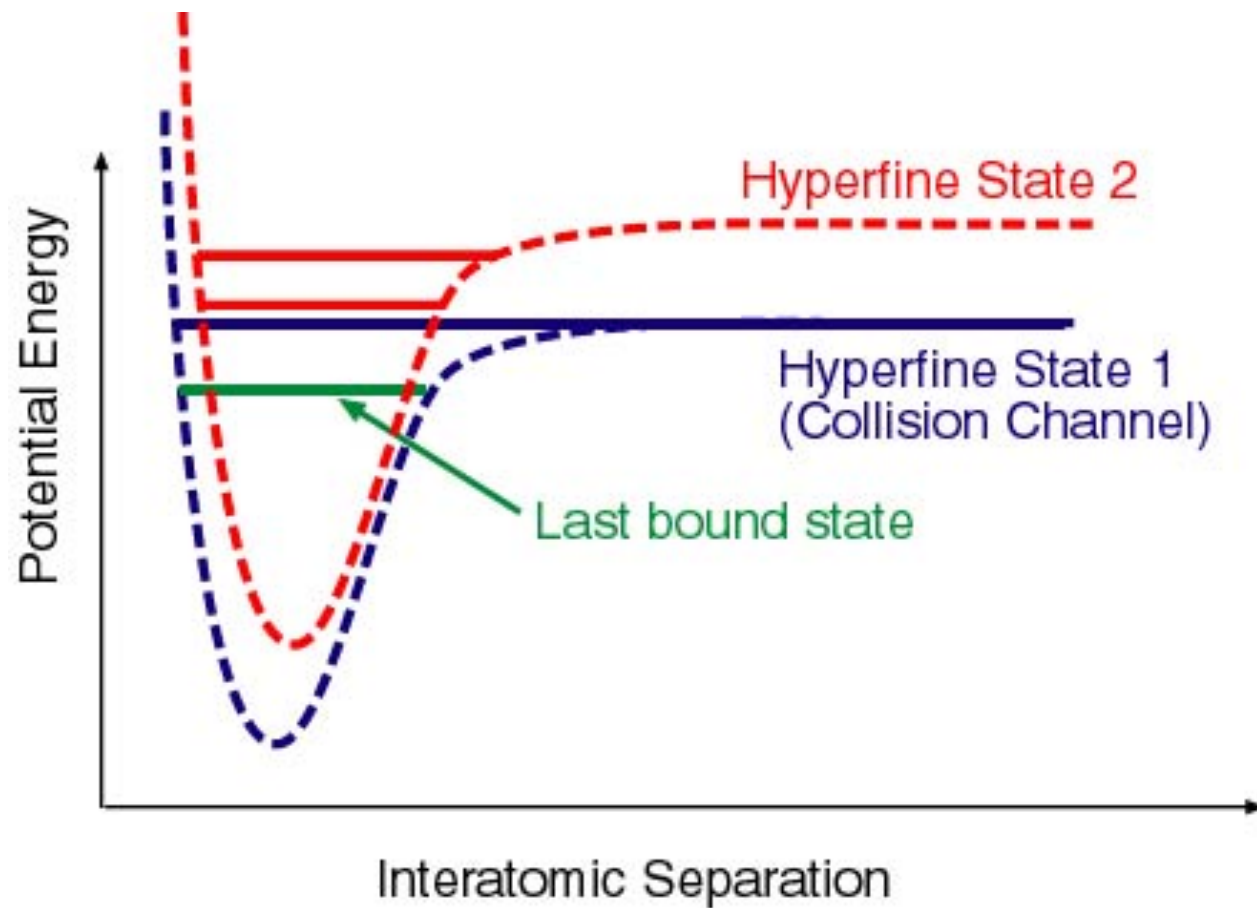
Herman Feshbach



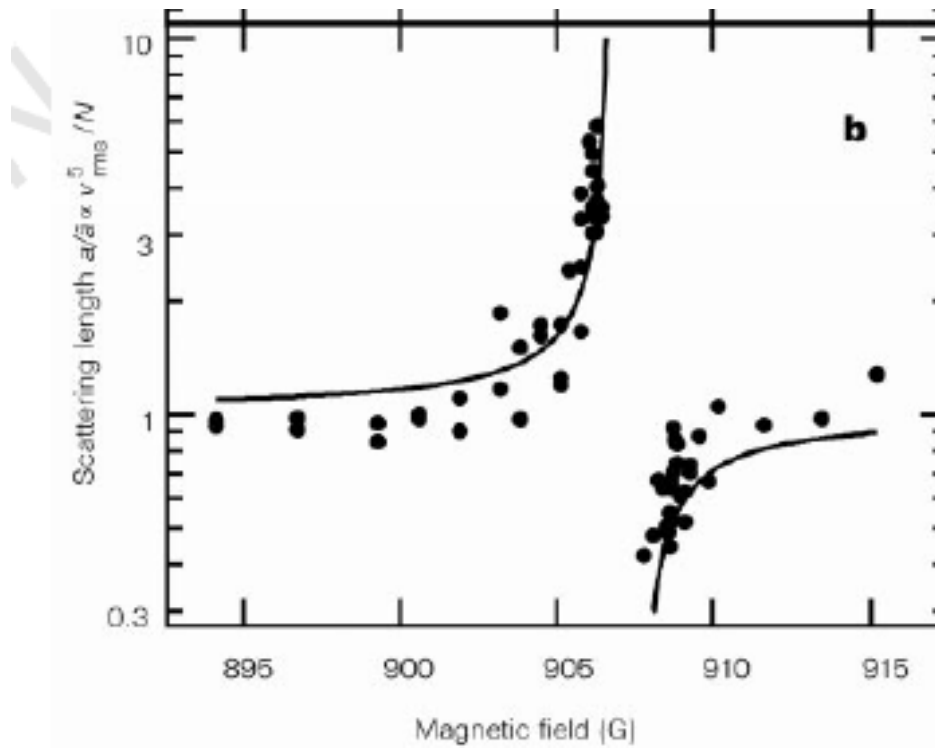
## Use nuclear spin



# Interference!

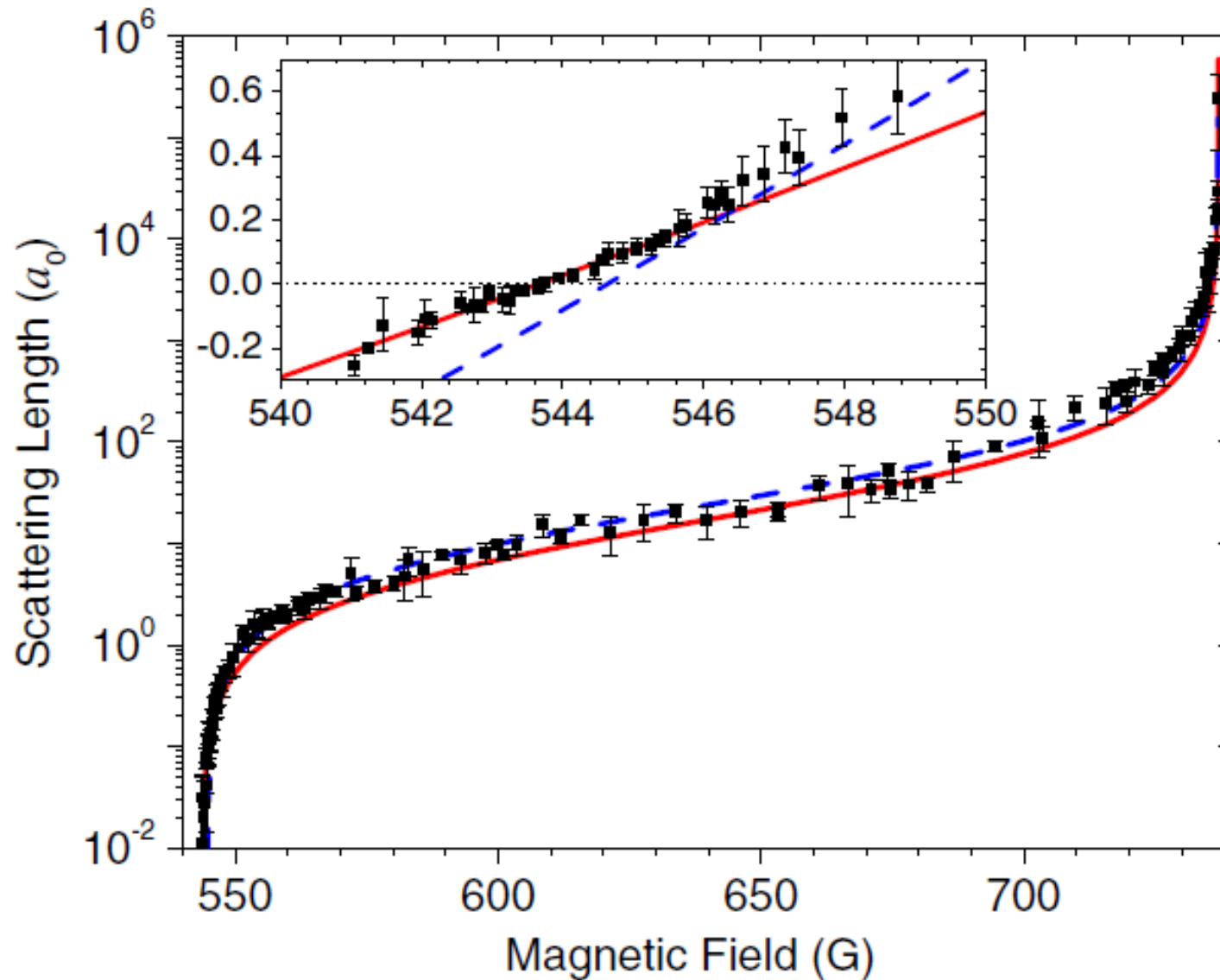


“U” is modified by factor of 20



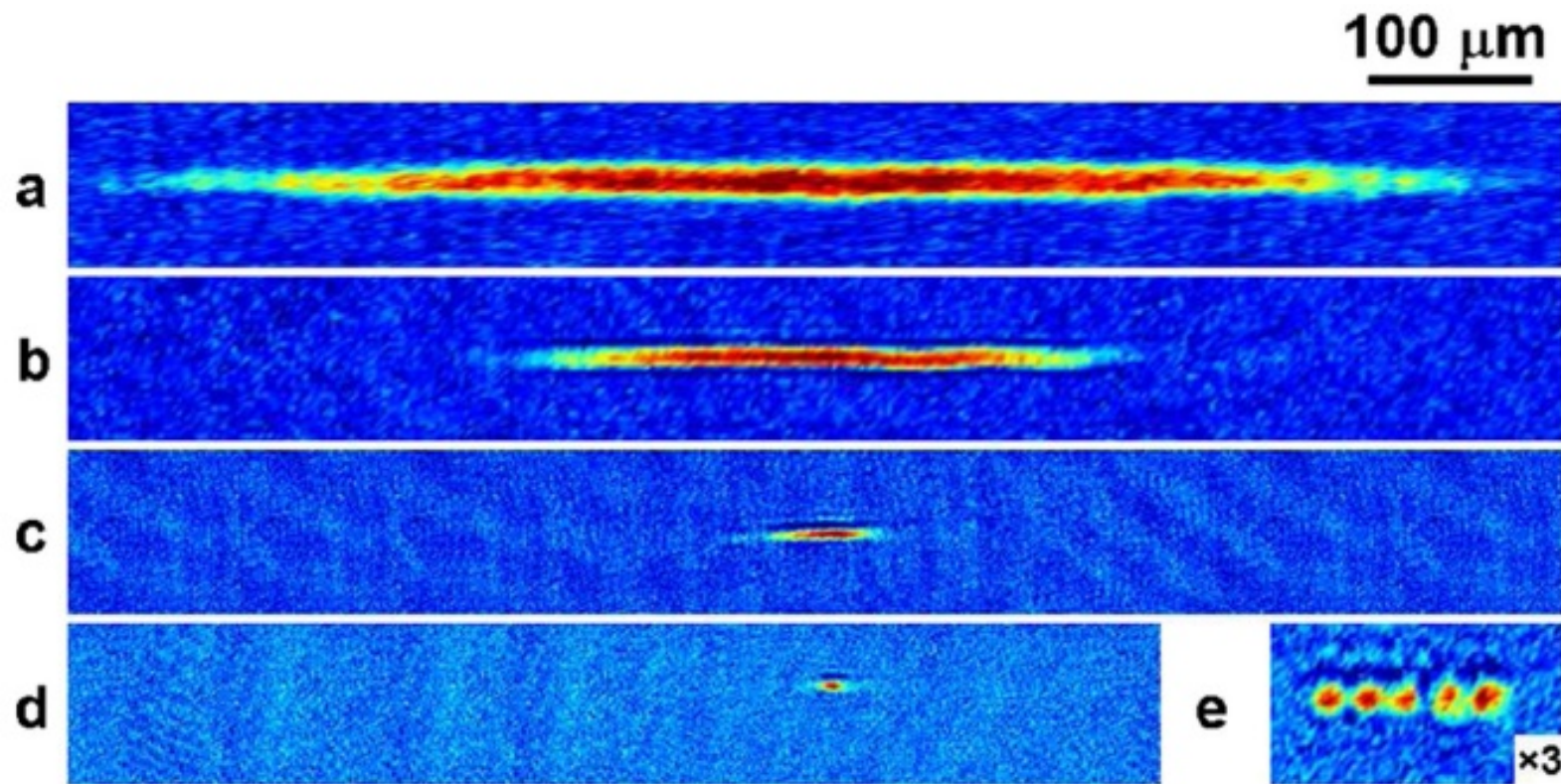
"Observation of Feshbach resonances in a Bose-Einstein condensate."  
S. Inouye *et al.*, Nature **392**, 151 (1998).

“U” is modified by seven orders of magnitude



"Extreme Tunability of Interactions in a 7Li Bose-Einstein Condensate"  
S. E. Pollack, D. Dries, M. Junker, Y. P. Chen, T. A. Corcovilos, and R. G. Hulet,  
Physical Review Letters 102, 090402 (2009).





$$i\hbar \frac{\partial \psi(r)}{\partial t} = \left( -\frac{\hbar^2}{2m} \nabla^2 + V_{\text{trap}}(r) + \frac{4\pi\hbar^2 a}{m} |\psi(r)|^2 \right) \psi(r)$$

