

関西相対論・宇宙論合同セミナー

17 December 2012, Kyoto

“Studying Gravity with Quantum Optics
~ Test of Gravity at short range
using Bose-Einstein Condensates ~

Kyoto University, JST

Y. Takahashi



Quantum Optics Group Members



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H. Yamada
I. Takahashi

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M. Abe
J. Hutson

M. Baba

Outline

Introduction:

quantum optics researches for studying gravity

Proposed experiment:

test of gravity at short range using Bose-Einstein condensates:

current status and prospects

Outline

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quantum optics researches for studying gravity

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current status and prospects

Gravity and Quantum Optics



Gravitational Effect

↓

Very Weak in Laboratory Scale

↓

Need of Precision Measurement
(sometimes, beyond quantum limit)

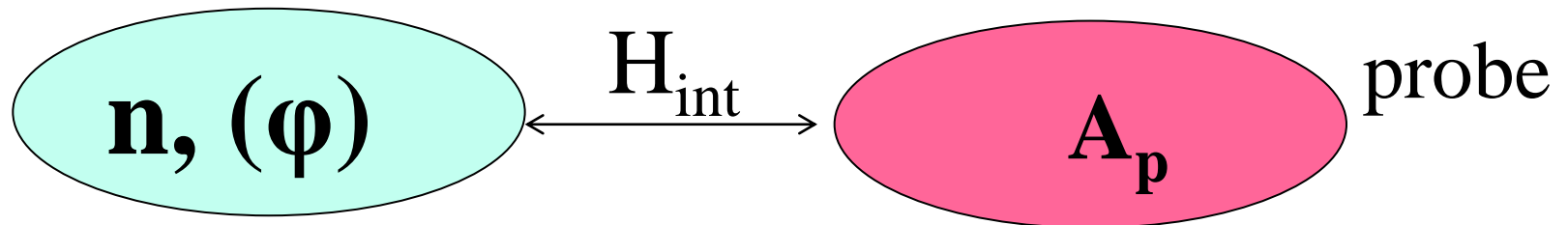


Quantum Optics Approach

Gravity and Quantum Optics

For gravitational wave detection:

Quantum Non-Demolition Measurement (proposed by Braginsky)



$$[\mathbf{n}, H_{\text{int}}]=0 \text{ (Back-action evasion)}$$

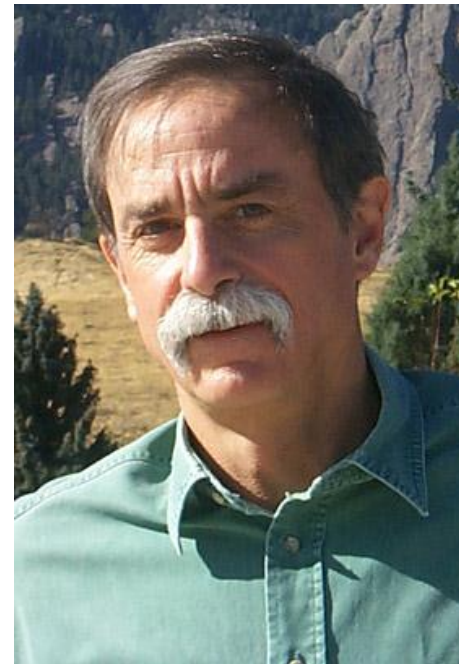
The Nobel Prizes in Physics 2012

"for ground-breaking experimental methods that enable measuring and manipulation of individual quantum systems"

“Development of Quantum Optics”



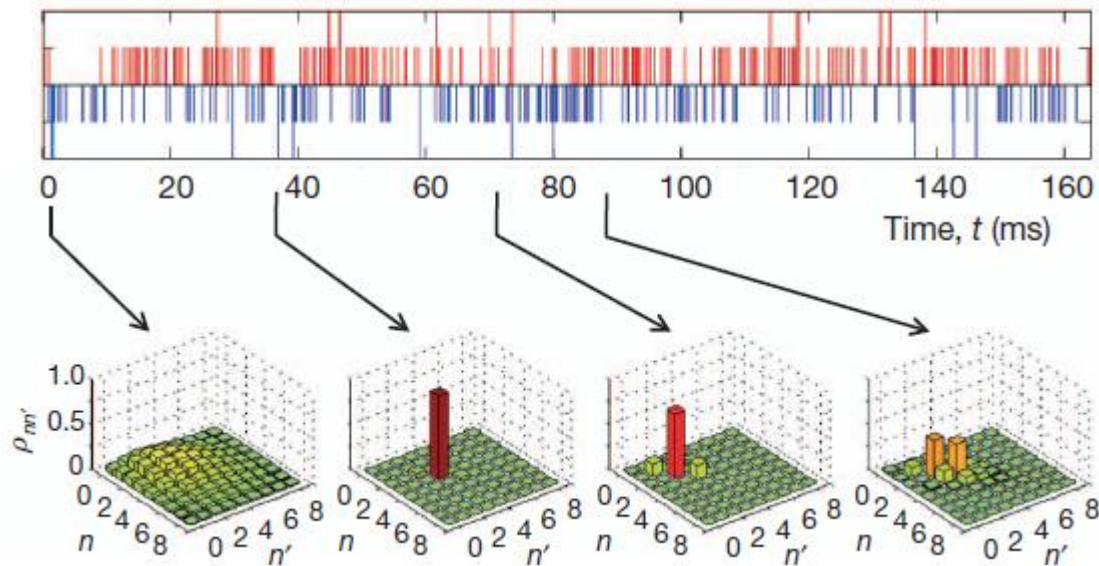
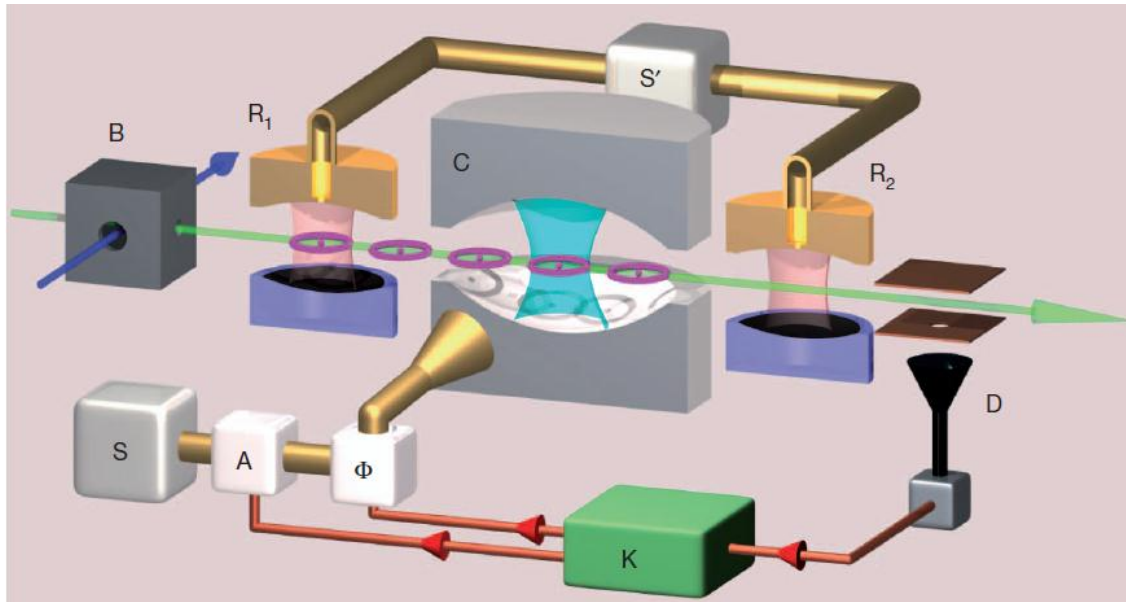
S. Haroche



D. Wineland

QND of photons and Quantum Feedback control

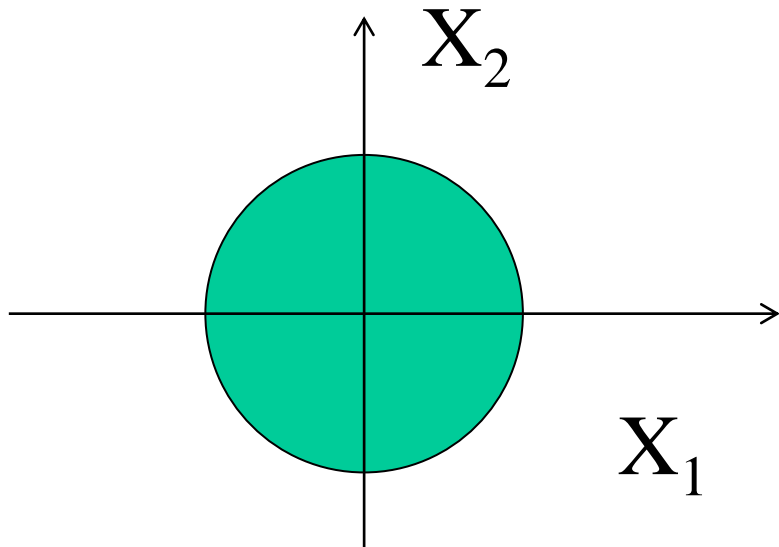
by S. Haroche



Gravity and Quantum Optics

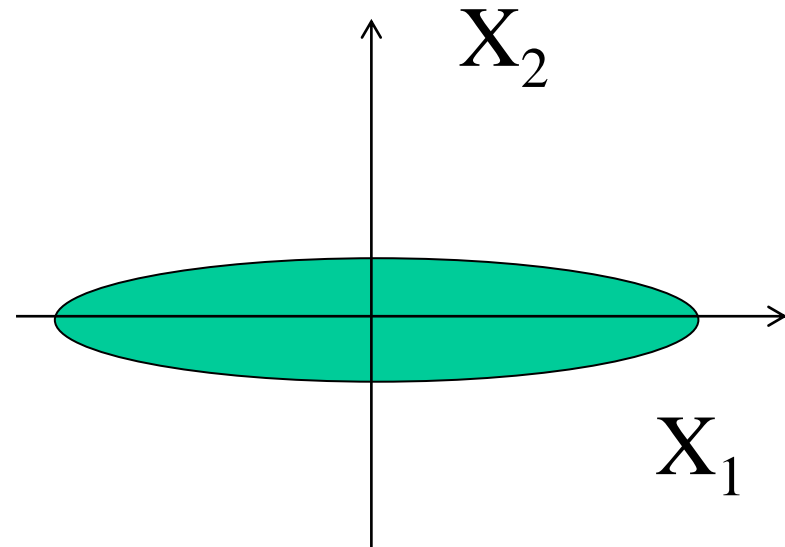
For gravitational wave detection:

