

The gravity duals of SO/USp superconformal quivers

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M5 on Σ_g

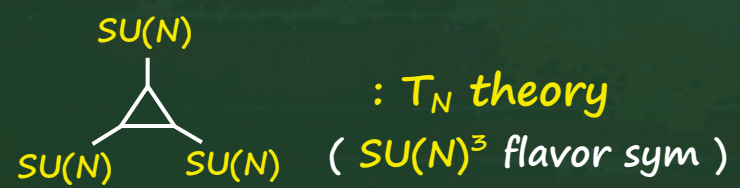
M5 wrapping a Riemann surface [Gaiotto '09]

- N M5-branes on $\Sigma_g \times \mathbb{R}^4$
 $d=4, N=2$ SCFT

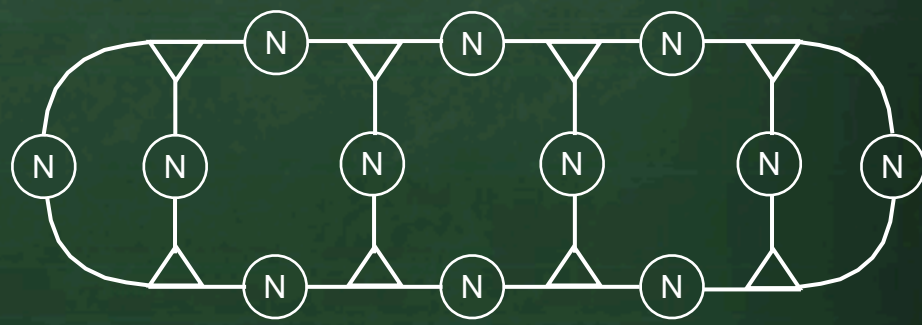


- $SU(N)$ generalized quivers

\textcircled{N} : $SU(N)$ gauge group



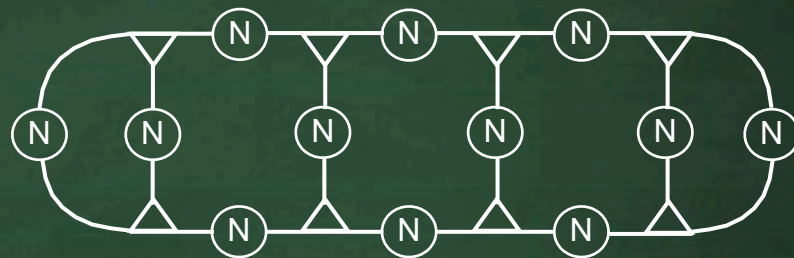
Σ_g



M5 on Σ_g

Gravity duals [Gaiotto-Maldacena '09]

The near horizon geometry of M5 on Σ_g :



$$AdS_5 \times \Sigma_g \times S^4$$

Here S^4 is non-trivially fibered over Σ_g , and the geometry has the symmetry

$$SU(2) \times U(1)$$

The **conformal anomaly** matches the field theory calculation:

$$\text{gravity side: } c = \frac{\pi R_{AdS_5}^3}{8G_N^5} = \frac{N^3}{3}(g-1),$$

$$\text{field theory side: } c = \frac{2n_v + n_h}{12} = \left(\frac{N^3}{3} - \frac{N}{6} - \frac{1}{6} \right) (g-1)$$

$$\begin{array}{c}
 SU(N) \\
 \triangle \\
 \begin{array}{cc}
 SU(N) & SU(N)
 \end{array}
 \end{array}$$

$$n_v = \frac{2N^3}{3} - \frac{3N^2}{2} - \frac{N}{6} + 1$$

$$n_h = \frac{2N^3}{3} - \frac{2N}{3}$$



Q: What is its *SO/USp* counterpart?