"Extreme Tunability of Interactions in a 7Li Bose-Einstein Condensate"  
 S. E. Pollack, D. Dries, M. Junker, Y. P. Chen, T. A. Corcovilos, and R. G. Hulet,  
 Physical Review Letters 102, 090402 (2009).

# *Outline*

*How to cool atoms*

*Properties of BEC*

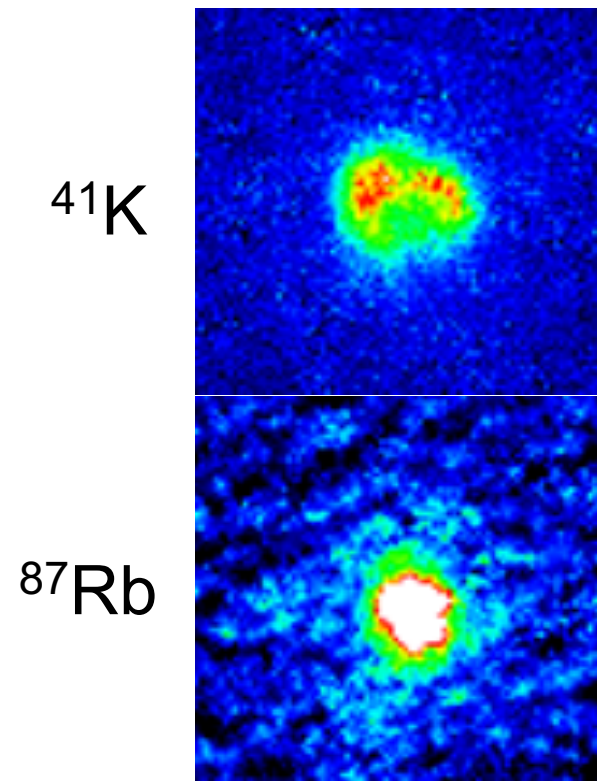
*Tuning interactions (Feshbach resonance)*

*Cold molecules*

*Conclusion and Outlook*

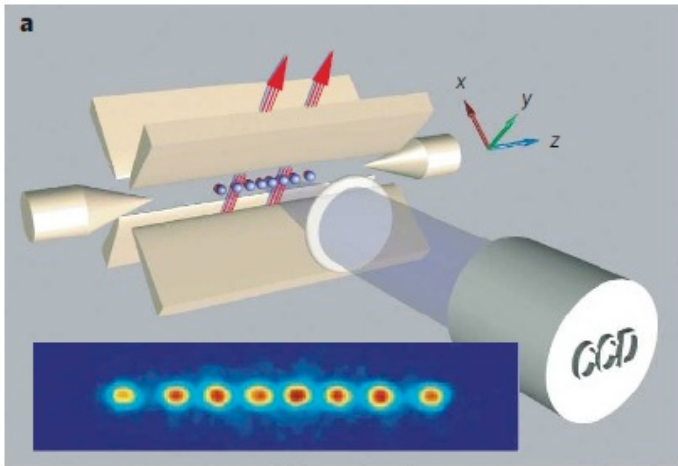


*What can we do with two BECs?*



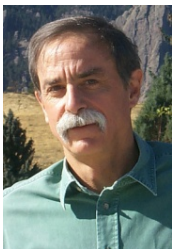
*Make molecules!?*

## Cold ions (trapped ions)

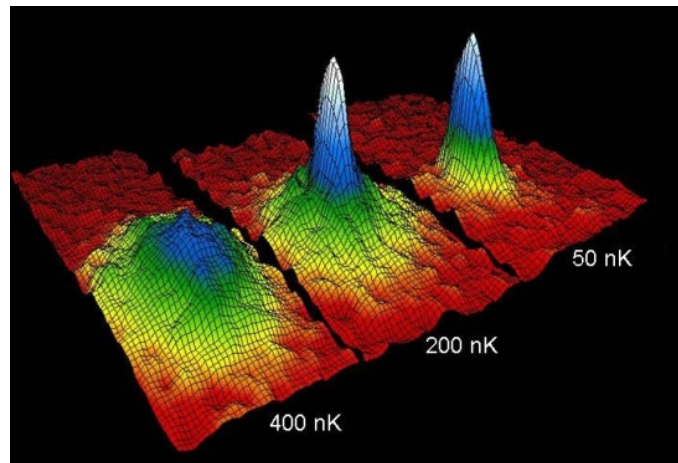


Blatt & Wineland, Nature  
453 1008 (2008)

- Frequency standards
- Quantum Information

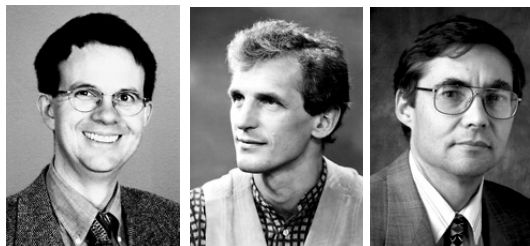


## Cold atoms



Anderson et al., Science,  
269 198 (1995)