Squeezed States of Light $[X_1, X_2] = i/2$
 $\Delta X_1 \Delta X_2 \geq 1/4$



$$\Delta X_1 = \Delta X_2 = 1/2$$

Coherent states (laser)



$$\Delta X_1 > 1/2, \Delta X_2 < 1/2$$

Squeezed states

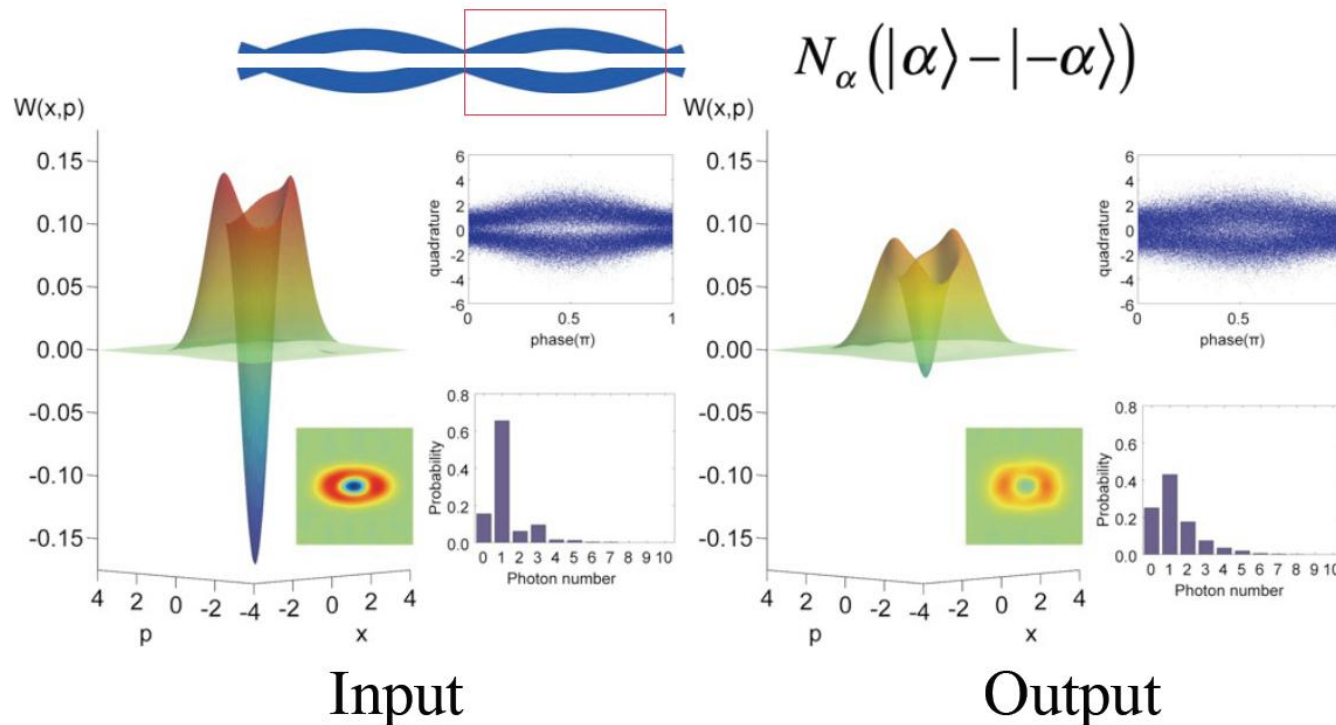
Gravity and Quantum Optics

For gravitational wave detection:

Squeezed States of Light

➡ Important resources for Quantum information processing

Teleportation of a Schrödinger cat state of light



Furusawa G
(U. of Tokyo)

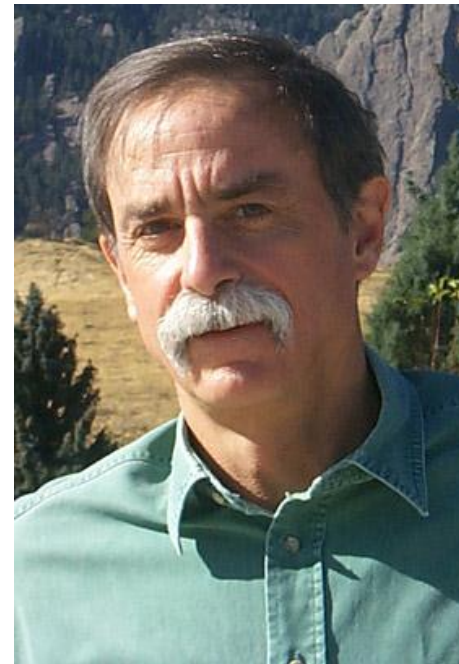
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S. Haroche

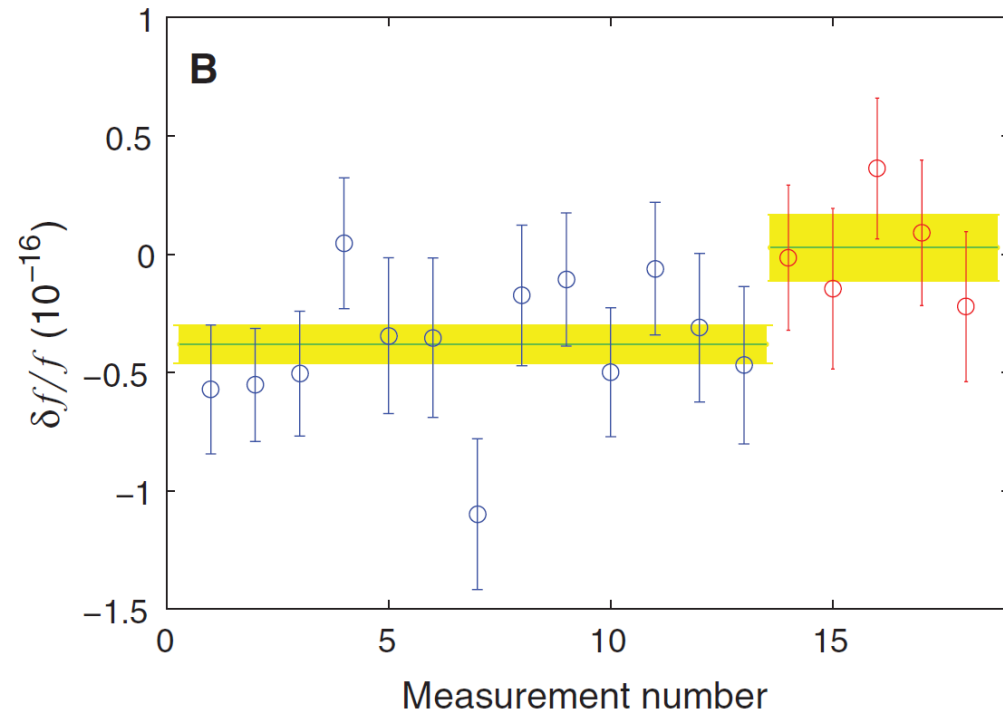
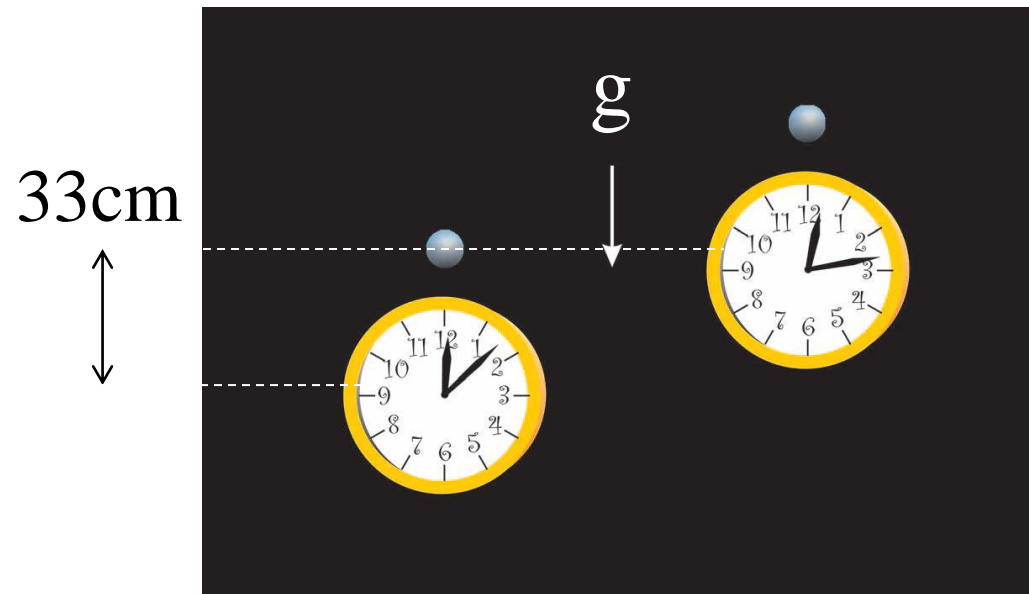