M5 on Σ_g with orbifolding

SO/USp generalized quivers [Tachikawa '09]

2N M5 on top of R^5/Z_2

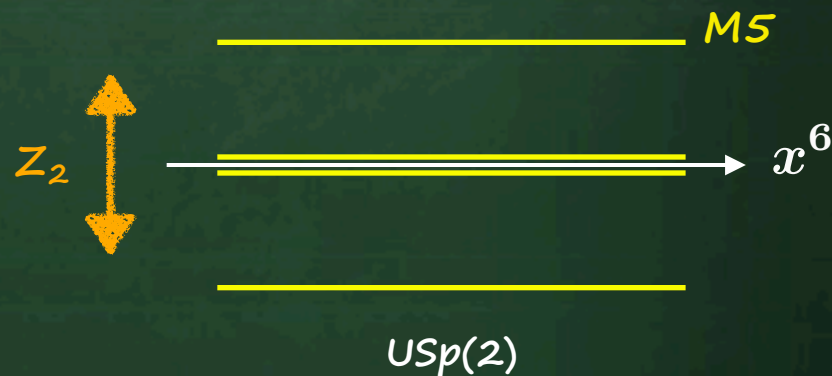


$\left\{ \begin{array}{l} SO(2N) \\ USp(2N-2) \end{array} \right\}$ gauge groups in 4dim

	$0 \sim 3$	R^5/Z_2	Σ_g	
M5	○	x	○	○

For $USp(2N-2)$, two M5 are localized at the Z_2 fixed plane.

[Hori '98]

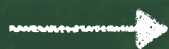


M5 on Σ_g with orbifolding

SO/USp counterparts of T_N theory

[Tachikawa '09]

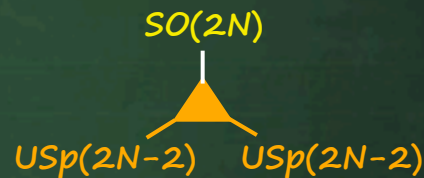
There are **two** counterparts.



T_{SO} theory





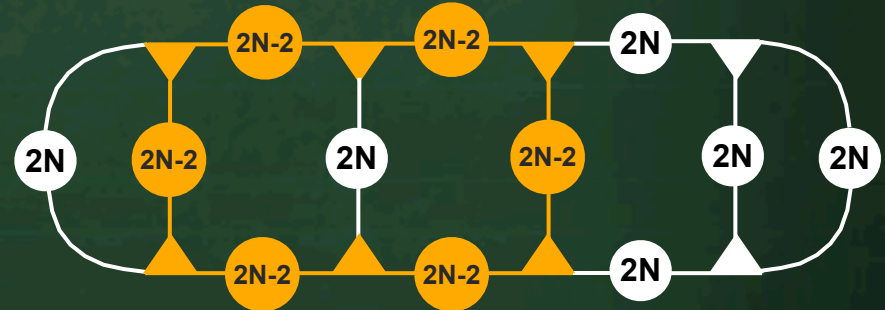
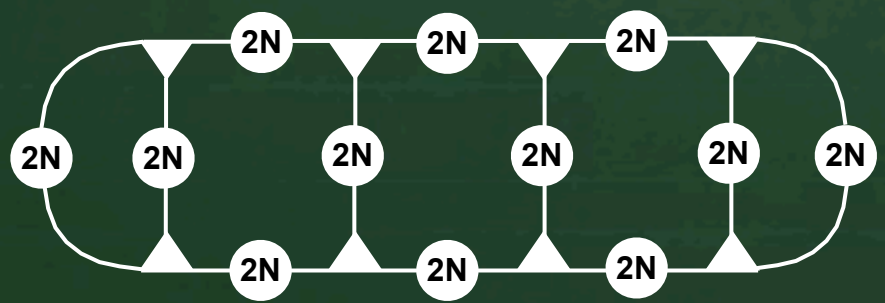
\tilde{T}_{SO} theory



Their anomaly contributions n_v and n_h are read off via S-duality.

There are several quivers sharing the same Σ_g .

-  : $SO(2N)$ gauge group
-  : $USp(2N-2)$ gauge group



M5 on Σ_g with orbifolding

Gravity duals

The difference between SO and USp is subleading in large N .

→ The dual **geometry** is determined by Σ_g as

$$AdS_5 \times \Sigma_g \times RP^4$$

(In comparison with SU -quivers, S^4 is replaced by RP^4)



M5 on Σ_g with orbifolding

Gravity duals

The difference between SO and USp is subleading in large N .