- Bose Condensation
- Strongly correlated gas
- Frequency standards

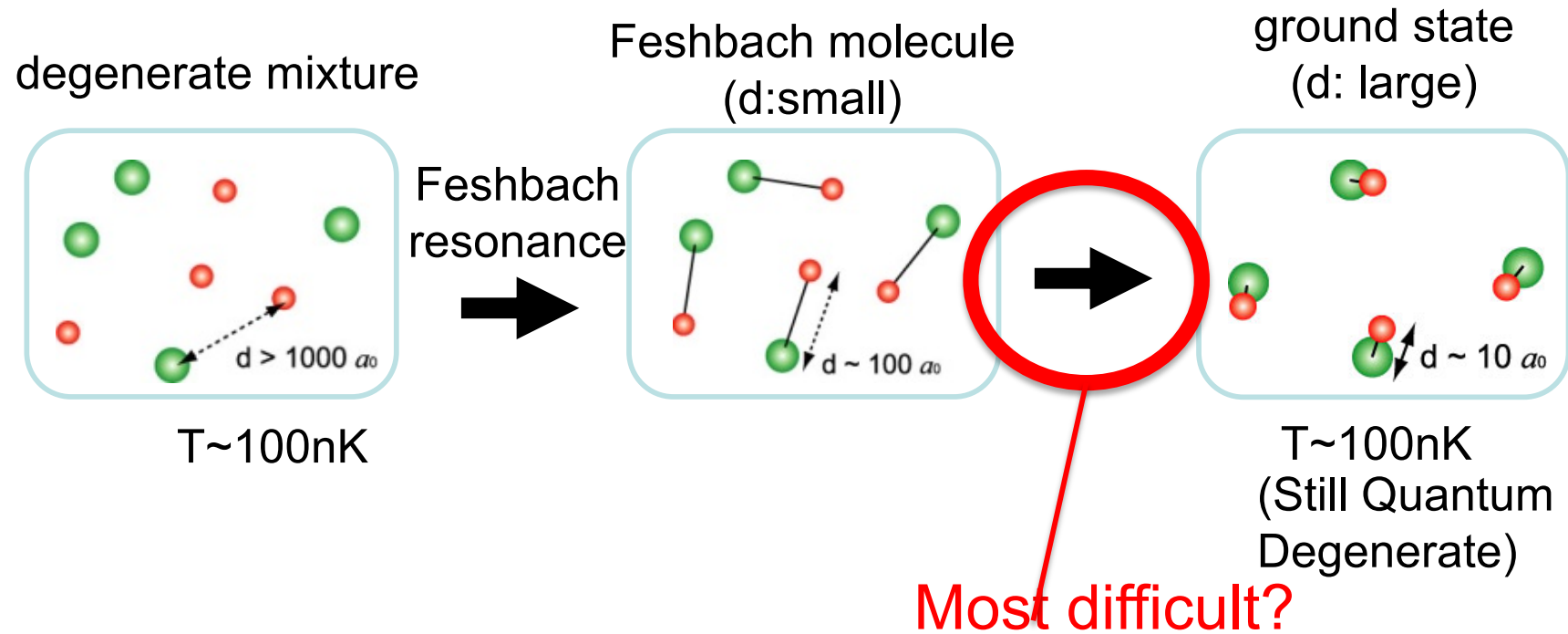


## *Cold molecules?*



“New Frontier”

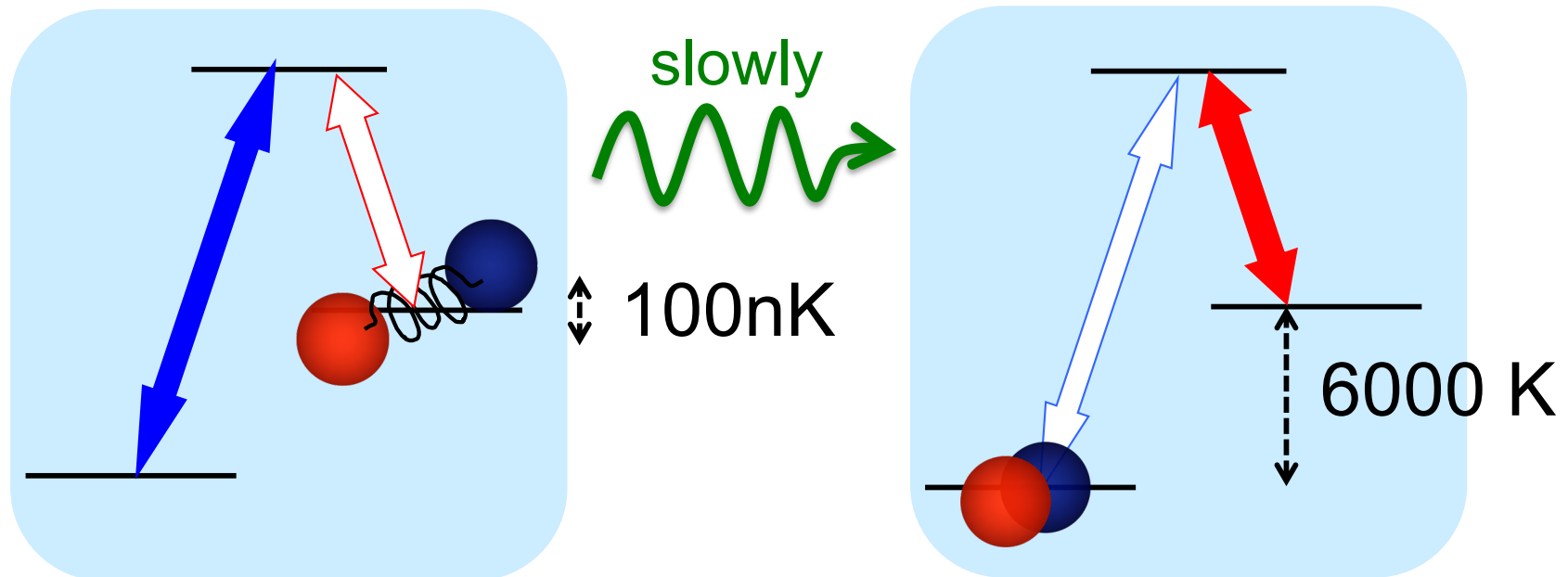
## “Indirect” method (2005~)





No heating: 100nK out of 6000K will kill the sample!

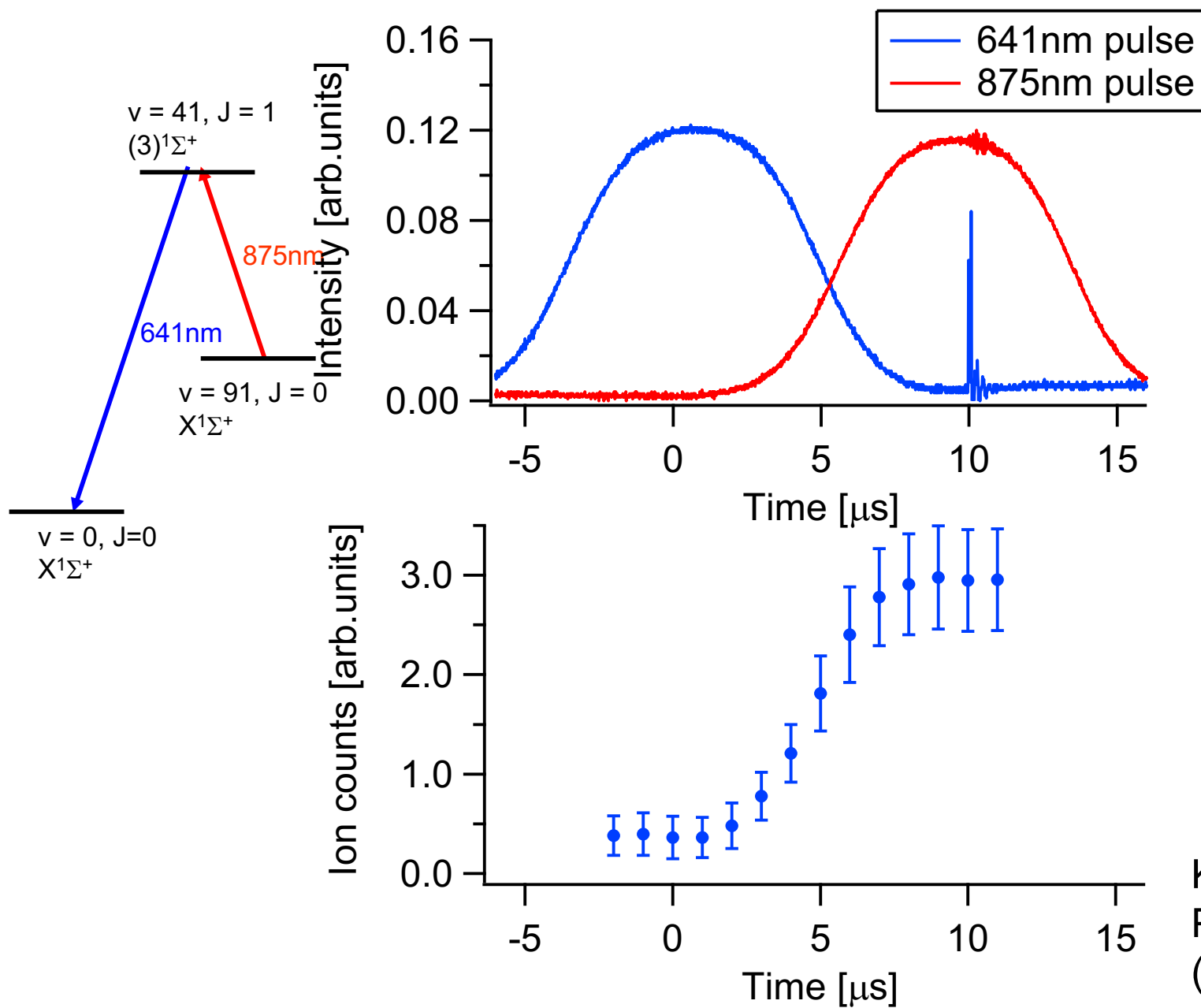
## STIRAP



\*Stimulated Raman Adiabatic Passage

- Find the right excited state
- Stabilize two laser frequencies in  $\sim 10^{-10}$  level (i.e.  $\sim$ kHz level)