D. Wineland

Optical clocks and relativity

D. Wineland Group, [Science 329,1630 (2010)]

$$\Delta f/f : \sim 10^{-17}!$$



$$\longrightarrow f(\text{Hg}^+)/f(\text{Al}^+) : 10^{-17}$$

$$\dot{\alpha} / \alpha = (-1.6 \pm 2.3) \times 10^{-17} / \text{yr}$$

Precise measurement of g using atoms

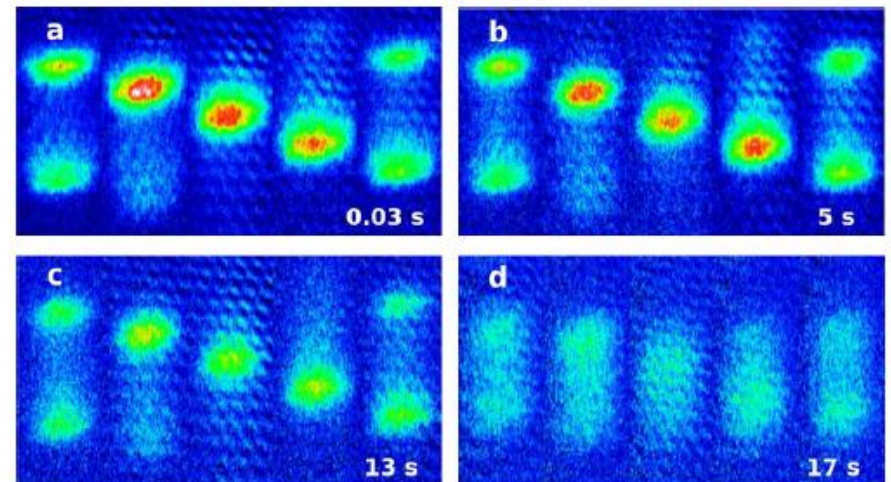
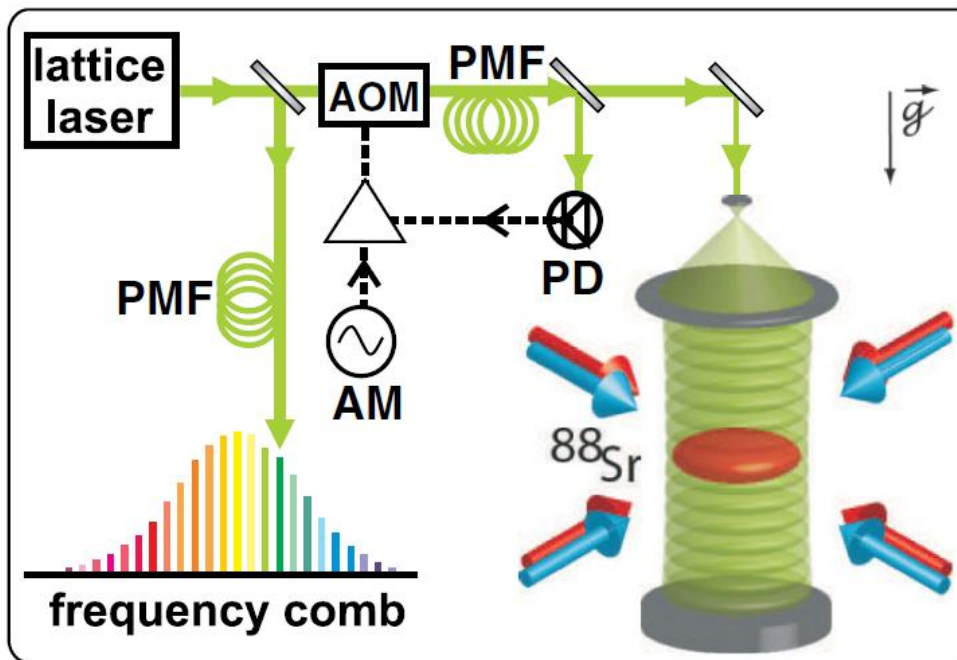
[PRL 106, 038501(2011)]

^{88}Sr atoms: $N \sim 10^6$, $T \sim 0.6 \mu\text{K}$,
almost non-interacting

“Bloch oscillation”

1st BZ: $2\hbar k_L = F \tau_B$, $F = m_{\text{Sr}} g$

$$\nu_B = m_{\text{Sr}} g \lambda_L / 2\hbar$$

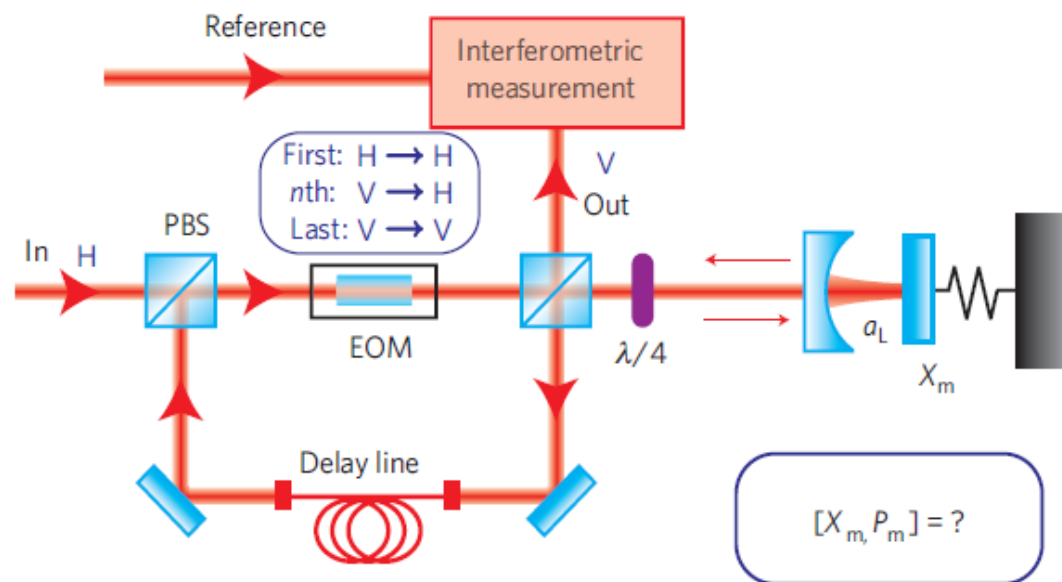
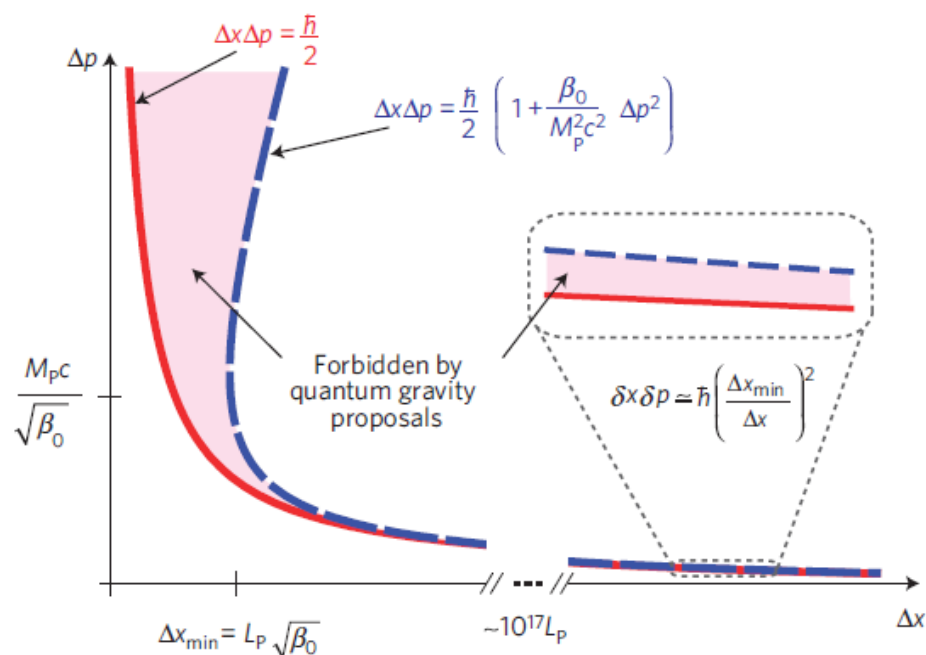


→ $g_{\text{atom}} = 9.804\,923\,2(14) \text{ m/s}^2$

→ no change up to $15 \mu\text{m}$ near surface

Probing Planck-scale physics with quantum optics

Igor Pikovski^{1,2*}, Michael R. Vanner^{1,2}, Markus Aspelmeyer^{1,2}, M. S. Kim^{3*} and Časlav Brukner^{2,4}



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quantum optics researches for studying gravity

Proposed experiment:

test of gravity at short range using Bose-Einstein condensates:

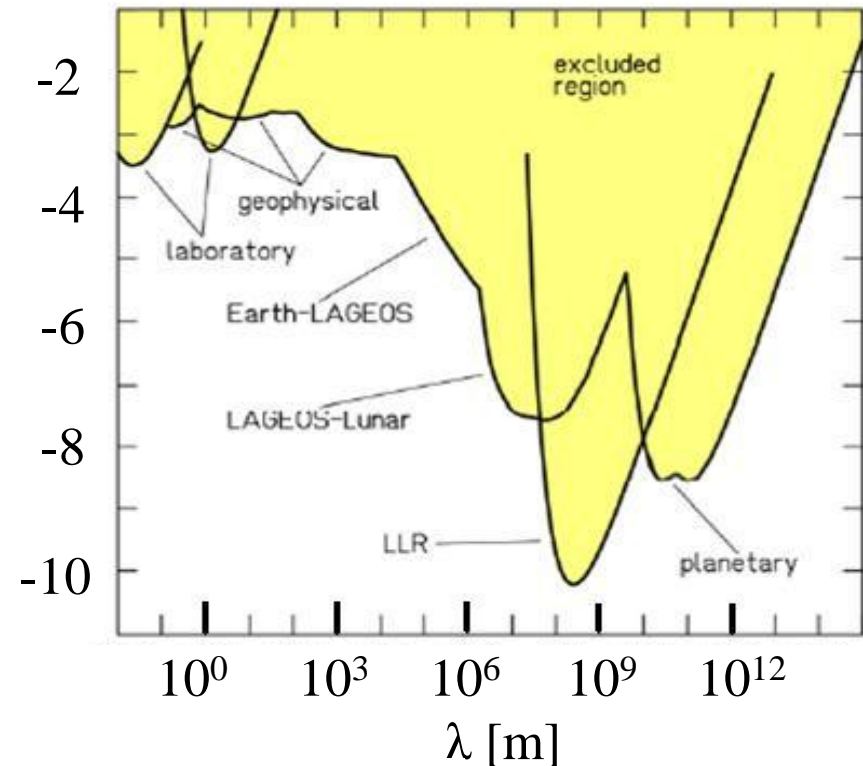
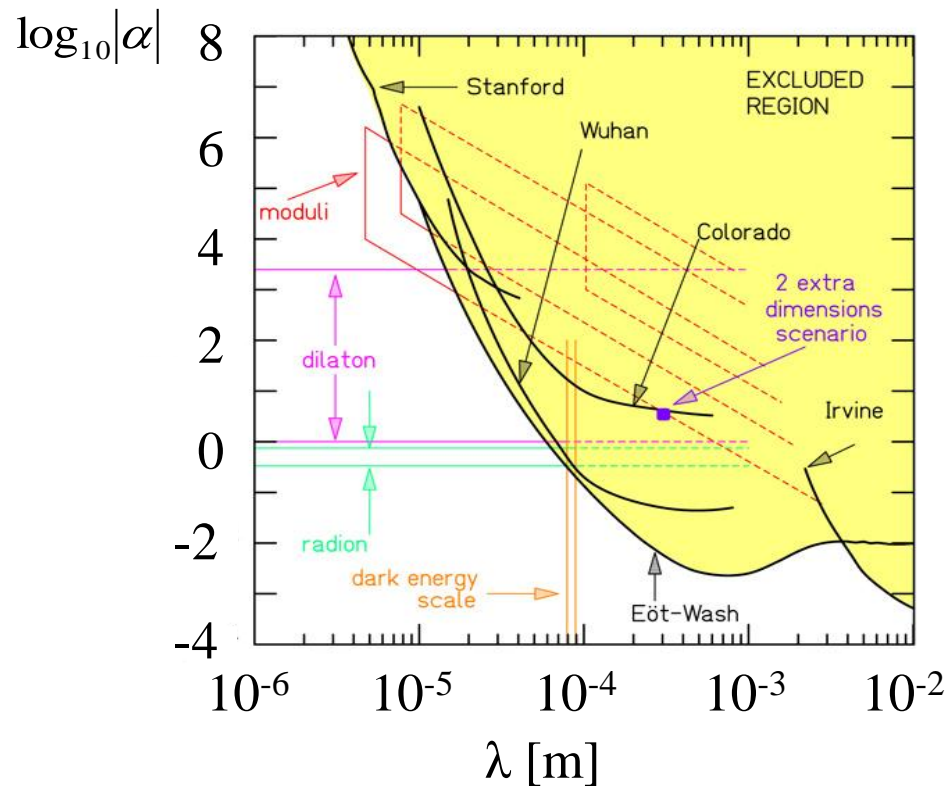
current status and prospects

Test of the Gravitational r^{-2} Law at Short Range

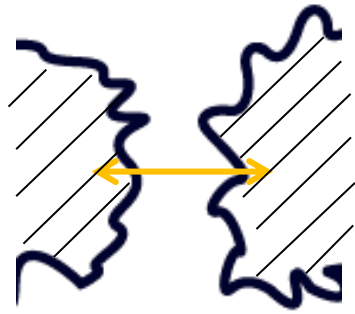
$$V(r) = -\frac{GM_1M_2}{r}$$



$$V(r) = -\frac{GM_1M_2}{r} \left(1 + \alpha e^{-r/\lambda} \right)$$



Gravity at Short Range



“neutron scattering data”

[*PRD*, **77**, 034020 (2008)]

$$|\alpha| \sim 10^{22} \text{ @ } 1 \text{ nm}$$

“New Boson”

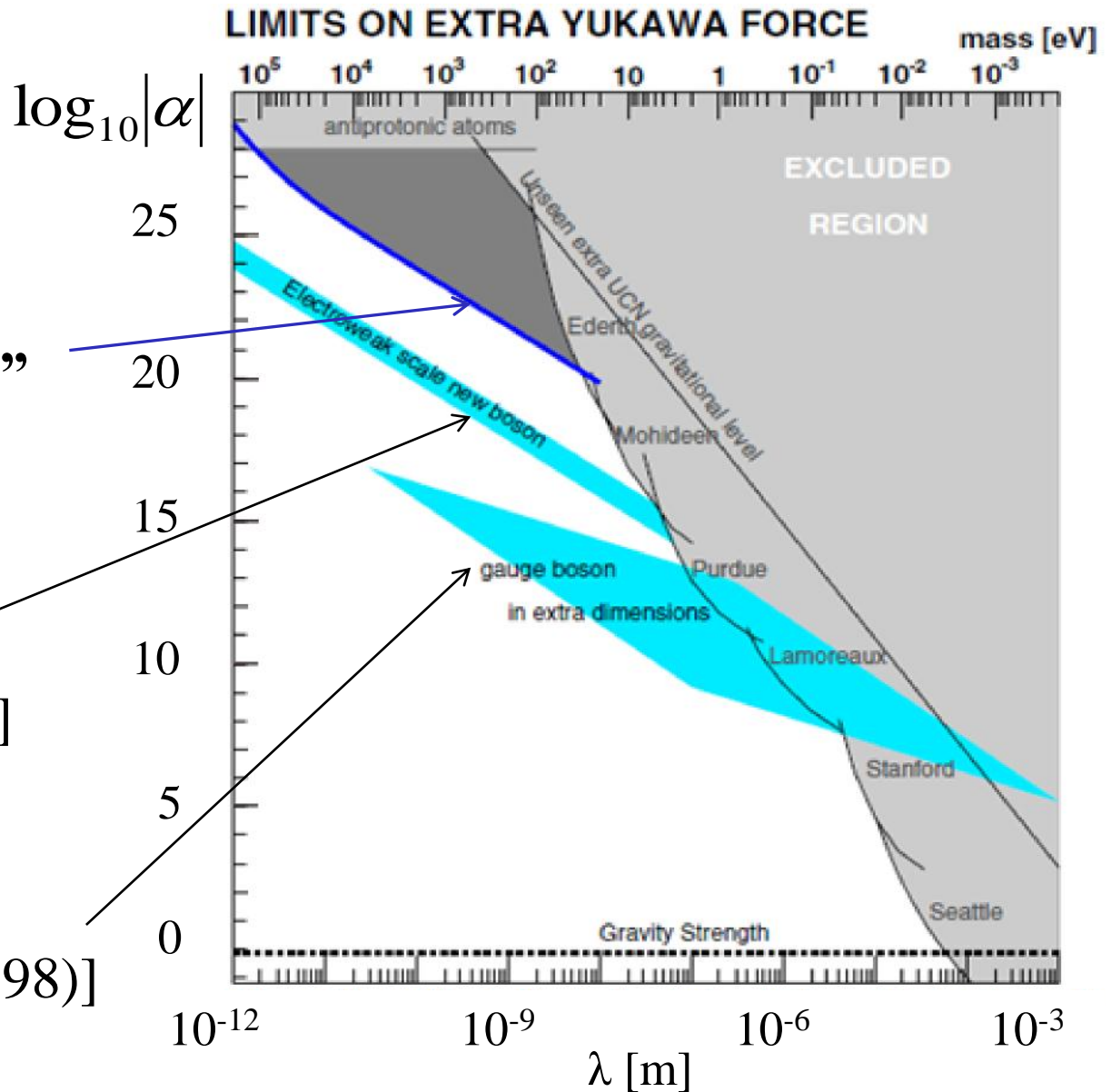
[*PRD*, **75**, 115017 (2007)]

$$|\alpha| \sim 10^{18} \text{ @ } 1 \text{ nm}$$

“Extra-Dimension”

[*Phys. Lett. B*, **429**, 263(1998)]

$$|\alpha| \sim 10^{15} \text{ @ } 1 \text{ nm}$$



Neutron scattering and extra-short-range interactions

V. V. Nesvizhevsky*

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Laboratoire de Physique Subatomique et de Cosmologie, UJF-CNRS/IN2P3-INPG, 53 Av. des Martyrs, Grenoble, France
 (Received 14 November 2007; published 25 February 2008)

The available data on neutron scattering were reviewed to constrain a hypothetical new short-range interaction. We show that these constraints are several orders of magnitude better than those usually cited in the range between 1 pm and 5 nm. This distance range occupies an intermediate space between collider searches for strongly coupled heavy bosons and searches for new weak macroscopic forces. We emphasize the reliability of the neutron constraints insofar as they provide several independent strategies. We have identified a promising way to improve them.

DOI: [10.1103/PhysRevD.77.034020](https://doi.org/10.1103/PhysRevD.77.034020)

PACS numbers: 28.20.Cz, 12.38.Qk

NEUTRON SCATTERING AND EXTRA-SHORT-RANGE ...

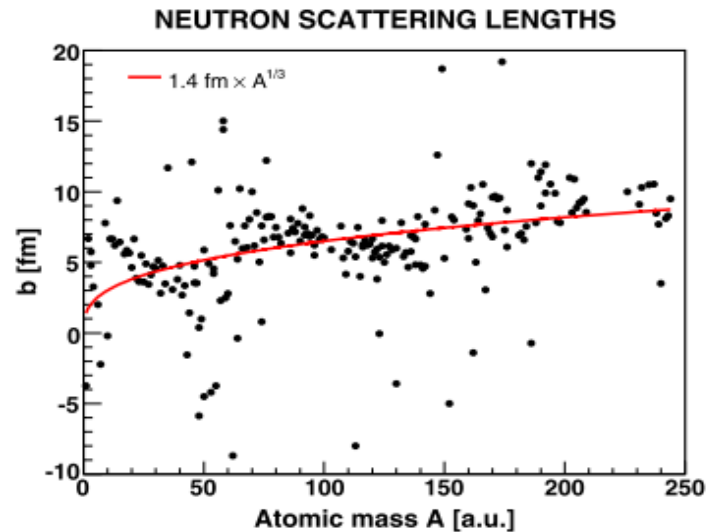


FIG. 1 (color online). Measured scattering lengths as a function of nucleus atomic number.