→ The dual **geometry** is determined by Σ_g as

$$AdS_5 \times \Sigma_g \times RP^4$$

(In comparison with SU -quivers, S^4 is replaced by RP^4)

→ The holographic conformal anomaly

$$c = \frac{\pi R_{AdS_5}^3}{8G_N^5} = \frac{4N^3}{3}(g-1)$$

is determined by **the genus g** of Σ_g and independent of the choice of SO or USp .



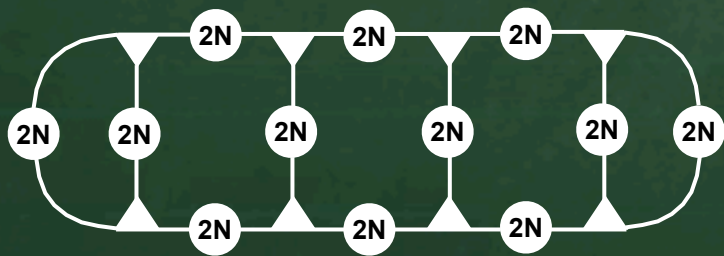
M5 on Σ_g with orbifolding

In fact, in the field theory side, we can show that n_v and n_h are *equal between theories with the same Σ_g* , by using the facts that

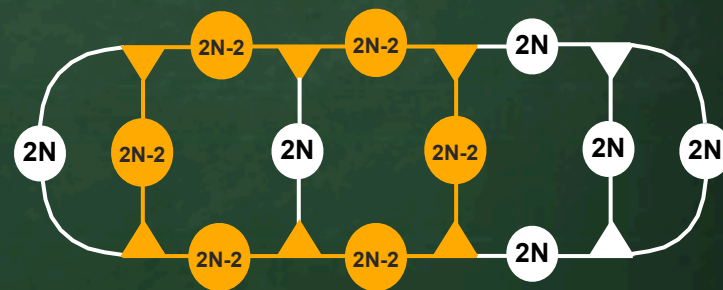
$$\begin{array}{c}
 \text{SO}(2N) \\
 \triangle \\
 \text{SO}(2N) \quad \text{SO}(2N)
 \end{array}
 \quad
 \begin{array}{l}
 n_v = \frac{8N^3}{3} - 7N^2 + \frac{10N}{3} \\
 n_h = \frac{8N^3}{3} - 4N^2 + \frac{4N}{3}
 \end{array}$$

$$\begin{array}{c}
 \text{SO}(2N) \\
 \triangle \\
 \text{USp}(2N-2) \quad \text{USp}(2N-2)
 \end{array}
 \quad
 \begin{array}{l}
 n_v = \frac{8N^3}{3} - 7N^2 + \frac{16N}{3} - 1 \\
 n_h = \frac{8N^3}{3} - 4N^2 + \frac{4N}{3}
 \end{array}$$

For example, both



and



have

$$c = \frac{2n_v + n_h}{12} = \left(\frac{4N^3}{3} - 2N^2 + \frac{5N}{6} \right) (g-1)$$



M5 on Σ_g with orbifolding

Torsion part of G-flux [Hori '98]

The topology of the 3-form potential is measured by

$$H^4(\mathbb{R}P^4 \times S^1, \tilde{\mathbf{Z}}) \simeq \mathbf{Z} \oplus \mathbf{Z}_2$$

($\tilde{\mathbf{Z}}$: integers *twisted* by the orientation bundle)

Torsion part

$$\begin{aligned} \mathbf{Z}_2 \ni \vartheta &\equiv \int_{S^1 \times \mathbb{R}P^3} [G_4/2\pi] \\ &= \begin{cases} 0 \cdots \cdots SO(2N) \\ 1 \cdots \cdots USp(2N-2) \end{cases} \end{aligned}$$

M5 on Σ_g with orbifolding

Torsion part of G-flux [Hori '98]