# Achieving rovibrational ground state



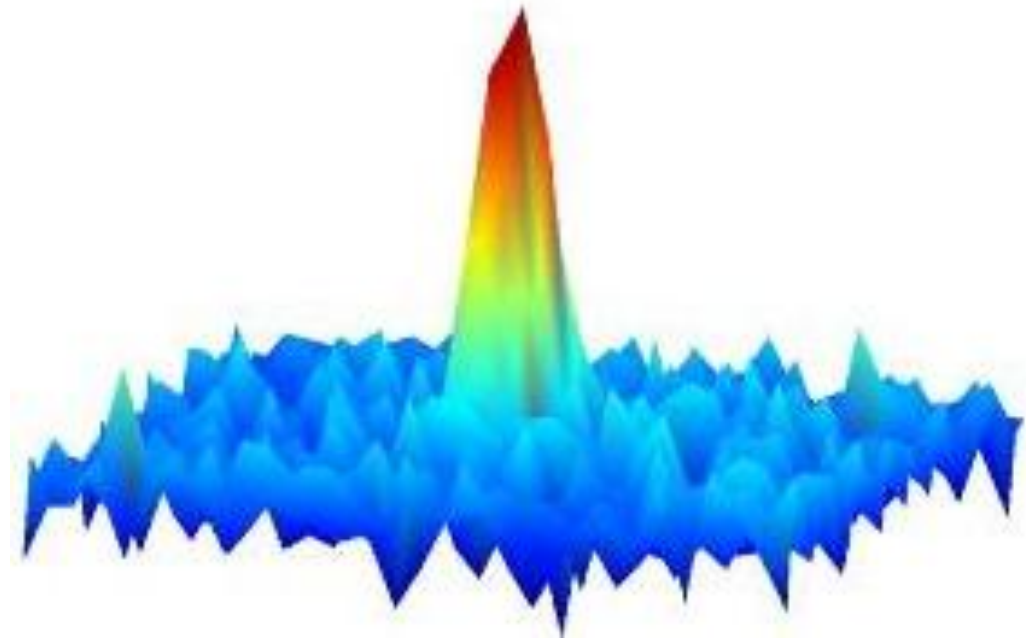
K. Aikawa et al.,  
PRL **105**, 203001  
(2010)

*There is a good news and bad news...*

*--- Good news is we produced ultracold  
groundstate polar molecules!*

*--- Bad news is the density is really really low!*

# Ultracold polar molecules near degeneracy (by JILA)

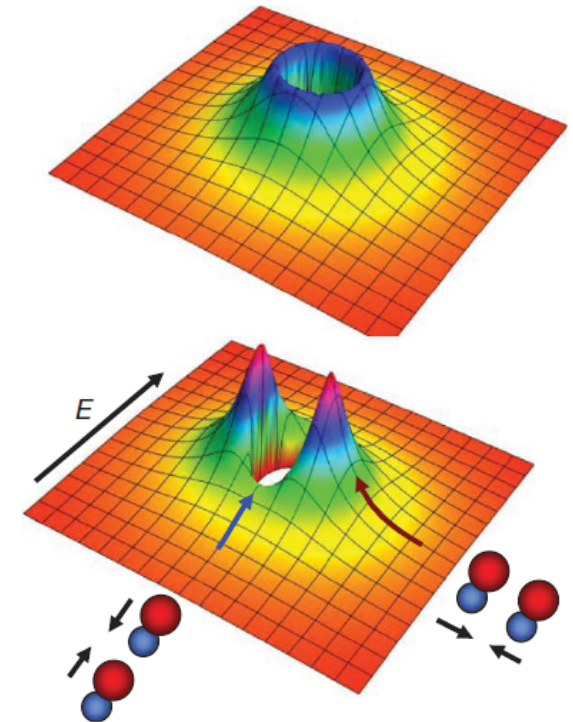
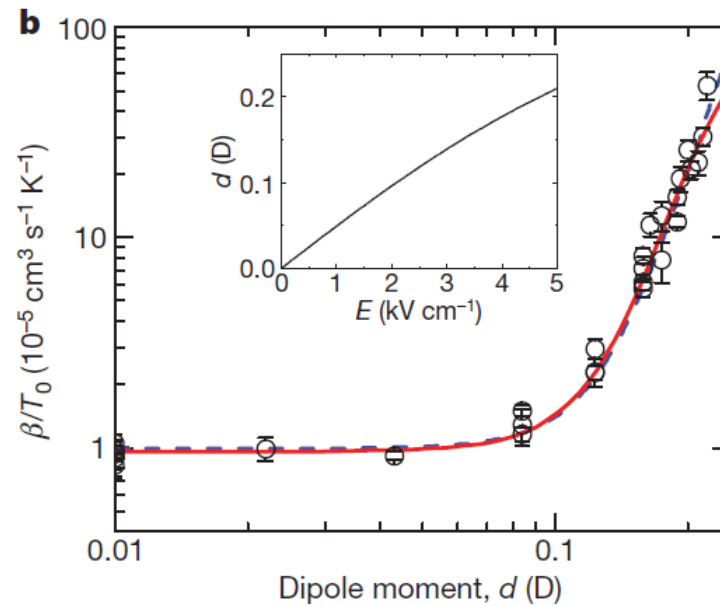
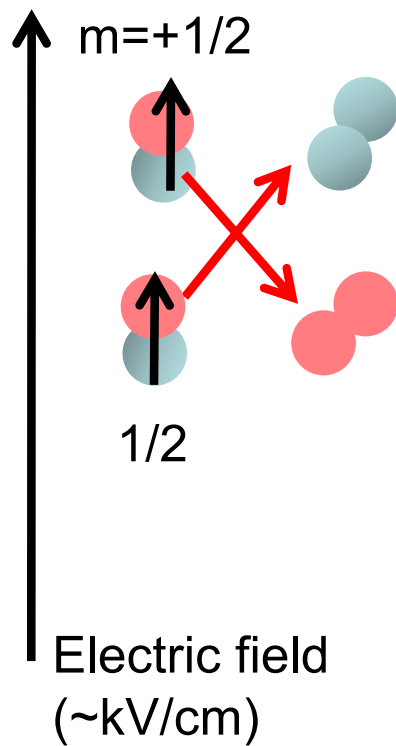


Ultracold KRb molecules imaged by direct absorption  
D.S. Jin and J. Ye, Physics Today, May 2011

# Directional chemistry (JILA)



same internal states AND  
dipoles aligned by an external field



K.-K. Ni et al., Nature 464, 1324 (2010)

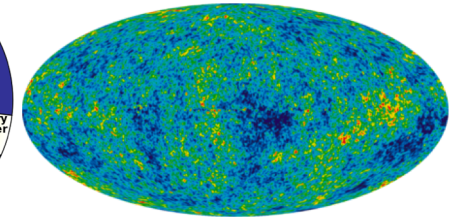
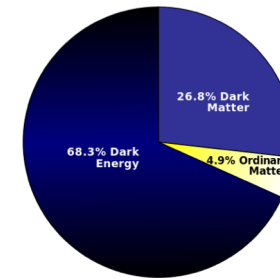
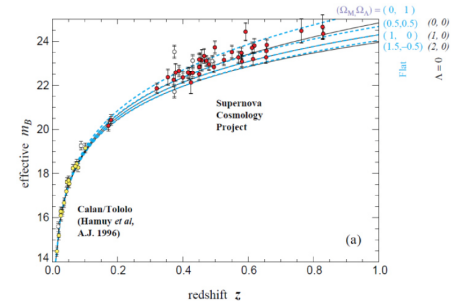


# Measure time variation of fundamental constants!

General relativity +  $\Lambda$ -CDM model is successful in explaining following phenomena:

- accelerating expansion of universe
- Cosmic Microwave Background
- Large scale structure

However, origin of dark energy (and dark matter) is not understood.