PHYSICAL REVIEW D 77, 034020 (2008)

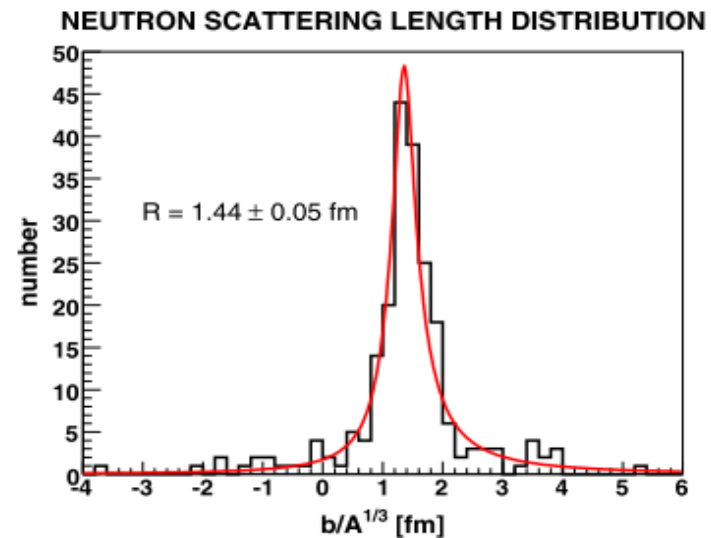
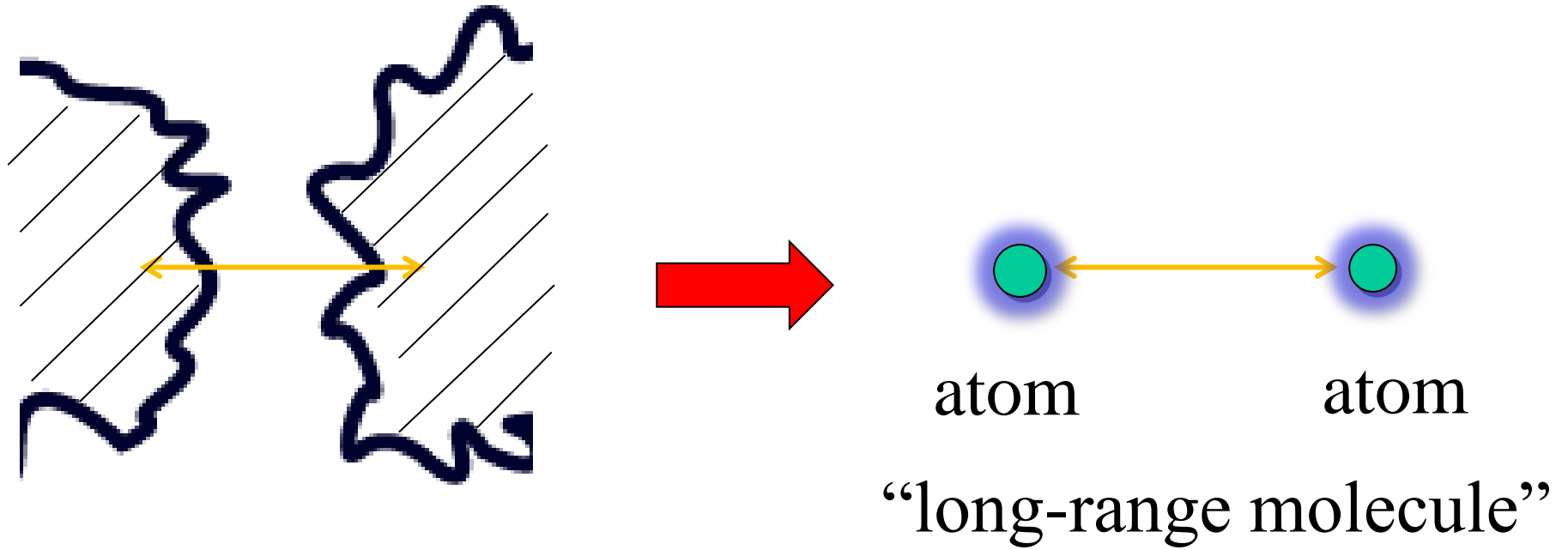
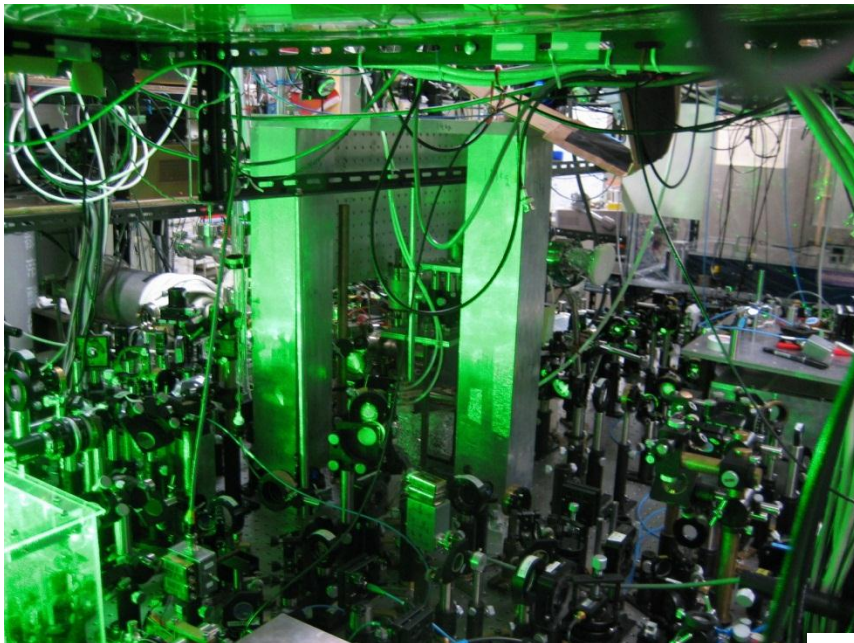


FIG. 2 (color online). This histogram shows the distribution of measured scattering lengths normalized to the radius of the nuclei. The curve corresponds to the random potential model.

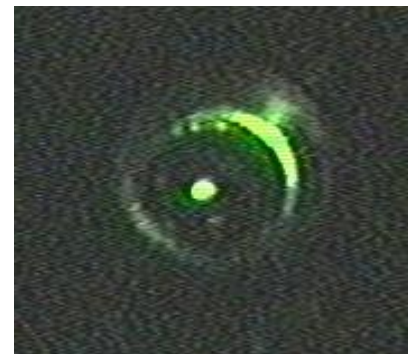
Our Approach : Photo-association



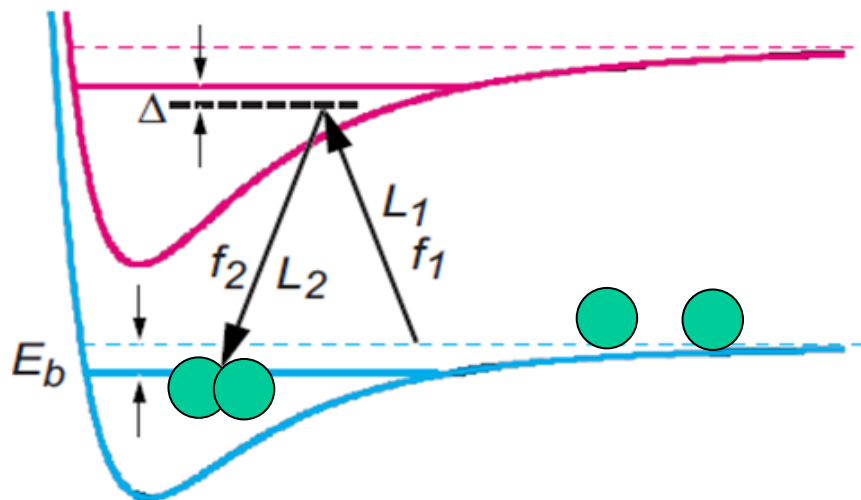
Our Approach : Photo-association



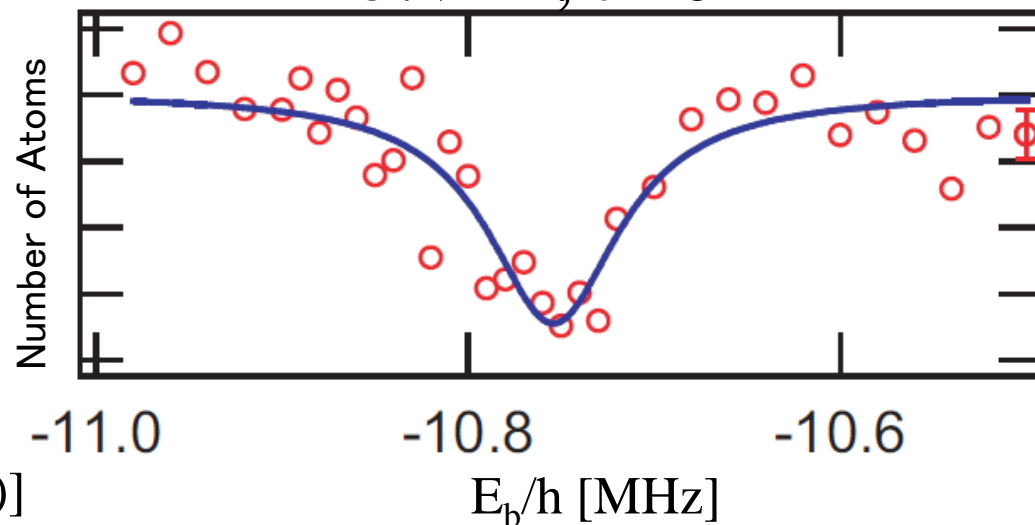
“Magneto-optical Trap”