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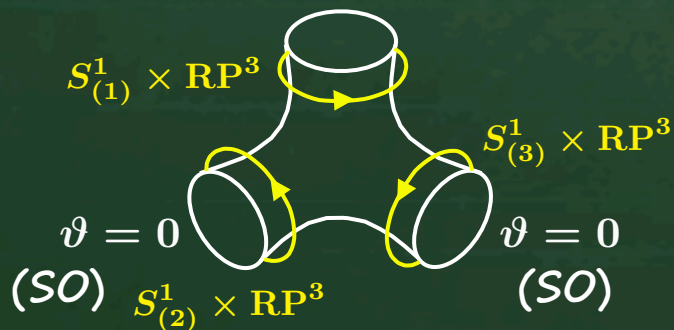
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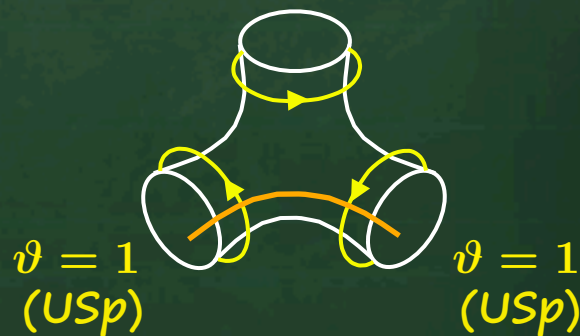
T_{SO} theory

$\vartheta = 0$ (SO)



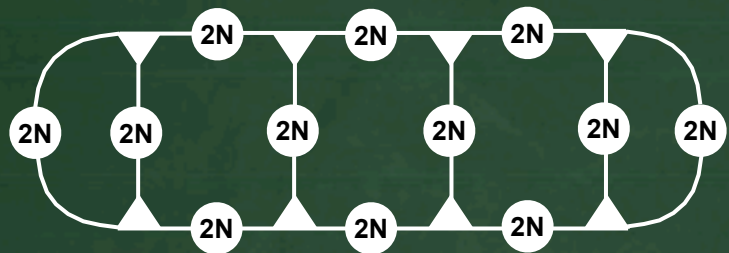
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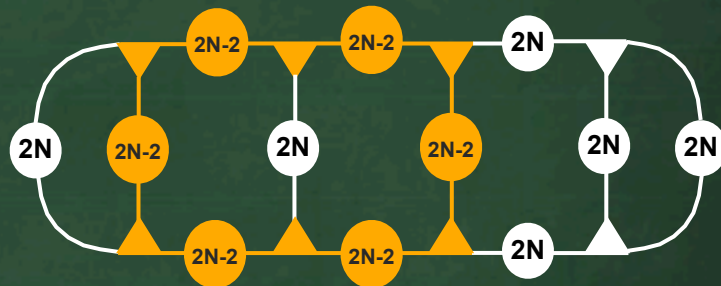


M5 on Σ_g with orbifolding

For example, for



and



the dual gravities are distinguished by the **torsion part of G -flux** along the “B-cycles” of Σ_g :



Summary

- We studied *the gravity duals of SO/USp superconformal quivers*, which are constructed by wrapped M5-brane on a Riemann surface *together with the Z_2 orbifold*.
- For a Riemann surface Σ_g without punctures, the gravity duals are characterized by *the genus g of Σ_g* and *the torsion part of the four-form flux*.
- *The conformal anomalies* of the theory is determined by *the genus g* of Σ_g .
- In the paper, we also studied the gravity duals of *SO/USp tails*. So, if you could take a look at it, I would be very happy!!



That's all for my presentation.

Thank you very much.



M5 on Σ_g

Gravity dual

[Gaiotto-Maldacena]

$$ds^2 = (\pi N l_p^3)^{\frac{2}{3}} \frac{W^{\frac{1}{3}}}{2} \left\{ 4ds_{AdS_5}^2 + 2 \left[4 \frac{dr^2 + r^2 d\beta^2}{(1-r^2)^2} \right] + 2d\theta^2 \right. \\ \left. + \frac{2}{W} \cos^2 \theta (d\psi^2 + \sin^2 \psi d\phi^2) + \frac{4}{W} \sin^2 \theta \left(d\chi + \frac{2r^2 d\beta}{1-r^2} \right)^2 \right\}$$

$$W \equiv 1 + \cos^2 \theta$$