## Possible extensions to the $\Lambda$ -CDM

### Quintessence

→ Fluctuation of fundamental constants??

$$\alpha = \frac{1}{4\pi\epsilon_0} \frac{e^2}{\hbar c} \quad \mu = \frac{m_e}{m_p} \approx \frac{1}{1836} \quad g_P, \text{ etc.}$$

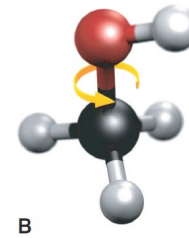
We focused on electron-to-proton mass ratio  $\mu$

# The limit of time variation of $m_e/M_p(\equiv\mu)$

## Radio-astronomical observations

Alcohol in the early universe  
(J. Bagdonaite *et al*, Science 339, 46 (2013))

$$\Delta\mu/\mu = (0.0 \pm 1.0) \times 10^{-7} \quad (\text{in } 7 \times 10^9 \text{ years})$$



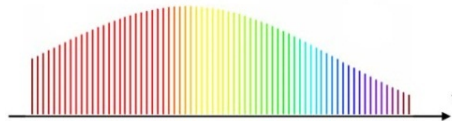
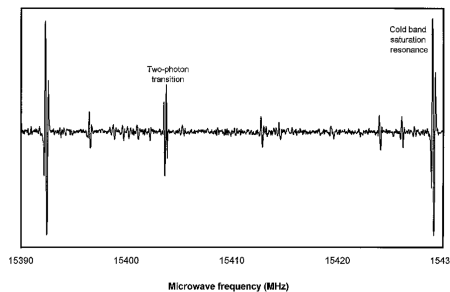
# The limit of time variation of $m_e/M_p(\equiv\mu)$

## Laboratory observations

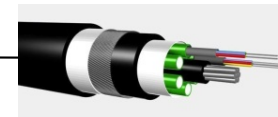
molecular spectroscopy of SF<sub>6</sub>

A. Shelkovnikov et al, PRL 100, 150801 (2008)

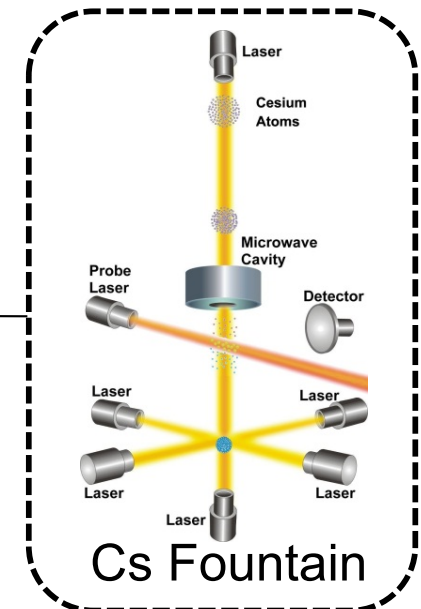
$$\dot{\mu} / \mu = (3.8 \pm 5.6) \times 10^{-14} / \text{year}$$



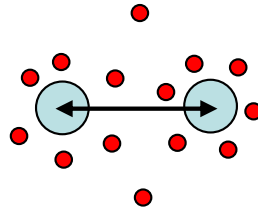
rovibrational transition in SF<sub>6</sub> + frequency comb



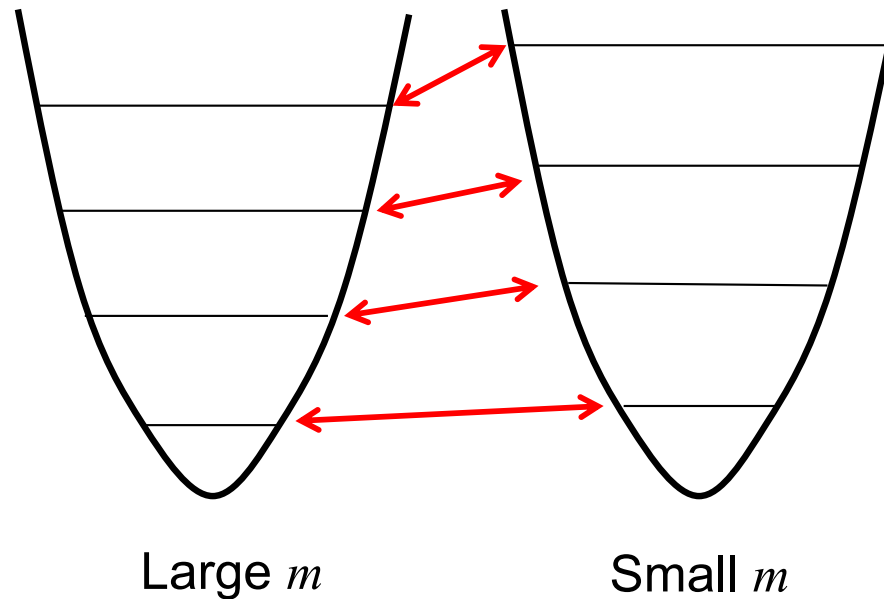
Optical Fiber link (~43km)



# Why molecule?

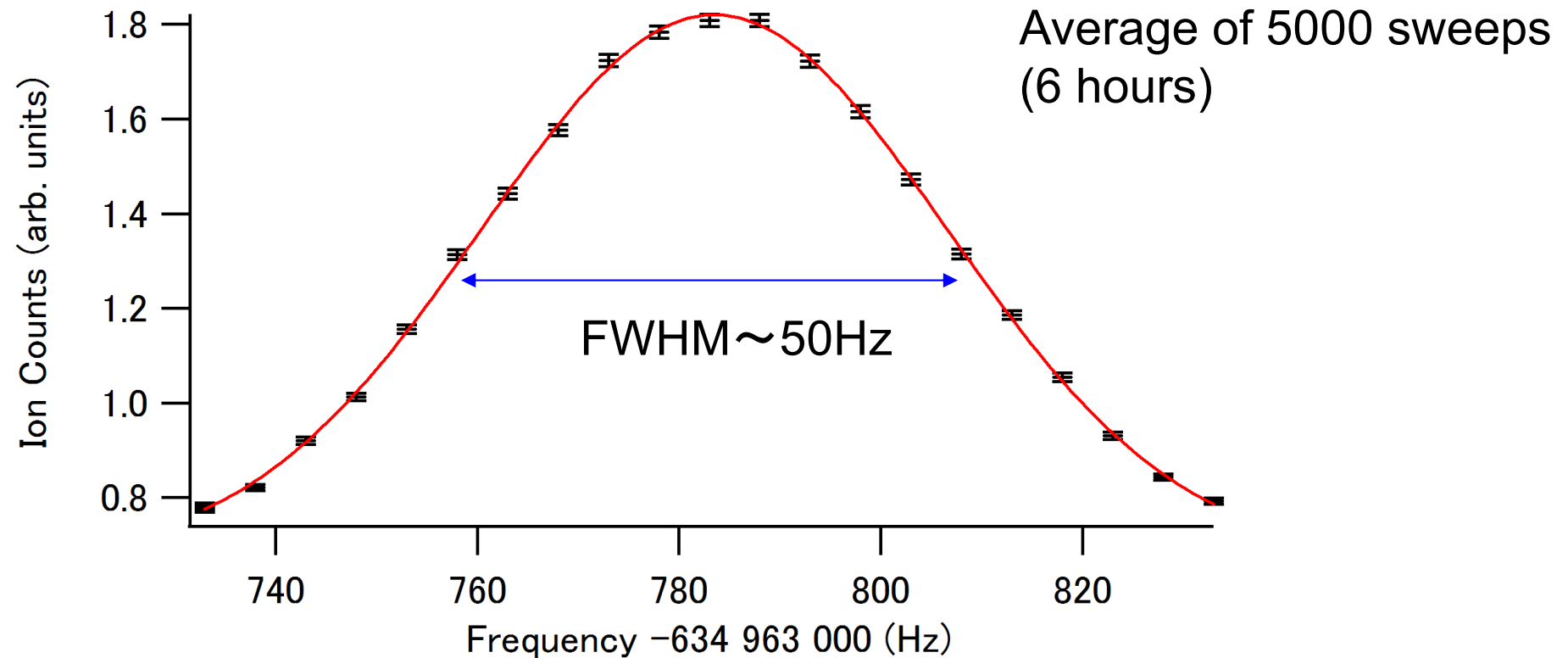


Frequencies are directly related to the inertial mass of nucleus.



$$\frac{\delta E}{E} = \frac{1}{2} \frac{\delta m}{m}$$

# Ultracold molecule is ideal for precision spectroscopy!



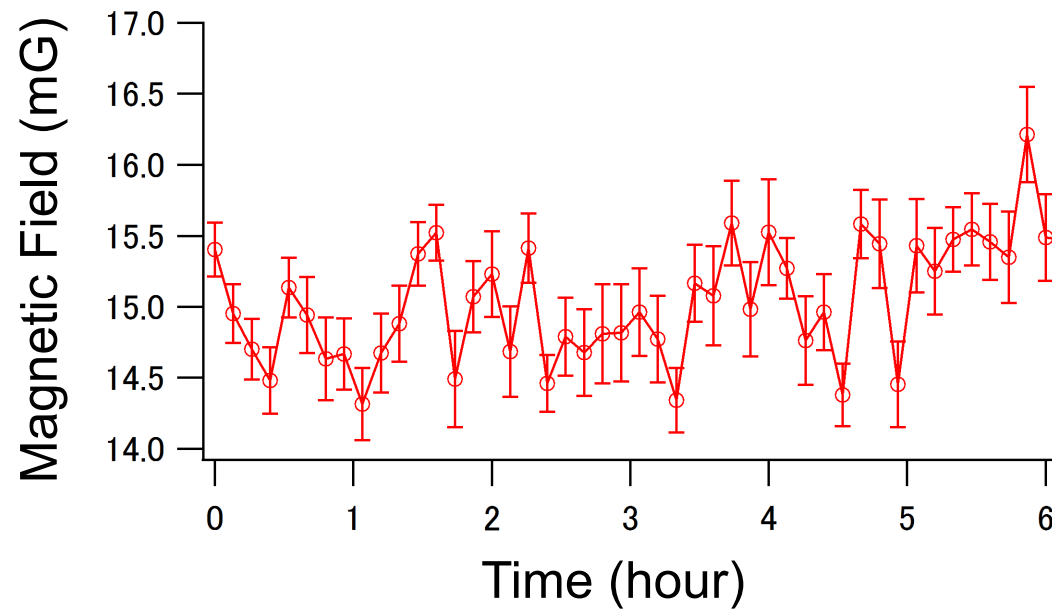
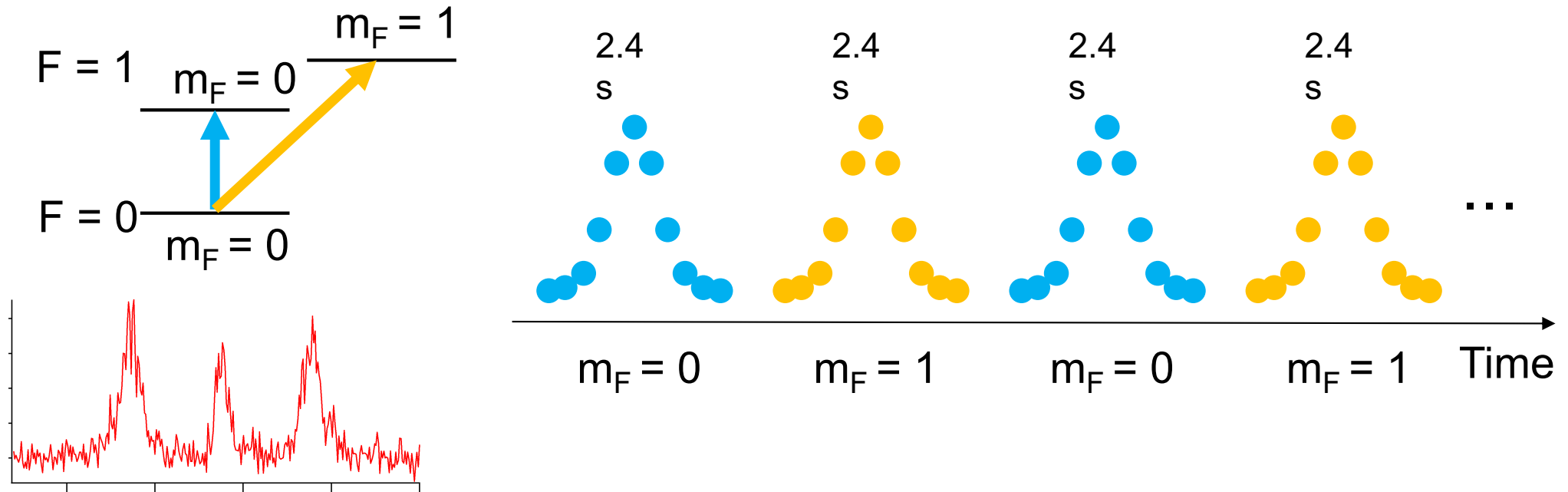
634 963 783.458  $\pm$  0.093 Hz