cold atomic gas at $1 \mu K!$



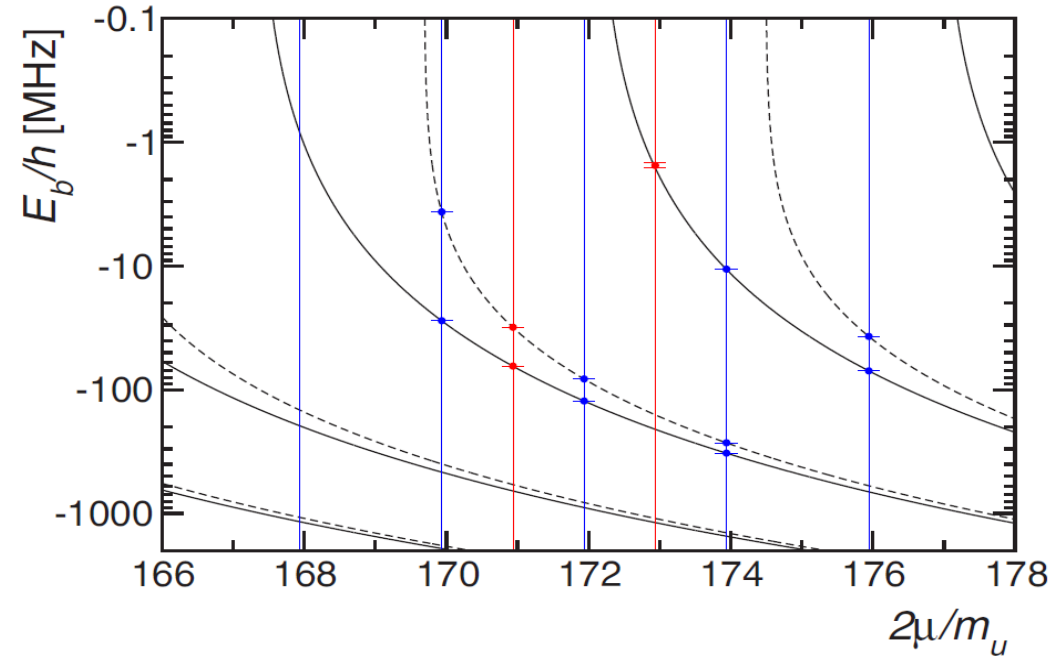
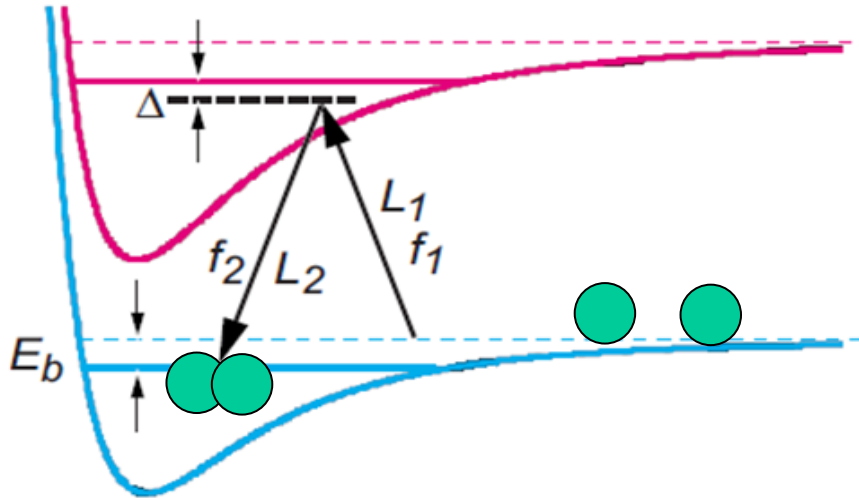
$^{174}\text{Yb}:v=1, J=0$: $\sim 100\text{kHz}$



[M. Kitagawa, et al., PRA **77**, 012719(2008)]

Our Approach : Photo-association

[M. Kitagawa, et al., PRA 77, 012719(2008)]



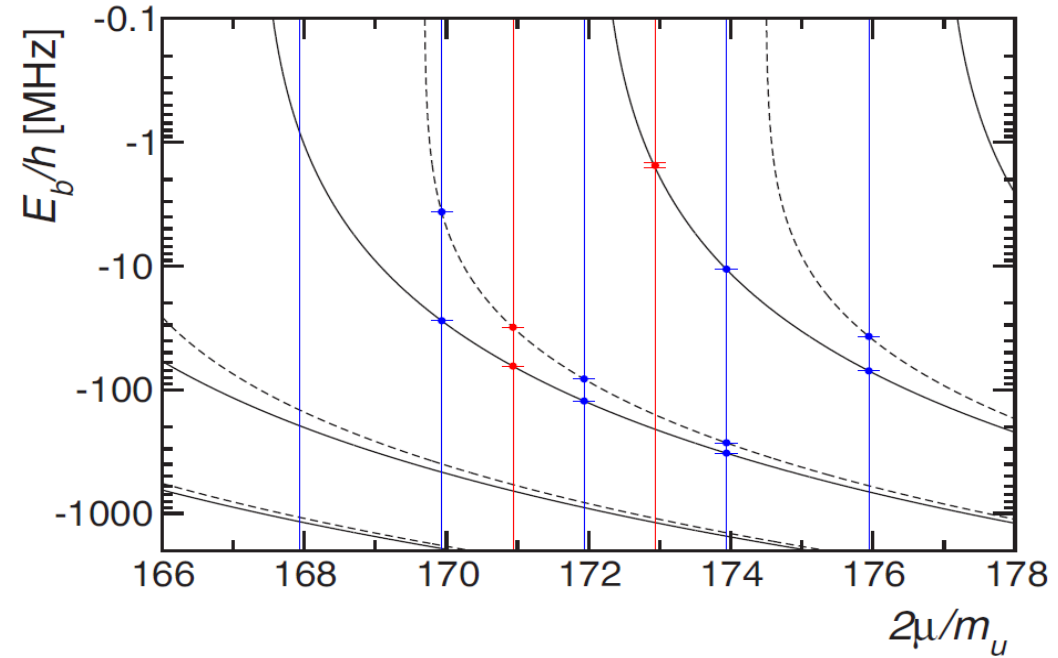
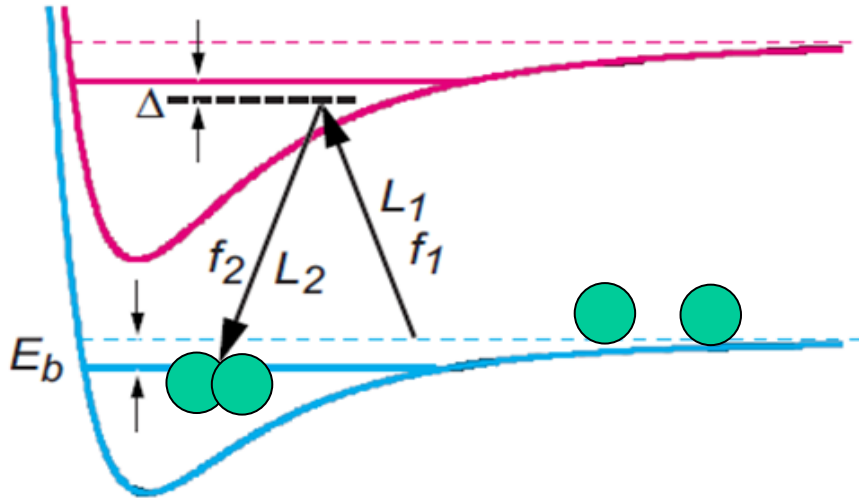
Lenard-Jones-type Potential

$$\Rightarrow V(r) = \frac{C_{12}}{r^{12}} - \frac{C_6}{r^6} - \frac{C_8}{r^8}$$

$$C_6 = 1931.7 E_h a_0^6, \quad C_8 = 1.93 \times 10^6 E_h a_0^8, \quad C_{12} = 1.03041 E_h a_0^{12}$$

Our Approach : Photo-association

[M. Kitagawa, et al., PRA 77, 012719(2008)]



Lenard-Jones-type Potential

$$\Rightarrow V(r) = \frac{C_{12}}{r^{12}} - \frac{C_6}{r^6} - \frac{C_8}{r^8} - \frac{GM_1M_2}{r} \left(1 + \alpha e^{-r/\lambda} \right)$$

$\Delta f = 1 \text{ kHz}$



$|\alpha| < \sim 10^{20}$

@ 1 nm

$$C_6 = 1931.7 E_h a_0^6, \quad C_8 = 1.93 \times 10^6 E_h a_0^8, \quad C_{12} = 1.3041 E_h a_0^{12}$$

Many Advantages of Ytterbium

Nice Atomic Species for this experiment !

- Heavy (N~174)
- Single Molecular Potential :No Hyperfine Structure

Contrary to Alkali Dimers

Insensitivity to magnetic field

- Many Isotopes:

^{168}Yb , ^{170}Yb , ^{171}Yb , ^{172}Yb , ^{173}Yb , ^{174}Yb , ^{176}Yb

Check the mass dependence

- Ultracold Quantum Gases :

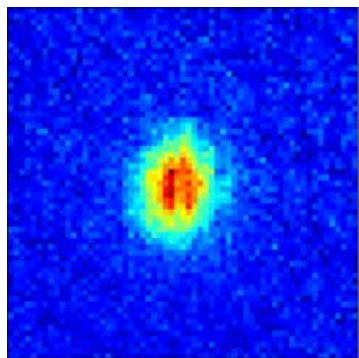
Free from thermal shift and broadening

Quantum Degenerate Gases of Yb

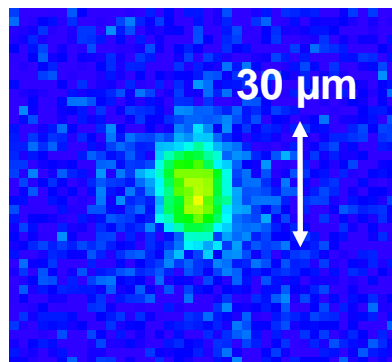
[Y. Takasu *et al.*, PRL **91**, 040404 (2003)] [T. Fukuhara *et al.*, PRA **76**, 051604(R)(2007)]

[S. Sugawa *et al.*, PRA **84**, 011610(R)(2011)]

^{168}Yb (0.13%)