634 963 781.564  $\pm$  0.094 Hz

Zeeman shift  
compensation

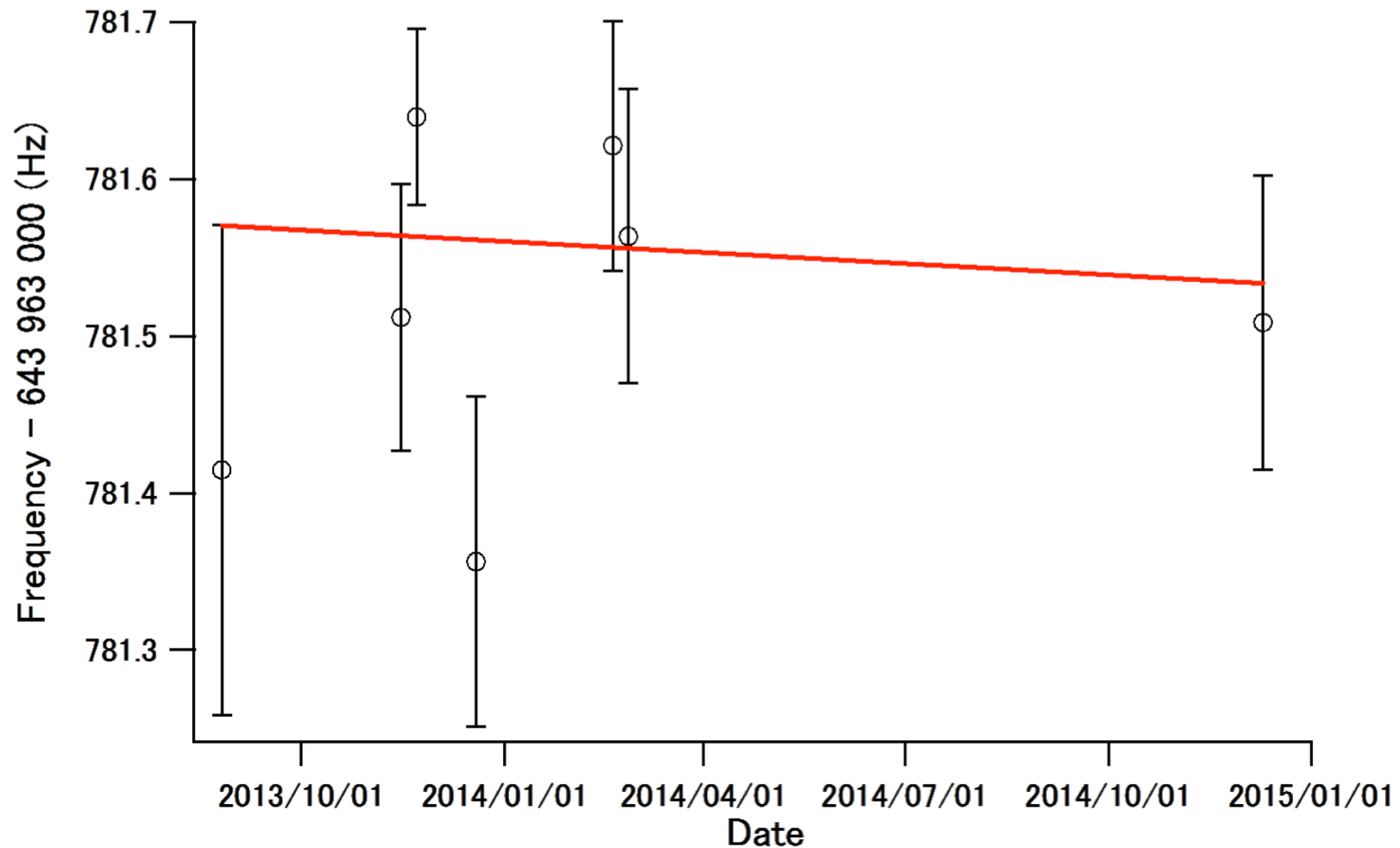
S/N  $\sim 500$  (c.f. Number of molecules used  $\sim 10^6$ )

# Calibration of the magnetic field





# Good News: we broke the world record set by SF<sub>6</sub>!

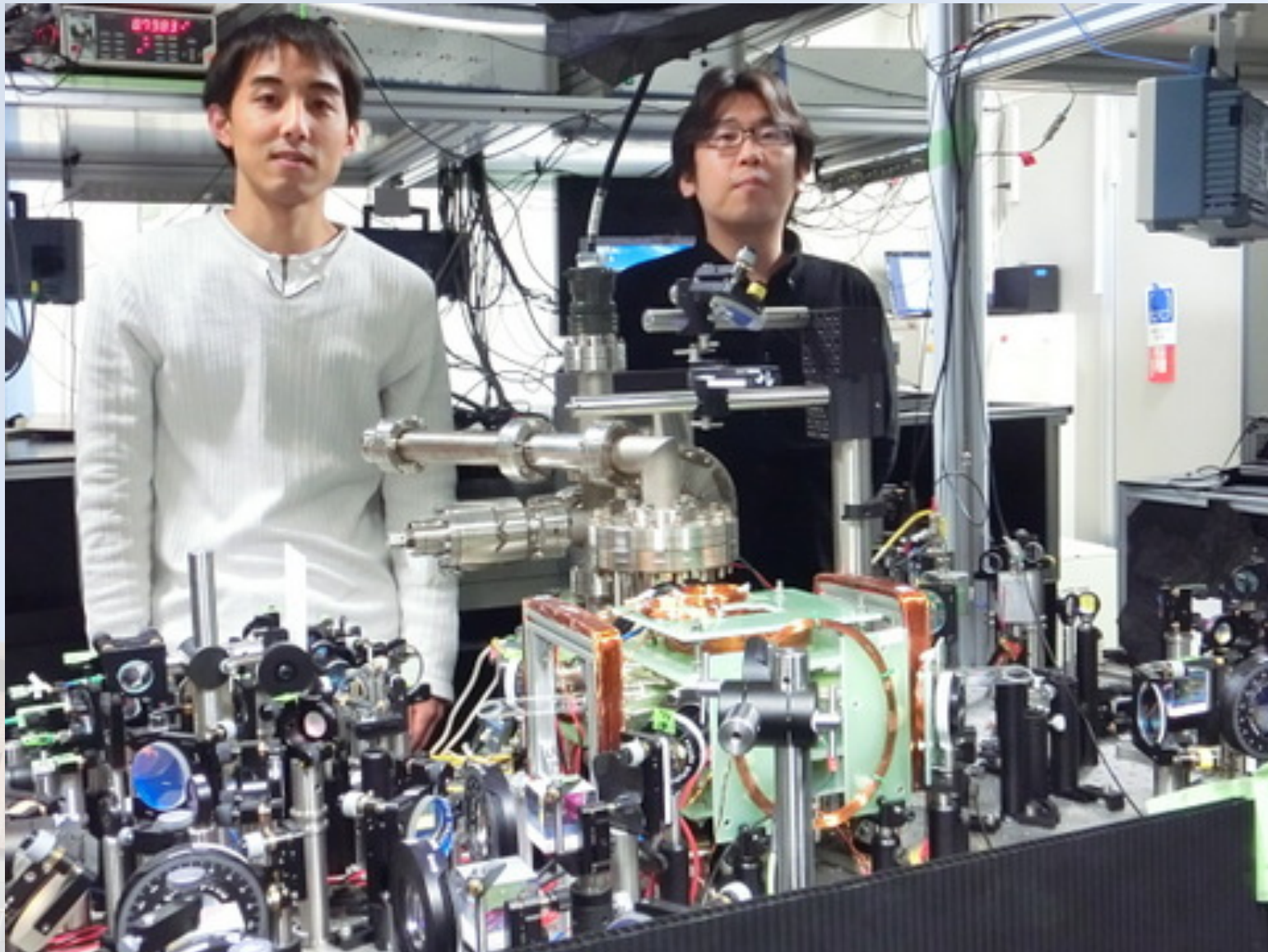


$$\frac{1}{\mu} \frac{\partial \mu}{\partial t} = (0.30 \pm 1.00_{\text{Stat}} \pm 0.16_{\text{Sys}}) \times 10^{-14} / \text{year}$$