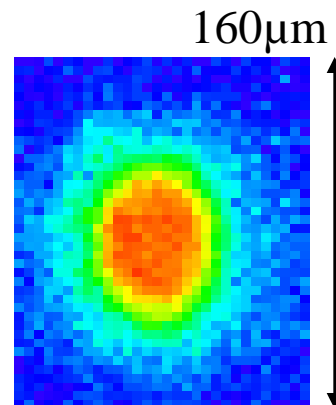


^{170}Yb

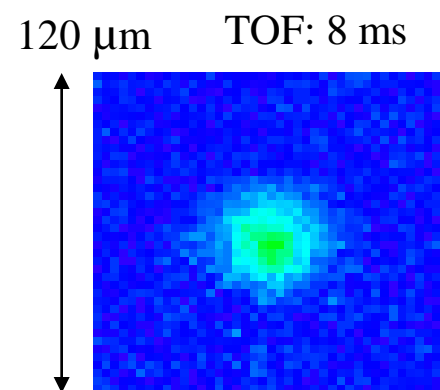


TOF:
10ms

^{174}Yb



^{176}Yb



Fermion

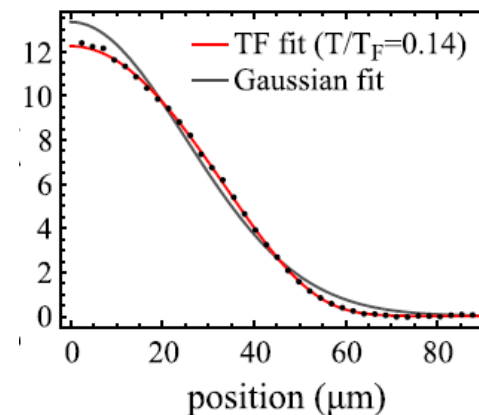
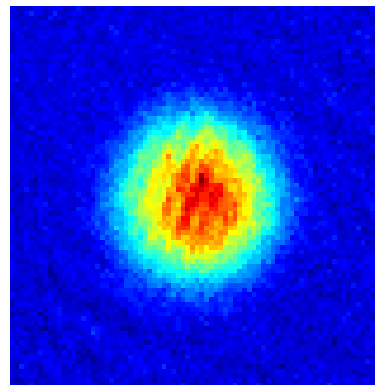
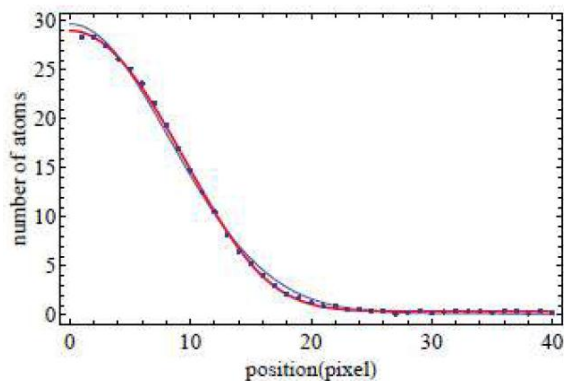
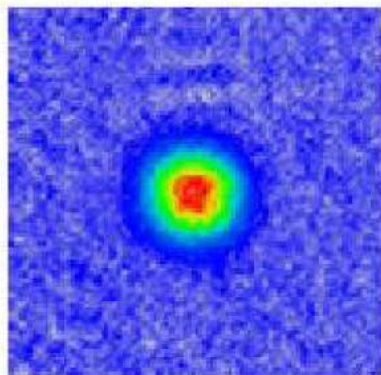
[T. Fukuhara *et al.*, PRL. **98**, 030401 (2007)] [S. Taie *et al.*, PRL**105**, 190401(2010)]

^{171}Yb ($I=1/2$)

$T/T_F = 0.3$

^{173}Yb ($I=5/2$)

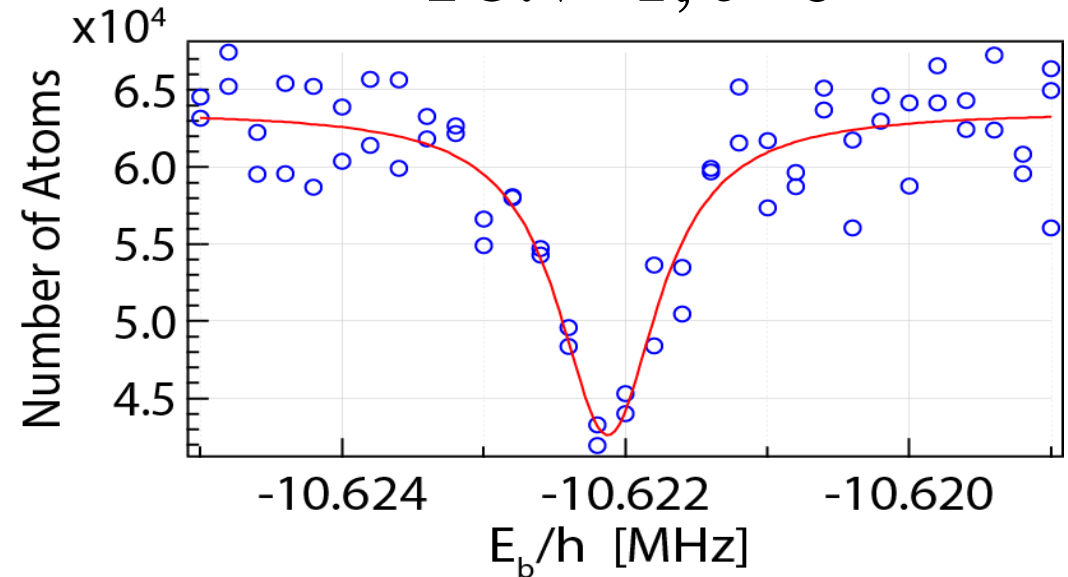
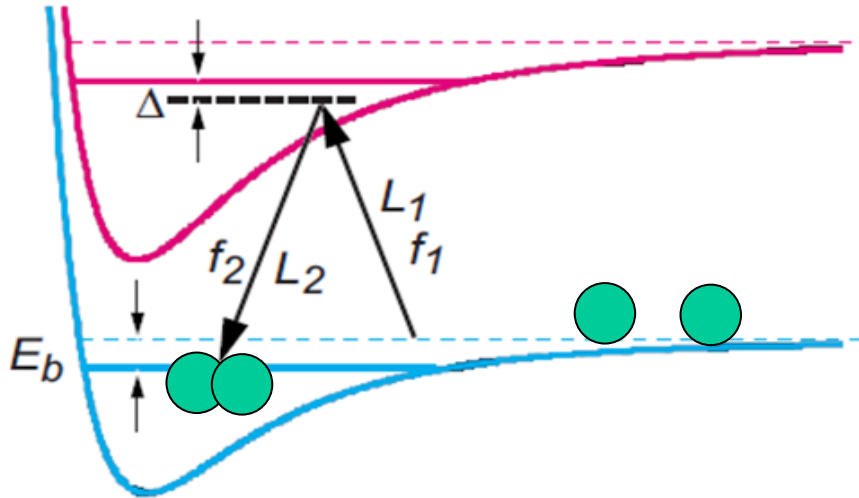
$T/T_F = 0.14$



Our Approach : Photo-association

BEC : ~1kHz !

$^{174}\text{Yb}:v=1, J=0$



Lenard-Jones-type Potential

$$\Rightarrow V(r) = \frac{C_{12}}{r^{12}} - \frac{C_6}{r^6} - \frac{C_8}{r^8} - \frac{GM_1M_2}{r} \left(1 + \alpha e^{-r/\lambda} \right)$$

$\Delta f = 1\text{kHz}$



$|\alpha| < \sim 10^{20}$

@ 1 nm

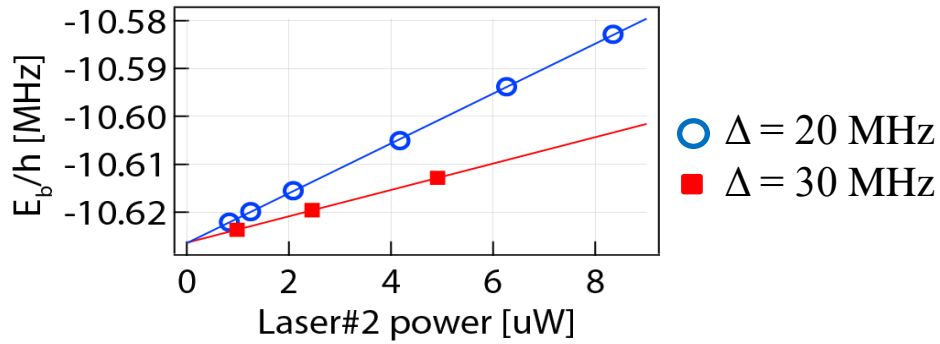
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Evaluation of Systematic Shifts