Factor of  
five improvement

$$\frac{1}{\mu} \frac{\partial \mu}{\partial t} = (3.8 \pm 5.6) \times 10^{-14} / \text{year}$$

A. Shelkovnikov et al.,  
PRL 100, 150801(2008)



J. Kobayashi, A. Ogino, and SI

## Isotopic Shift of Atom-Dimer Efimov Resonances in K-Rb Mixtures: Critical Effect of Multichannel Feshbach Physics

K. Kato,<sup>1,\*</sup> Yujun Wang,<sup>2,†</sup> J. Kobayashi,<sup>3</sup> P. S. Julienne,<sup>4</sup> and S. Inouye<sup>1</sup>

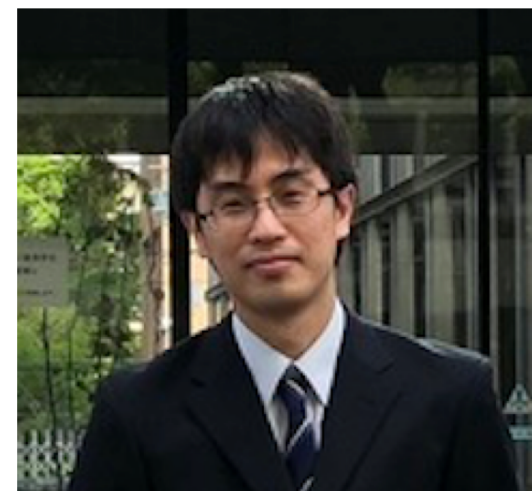
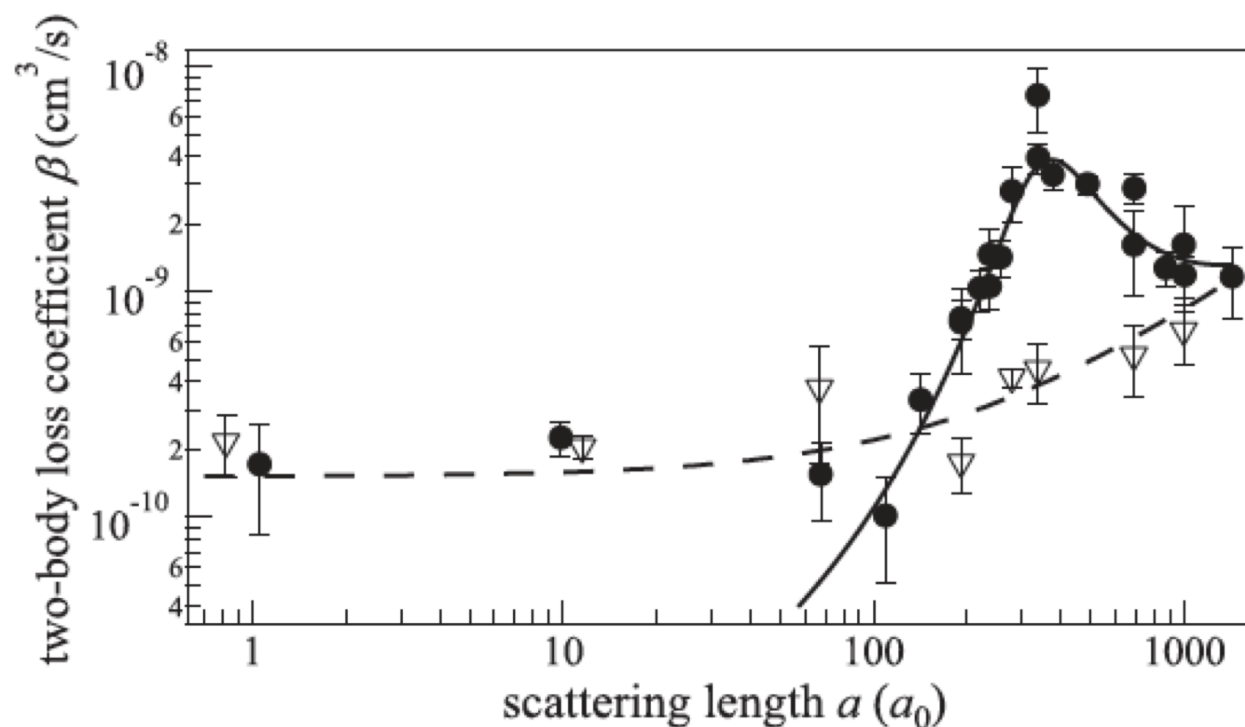
<sup>1</sup>Graduate School of Science, Osaka City University, Sumiyoshi-ku, Osaka 558-8585, Japan

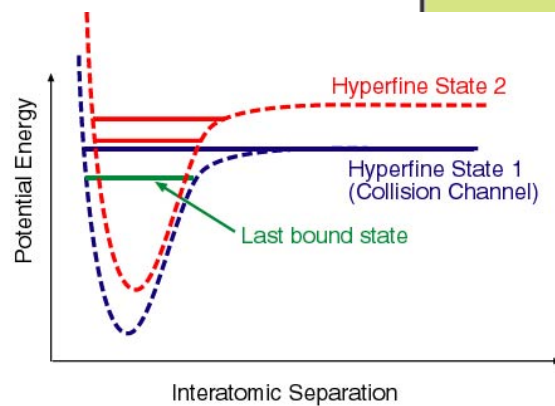
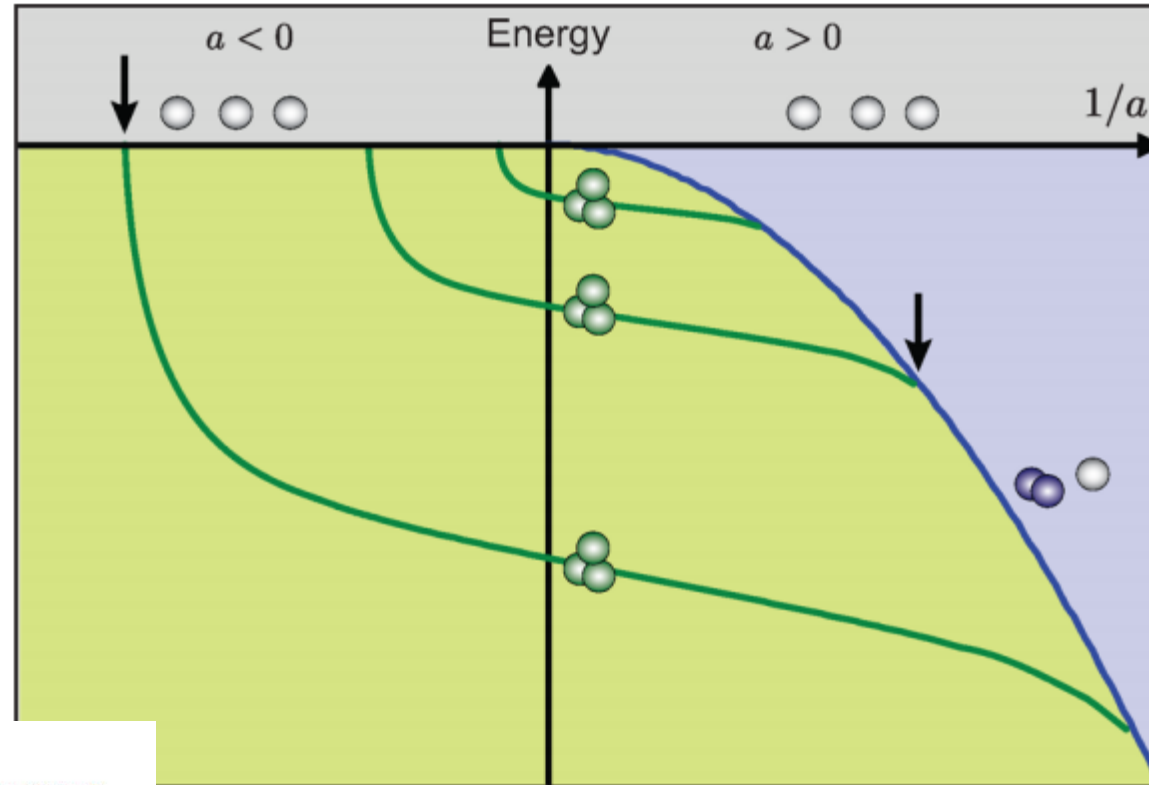
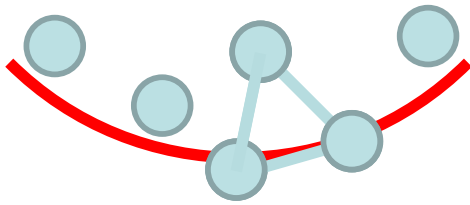
<sup>2</sup>Department of Physics, Kansas State University, 116 Cardwell Hall, Manhattan, Kansas 66506, USA

<sup>3</sup>Department of Physics, Graduate School of Science, Kyoto University, Kyoto 606-8502, Japan

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(Received 25 October 2016; published 17 April 2017)