Light Shift due to Photoassociation Laser

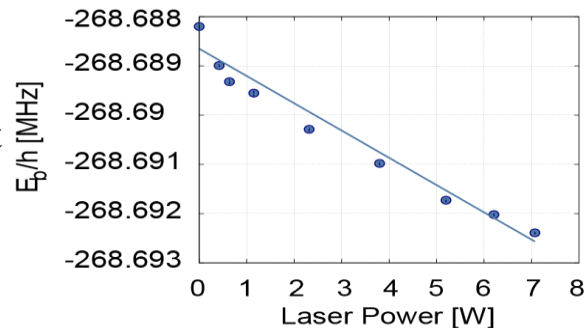
$$\delta_{LS} = \beta \left(\frac{I_1}{\Delta + f_1 - f_2} + \frac{I_2}{\Delta} \right)$$

$$= \alpha_1(\Delta) I_1 + \alpha_2(\Delta) I_2$$



Light Shift due to Optical Trapping Laser

Atoms and Molecules have slightly different polarizabilities

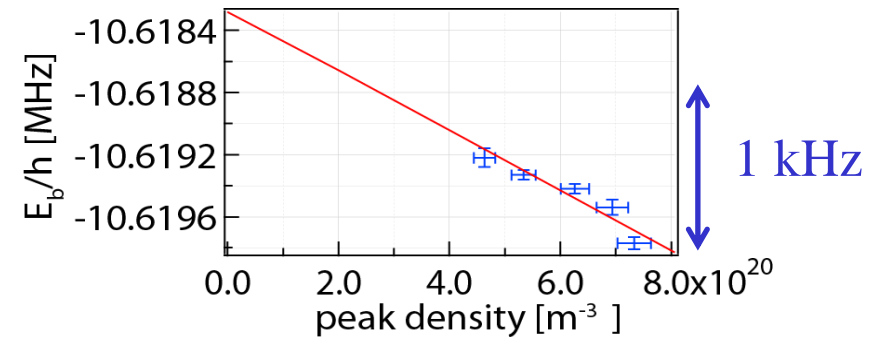
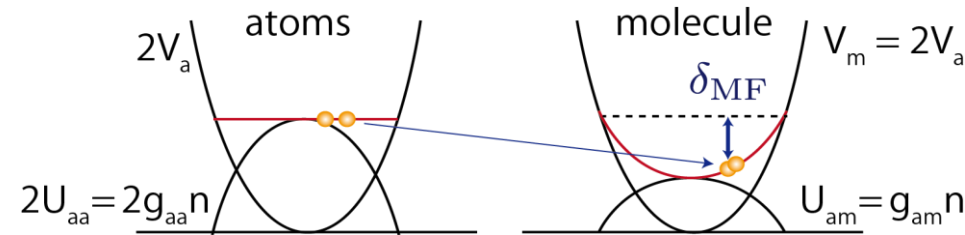


Collision Shift due to Atom-Dimer Collision

$$\delta_{MF} = 2\pi \hbar^2 \left(\frac{2a_{aa}}{\mu_{aa}} - \frac{a_{am}}{\mu_{am}} \right) n_{\text{atom}}(r)$$

a_{am} : scattering length between atom and molecule

$$\{V(r) + g |\psi(r)|^2\} \psi(r) = \mu \psi(r)$$



Experimental Results

Level	Binding energy[MHz]
$^{168}\text{Yb}(v=2, J=0)$	-195.18141(46)
$^{168}\text{Yb}(v=1, J=2)$	-145.53196(48)
$^{170}\text{Yb}(v=1, J=0)$	-27.70024(44)
$^{170}\text{Yb}(v=2, J=0)$	-463.72552(80)
$^{170}\text{Yb}(v=3, J=0)$	-1922.01467(504)
$^{170}\text{Yb}(v=1, J=2)$	-3.66831(32)
$^{170}\text{Yb}(v=2, J=2)$	-398.05626(46)
$^{170}\text{Yb}(v=3, J=2)$	-1817.14074(80)
$^{174}\text{Yb}(v=1, J=0)$	-10.62513(53)
$^{174}\text{Yb}(v=2, J=0)$	-325.66378(98)
$^{174}\text{Yb}(v=3, J=0)$	-1527.88543(34)
$^{174}\text{Yb}(v=1, J=2)$	-268.63656(56)
$^{174}\text{Yb}(v=2, J=2)$	-1432.82493(64)

13 binding energies
with
about **500Hz** accuracy

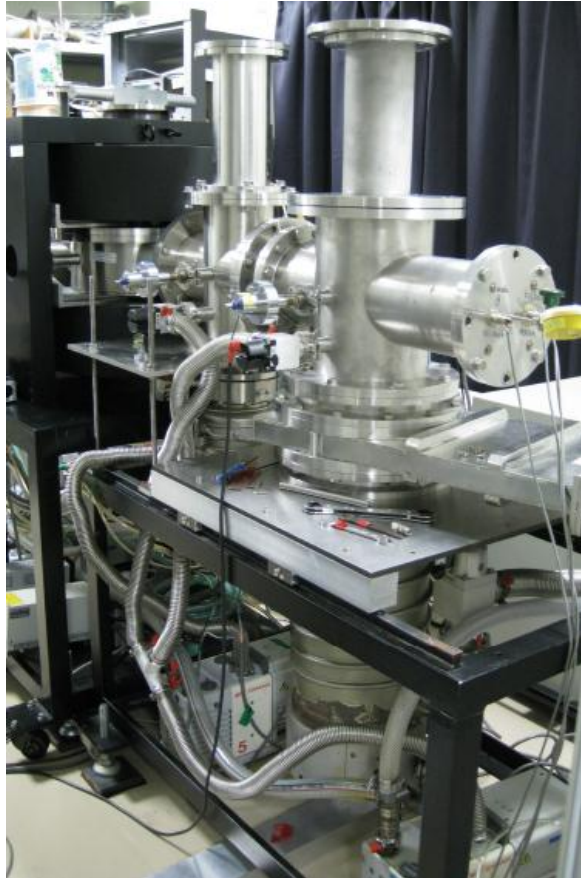
$$\Delta f/f = 2.6 \times 10^{-7}$$

Experimental Results

Level	Binding energy[MHz]	$v=1$	$v=2$	$v=3$
$^{168}\text{Yb}(v=2, J=0)$	-195.18141(46)	-27.70024(44)	-463.72552(80)	-1922.01467(505)
$^{168}\text{Yb}(v=1, J=2)$	-145.53196(48)	-27.72151	-463.78895	-1920.86562
$^{170}\text{Yb}(v=1, J=0)$	-27.70024(44)	-27.22112	-463.77931	-1924.93591
$^{170}\text{Yb}(v=2, J=0)$	-463.72552(80)	no good Fit with Lenard Jones Potential		
$^{170}\text{Yb}(v=3, J=0)$	-1922.01467(504)			
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$^{170}\text{Yb}(v=2, J=2)$	-398.05626(46)	$v=1$	$v=2$	$v=3$
$^{170}\text{Yb}(v=3, J=2)$	-1817.14074(80)	-10.62513(53)	-325.66378(98)	-1527.88543(34)
$^{174}\text{Yb}(v=1, J=0)$	-10.62513(53)	-10.66637	-325.94879	-1527.87270
$^{174}\text{Yb}(v=2, J=0)$	-325.66378(98)	-10.20006	-324.59570	-1527.93747
$^{174}\text{Yb}(v=3, J=0)$	-1527.88543(34)	no good Fit with Lenard Jones Potential		
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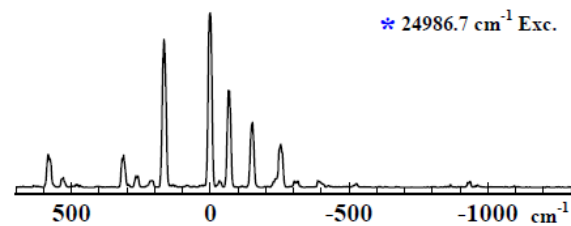
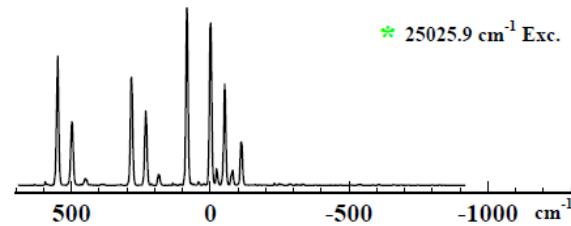
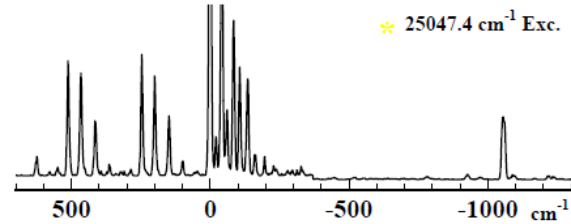
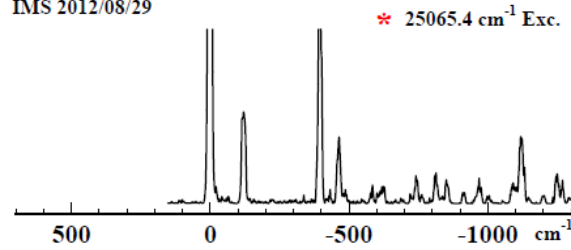
Conventional Molecular Spectroscopy

by M. Baba



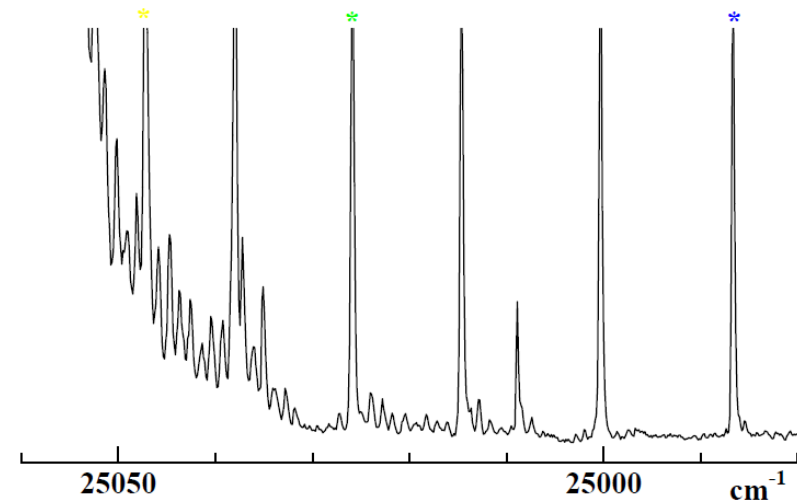
Yb₂ Dispersed Fluorescence Spectra

IMS 2012/08/29



Yb₂ LIF Spectrum

Yb₂-712 2012/08/28 IMS



Plan to do

- Determination of all molecular vibrational binding energies (N=70) with sub-kHz accuracy

Conventional Spectroscopy
using molecular beam:
Collaboration with Prof. Baba

Resonant Ionization Spectroscopy
using cold Photo-associated molecule:
New construction

- Determination of molecular potential energies with quantum chemical calculation

BO Correction, Nuclear Finite-size effect:
Collaboration with Prof. Hutson,
Dr. Abe

Potential Fitting:
Collaboration with Dr. P. Julienne
Dr. R. Ciulylo, M. Borkowski

Thank you very much for attention



16 August Mount Daimonji at Kyoto