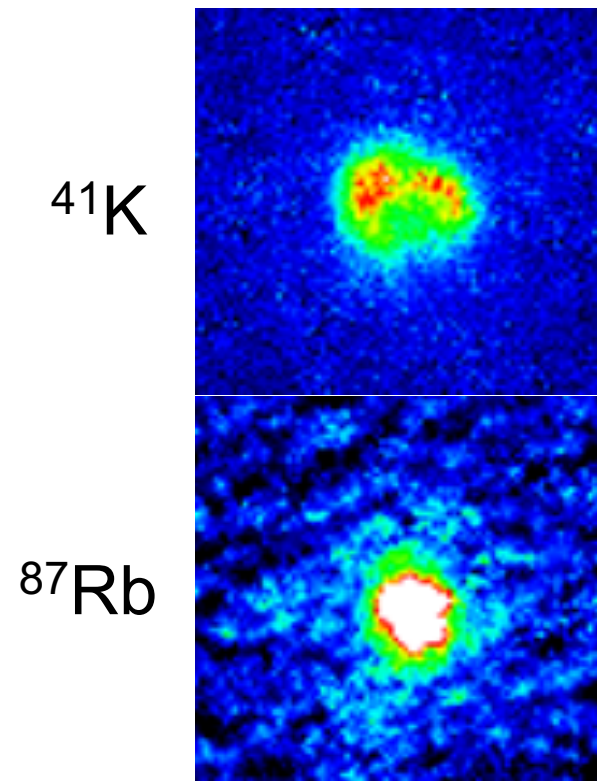




Francesca Ferlaine and Rudolf Grimm,  
*Physics* **3**, 9 (2010).

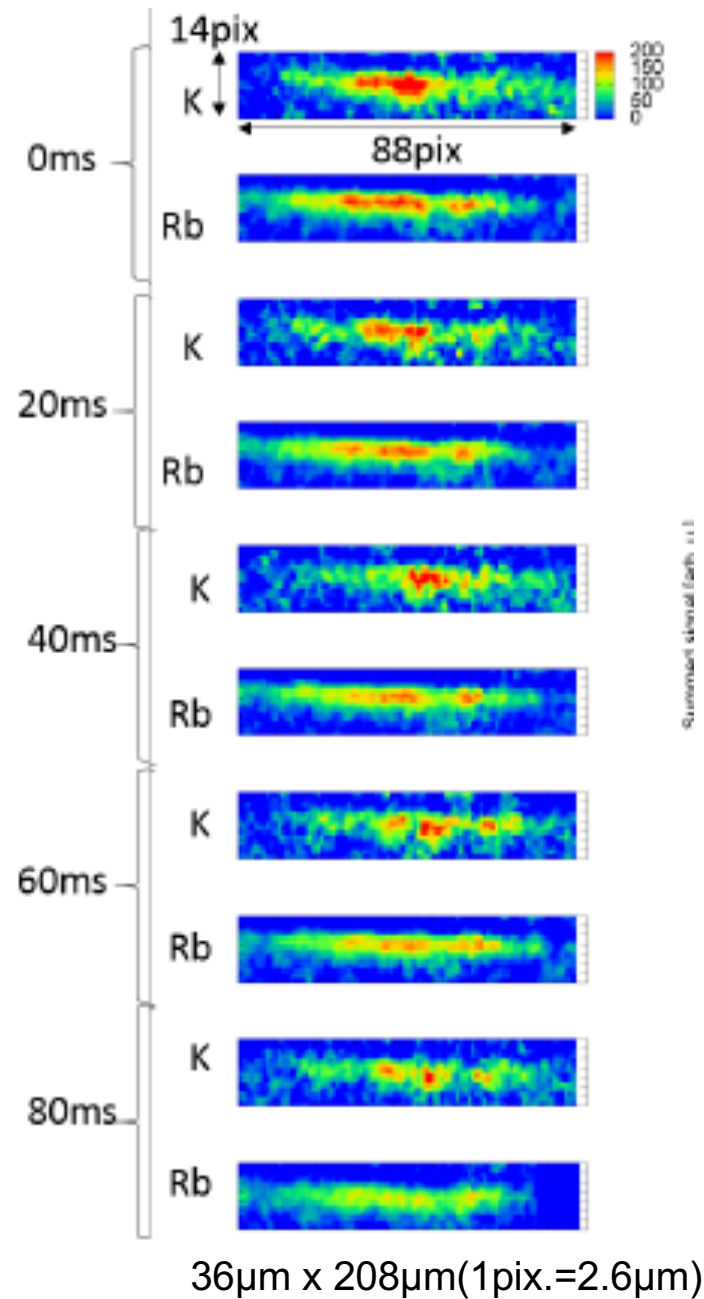


*What can we do with two BECs?*



*Phase separation!?*

# Phase separation after quenching the interaction



1D

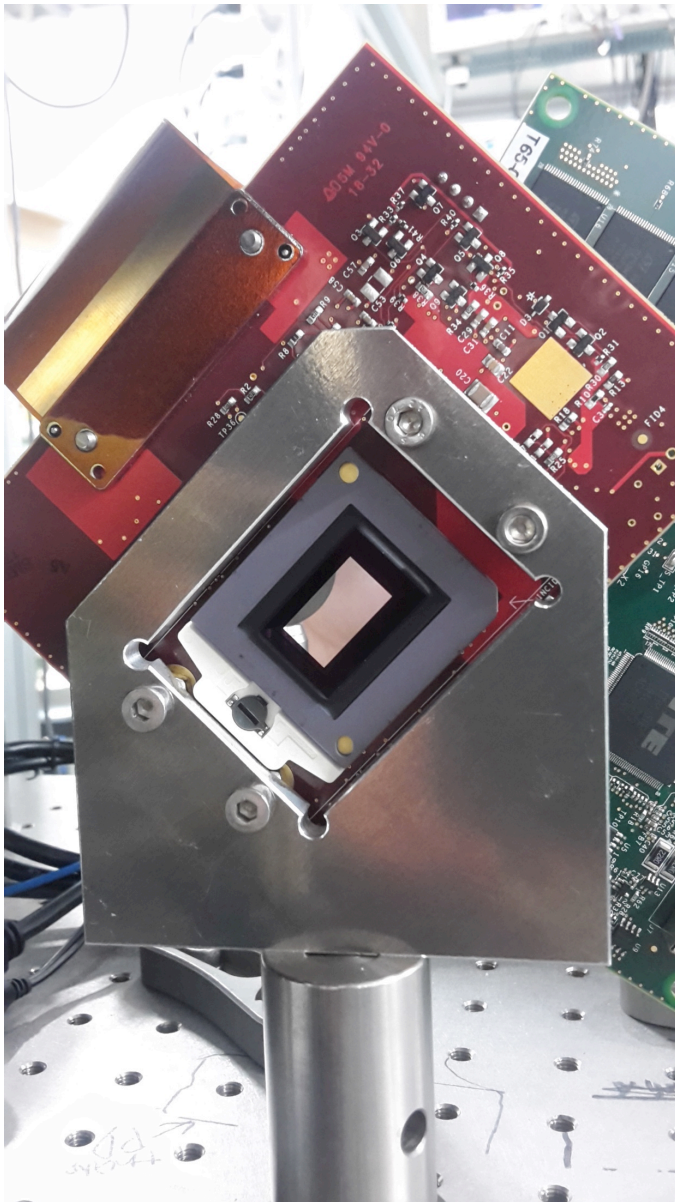


2D

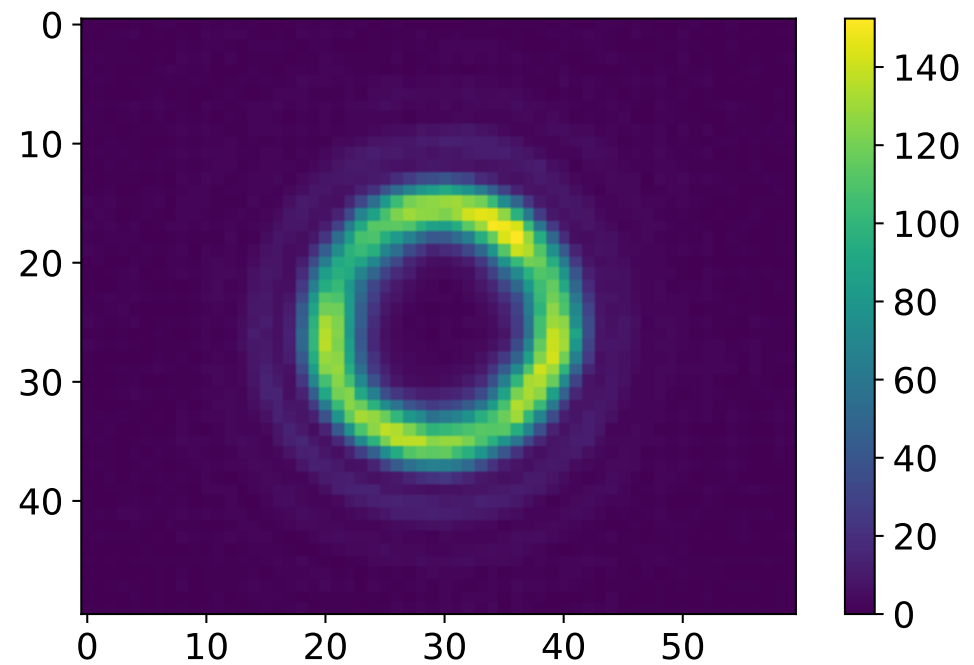




# Digital Mirror Device



## Holographically generated ring beam



# Conclusion

*Cold atom is a versatile ground both for*

*condensed matter physics*

*precision measurement*

*... please stay tuned*

